

# 1 Estimating the urban atmospheric boundary layer height from 2 remote sensing applying machine learning techniques

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## 11 Abstract

12 This study proposes a new methodology to estimate the Atmospheric Boundary Layer Height (ABLH),  
13 discriminating between Convective Boundary Layer and Stable Boundary Layer heights, based on the machine  
14 learning algorithm known as Gradient Boosting Regression Tree. The algorithm proposed here uses a first  
15 estimation of the ABLH derived applying the gradient method to a ceilometer signal and several meteorological  
16 variables to obtain ABLH values comparable to those derived from a microwave radiometer. A deep analysis of  
17 the model configuration and its inputs has been performed in order to avoid the model overfitting and ensure its  
18 applicability. The hourly and seasonal values and variability of the ABLH values obtained with the new algorithm  
19 have been analyzed and compared with the initial estimations obtained using only the ceilometer signal. Mean  
20 Relative Errors (MRE) between the ABLH estimated with the new algorithm and microwave radiometer show a  
21 daily pattern with their highest values during the night-time (stable situations) and their lowest values along the  
22 day-time (convective situations). This pattern has been observed for all the seasons with MRE ranging between -  
23 5% and 35%. This result notably improves those ABLH values derived by applying the gradient method to  
24 ceilometer data during convective situations and enables the Stable Boundary Layer height detection at night and  
25 early morning, instead of only Residual Layer top height. Finally, the model performance has been directly  
26 validated in three particular cases: clear-sky day, presence of low-clouds and dust outbreak event. In these three  
27 particular situations, ABLH values obtained with the new algorithm follow the pattern obtained with the  
28 microwave radiometer presenting very similar values, thus confirming the good model performance. In this way  
29 it is feasible by the combination of the proposed method with gradient method, to estimate Convective, Stable and  
30 Residual Boundary Layer height from ceilometer data and surface meteorological data in extended network that  
31 include ceilometer profiling.

## 32 1 Introduction

33 The Atmospheric Boundary Layer (ABL) is defined as the part of the troposphere that is directly influenced by  
34 the presence of the Earth's surface, and responds to surface forcings with a timescale of about an hour or less  
35 (Stull, 1988). The ABL is the atmospheric region directly affected by turbulent and evapotranspiration processes  
36 and where the air pollutants are dispersed (Stull, 1988). The characteristics of the ABL, and particularly, the ABL  
37 height (ABLH), play a fundamental role in numerous atmospheric areas such as weather forecasting, air quality  
38 and/or numerical modeling (e.g. Cheng et al., 2011).

39 The estimation of the ABLH with high temporal resolution is not an easy task, due mainly to its high variability  
40 throughout its daily cycle. Thus, based on an ideal scenario, some instants after the sunrise, the ground surface  
41 temperature begins to increase, due to the positive net radiative fluxes. Such a phenomenon causes the warming  
42 of air masses located at low heights favoring the convective process, and the heat transfer from the surface to  
43 upper atmospheric layers in the troposphere. This process generates a layer known as Convective Boundary Layer  
44 (CBL). Just before the sunset, the CBL becomes a layer called Residual Layer (RL), which is stably stratified and  
45 contains the characteristics from the previous CBL. In conjunction with this process arises from the ground a  
46 thermally stratified layer and endowed of lower heights (in comparison with RL and CBL), denominated Stable  
47 Boundary Layer (SBL).

48 In the last years remote sensing systems, such as elastic lidars (e.g. Toledo et al., 2017; Bravo-Aranda et al., 2017;  
49 Moreira et al., 2019; Vivone et al., 2021), ceilometers (e.g. Haeffelin et al., 2012; Caicedo et al., 2017; Lee et al.,  
50 2019; Uzan et al., 2020; Moreira et al., 2020a; Jiang et al., 2021), Doppler lidars (e.g. Manninen et al., 2018;  
51 Marques et al., 2018; Moreira et al., 2019) and microwave radiometers (e.g. Cimini et al., 2013; Bravo-Aranda et  
52 al., 2017; Moreira et al., 2020a; Jiang et al., 2021) have been widely used to characterize the ABLH. Among these  
53 remote sensing systems, ceilometers have the advantage to be a low-cost and low-maintenance system that  
54 monitors aerosol and clouds layers (Lee et al., 2019). Such characteristics have favored the creation of national  
55 (e.g., Automated Lidar-Ceilometer network – ALICENet (Haefele et al., 2016); Unified Ceilometer Network -  
56 UCN (National Research Council, 2009)) and international networks (e.g., EUMENET-Profiling Program  
57 [<https://www.eumetnet.eu/>]; E-PROFILE [<https://e-profile.eu/>]; Iberian Ceilometer Network - ICENET) (Cazorla  
58 et al., 2017), which have been dedicated to standardize and expand the activities of ABL monitoring by ceilometer  
59 data.

60 Ceilometers have been applied in many previous works related to ABLH detection, which vary from short-term  
61 (e.g. Helmis et al., 2012; Bruine et al., 2017; Caicedo et al., 2017) to long-term studies (e.g. Stachlewska et al.,  
62 2012; Schween et al., 2014; Moreira et al., 2020), and various mathematical algorithms such as, vertical gradients  
63 (Emeis et al., 2008), wavelet covariance transform (Baars et al., 2008; Granados-Muñoz et al., 2012), STRAT  
64 (STRucture of the ATmosphere) [application of first derivative of the Gaussian filter on Range Corrected Signal  
65 (RCS) profile] (Morille et al., 2007), STRAT-2D [it has same structure of STRAT and includes an edge detection  
66 method based on both vertical and temporal gradients of RCS] (Haeffelin et al., 2012), STRAT+ [combination  
67 of radiosoundings information and Canny edge detection applied to gradient and variance profiles of RCS] (Pal  
68 et al., 2013), PathfinderTURB [it combines the strength points of gradient and variance of RCS methods and  
69 addresses the layer attribution problem by adopting a geodesic approach] (Poltera et al., 2017), or COBOLT  
70 (COntinuous BOundary Layer Tracing) [a time-height tracking procedure] (Geiß et al., 2017) have been  
71 developed in order to improve the ABLH values derived from them. In spite of this, there are still limitations in  
72 the application of ceilometers for ABLH monitoring. Special difficulties occur in cases considered as complex  
73 such as rainy situations, presence of low clouds, and dust outbreaks. In these situations, the abrupt changes of the  
74 aerosol vertical profile notably differ from the idealized profile on which most of the ABLH detection methods  
75 are based. Although some methods have been proposed to improve the ABLH detection from lidar data in the  
76 situations mentioned above (Bravo-Aranda et al., 2017; Liu et al., 2018), the use of only one wavelength and/or  
77 low signal-to-noise ratio make it difficult to apply such techniques in ceilometers. Another weakness in the  
78 application of ceilometers to obtain ABLH is the difficulty for discriminating between the RL top height (RLH)

79 and SBL height (SBLH) during stable periods (Moreira et al., 2020a). This limitation comes from the basis of the  
80 detection procedure applied to ceilometers, based on the vertical profile of the atmospheric aerosol that prevents  
81 the detection of the top of the thermal inversion (SBLH) in this situation. Having in mind these facts, there is still  
82 room for some improvements in the ABLH retrieval with ceilometers on the basis of alternative data processing  
83 of the ceilometer's output.

84 Machine learning techniques have been widely applied in the environmental sciences during the last years (e.g.  
85 Cadeddu et al., 2009; McGovern et al., 2017; Bonnin et al., 2018; Vassalo et al., 2020; Moreira et al., 2021). These  
86 ML techniques can account for complex relationships on atmospheric processes and have been successfully  
87 applied in several atmospheric areas, ranging from the estimation of atmospheric parameters such as the mixing  
88 layer height (Bonin et al., 2018) or the analysis of sky-camera images to characterize the aerosol layer (Cazorla  
89 et al., 2008; Cazorla et al., 2009) to predict pollutants concentration (Moreira et al., 2021). Particularly for the  
90 estimation of the ABLH, Jiang et al. (2021) applied machine learning combined GPS radio occultation technology  
91 to build a simulation model to estimate the ABLH, providing reliable results for several months. Krishnamurthy  
92 et al. (2021) proposes a method based on Random Forest algorithm to estimate the ABLH from meteorological  
93 and Doppler lidar data. Such an algorithm provides an improvement of 50%, in the CBLH detection during clear  
94 sky or cloudy conditions, in comparison with a method based on vertical wind speed profiles.

95 Thus, the main objective of this study is to propose a machine learning algorithm to improve the ABLH  
96 estimations obtained from a ceilometer. To this aim, a Gradient Boosting Regression Trees (GBRT) algorithm  
97 has been trained using as input the ABLH values derived from a ceilometer, surface meteorological data and  
98 ABLH values derived from a co-located microwave radiometer (Moreira et al., 2018; Moreira et al., 2020a). From  
99 this algorithm it is possible to estimate the height of CBL and SBL combining ceilometer and meteorological  
100 surface data. Therefore, application of such methodology can expand ceilometer data applicability, so that it is  
101 possible to discriminate the three main ABL sublayers (CBL, SBL and RL) without acquiring expensive  
102 instruments. These ABLH values derived from the microwave radiometer have been the reference dataset for both  
103 the fitting and validation analysis. The model performance has been assessed analyzing its temporary and seasonal  
104 variability as well as the dependence of its residuals against several meteorological variables. Finally, the model  
105 has been directly validated in three particular cases (clear-sky day, presence of low-clouds and dust outbreak  
106 event).

107 The paper is organized as follows. First, the experimental site and the instrumentation used in this study have been  
108 described in Section 2. Then, in Section 3 the development and set-up of the machine learning algorithm here  
109 proposed are presented. Next the results of a seasonal analysis as well as the analysis of particular cases are shown  
110 in Section 4, while the main conclusions of this study are discussed in Section 5.

## 111 **2 Experimental site and instrumentation**

112 The measurements analyzed in this study were recorded at the University of Granada (UGR) station located on  
113 the roof of the Andalusian Institute of Earth System Research (IISTA-CEAMA) at Granada (37.164° N, 3.605°  
114 W, 680 m a.s.l.). These facilities are managed by the Atmospheric Physic Research Group (GFAT) and they are  
115 part of the observatory AGORA (Andalusian Global ObservatoRy of the Atmosphere) in the framework of

116 ACTRIS (Aerosol, Clouds and Trace Gases Research Infrastructure) and of the Iberian Ceilometer Network  
117 (ICENET) (Cazorla et al., 2017).

118 Granada is a medium sized non-industrialized city in the West Mediterranean region, at the Southeast of Spain,  
119 and presents a large seasonal temperature range associated with its Mediterranean-continental conditions. The city  
120 is characterized by cool winters and hot summers with the most humid period from late autumn to early spring  
121 (AEMET, 2015). This region is usually affected by mineral dust outbreaks from the Sahara desert in summer and  
122 spring (e.g. Guerrero-Rascado et al., 2008, 2009; Bravo-Aranda et al., 2015), and some extreme events have also  
123 occurred in winter (Cazorla et al., 2017; Fernández et al., 2019), but also for more local sources of aerosol particles  
124 such as traffic, domestic-heating or biomass burning in winter time (Titos et al., 2012, 2017). From roughly  
125 February to July, primary biological aerosol particles (pollen-type) are present in the region (e.g., Cariñanos et  
126 al., 2021). To a lesser extent, the area is also affected by advected fresh and aged smoke mainly from the Iberian  
127 Peninsula (Alados-Arboledas et al., 2011) and from North America (Ortiz-Amezcuca et al., 2017), respectively.  
128 The combination of all these factors highly affect the local meteorology, and, therefore the ABL detection (Stull,  
129 1988).

130 A ceilometer Jenoptik model CHM15k was operated at the UGR station. This instrument measures the  
131 backscattered signal of a pulsed Nd:YAG laser emitting at 1064 nm, with an energy per pulse of 8.4  $\mu$ J, a repetition  
132 frequency in the range of 5–7 kHz and a laser beam divergence less than 0.3 mrad. The backscattered signal is  
133 received by a telescope with a field of view of 0.45 mrad. The spatial and temporal resolution used were 15 m and  
134 15 s, respectively. The complete overlap of the instrument is found around 1500 m above a.g.l. and its overlap is  
135 90% at 555 m a.g.l., in accordance with the overlap function provided by the manufacturer (Cazorla et al., 2017).  
136 This equipment has been operating continuously since December 2012 and it is part of the Iberian Ceilometer  
137 Network (ICENET), an initiative of the Atmospheric Physics Group of the University of Granada (Cazorla et al.,  
138 2017). Measurements recorded with this instrument were employed to derive initial estimations of the ABLH,  
139  $ABLH_{CEIL}$ , as input (feature) of the machine learning algorithm. The range of values to  $ABLH_{CEIL}$  [200 – 4500  
140 m] (Table 1) is based on a previous long-term study (2012-2016) presented in Moreira et al. (2020a).

141 The surface meteorological dataset consists of 1-min data of air temperature (T), relative humidity (RH),  
142 atmospheric pressure (P), and wind speed (WS) measured at the roof of the UGR station facilities and covering  
143 the whole analyzed period 2015-2017. T and RH at this station were monitored by a HMP60 probe manufactured  
144 by Vaisala. This probe has an accuracy of  $\pm 0.6$  °C and 2% for T and RH measurements, respectively. In this station  
145 WS was measured by an anemometer model 05103, manufactured by Campbell Scientific, with an accuracy of  
146  $\pm 0.3$  m/s. Simultaneously, P was monitored by a Vaisala PTB110 barometer with a silicon capacitive sensor  
147 specially designed to guarantee accurate ( $\pm 0.3$  hPa at +20 °C) and stable ( $\pm 0.1$  hPa/year) measurements. Global  
148 horizontal irradiance (G) in the range 280-2800 nm was measured by a CM-11 pyranometer manufactured by  
149 Kipp & Zonen while downward infrared irradiance (IR) in the range of 4000-50000 nm is measured by a Precision  
150 Infrared Radiometer (PIR) manufactured by EPPLEY. Both instruments comply with the specifications for the  
151 first-class WMO pyranometer classification with an accuracy below  $\pm 5$  W/m<sup>2</sup> for daily measurements. All these  
152 sensors operated following the WMO standard protocols and procedures (WMO, 2013). These measurements and

153 magnitudes derived from them were employed as input for the machine learning algorithm developed in this study  
154 as both input (features).

155 Co-located to the ceilometer, a ground-based passive microwave radiometer (MWR), model RPG-HATPRO G2  
156 (Radiometer Physics GmbH) was operating in the scanning mode in automatic and continuous mode since  
157 November 2011 as part of MWRnet [<http://cetemps.aquila.infn.it/mwrnet/>] (Rose et al., 2005; Caumont et al.,  
158 2016). This instrument measures the sky brightness temperature with a radiometric resolution between 0.3 and  
159 0.4 K root mean square error at 1 s integration time. The MWR uses direct detection receivers within two bands,  
160 22-31 GHz (water vapor - K band) and 51-58 GHz (oxygen - V band), for deriving RH and T profiles, respectively,  
161 by inversion algorithms described in Rose et al. (2005). Both profiles have a range resolution varying between 10  
162 and 200 m in the first 2 km and varying between 200 and 1000 m up to 10 km (Navas-Guzmán et al., 2014). This  
163 change in the profile resolution is associated with an exponential decrease with height of the MWR weighting  
164 functions (Spänkuch et al., 1996). The measurements recorded with this instrument were employed to derive the  
165 reference values (target) of the ABLH,  $ABLH_{MRW}$ . In the same way of the  $ABLH_{CEIL}$ , the range of values to  
166  $ABLH_{MWR}$  [200 – 4500 m] (Table 1) is based on Moreira et al. (2020a). The application of MWR data to ABLH  
167 detection have been extensively validated with other instruments such as: Doppler lidar (Moreira et al., 2018;  
168 Moreira et al., 2020b), elastic lidar (Granados-Muñoz et al., 2012; Bravo-Aranda et al., 2017; Moreira et al., 2018;  
169 Moreira et al. 2020a) and radiosoundings (Bedoya-Velásquez et al., 2019). Particularly,  $ABLH_{MRW}$  has shown to  
170 be less influenced by presence of clouds (Moreira et al., 2020a) and decoupled aerosol layers (Bravo-Aranda et  
171 al., 2017) compared with other devices. Moreover, the MWR temporal resolution of 2 min guarantees the volume  
172 of data required for the development of the machine learning algorithm.

173 Finally, a database of hourly values of all these variables, listed in Table 1, were built for the period analyzed in  
174 this study, which encompasses three entire years from 2015 to 2017. This final dataset was split in two subsets:  
175 (1) a training subset, formed by measurements recorded along 2015 and 2016, and (2) a validation subset,  
176 composed by measurements taken along 2017.

## 177 **3 Methodology**

### 178 **3.1 Gradient Boosted Regression Trees**

179 The Gradient Boosting Regression Trees (GBRT) is a supervised non-parametric machine learning technique  
180 widely applied in classification and regression problems (e.g., Friedman 2001; Li et al. 2008; Ye et al. 2009; Chen  
181 et al. 2015; Baturynska et al. 2020). The idea behind boosting is to sequentially fit multiple ‘weak learners’, that  
182 is, simple models that perform relatively poorly with low accuracy (Friedman, 2001). In each iteration, a new  
183 model is proposed using information from the previous model trying to learn from its mistakes and improving  
184 iteration by iteration. In the case of GBRT, the ‘weak learners’ are decision tree models with very few branches.  
185 Because GBRT operates with small models training sequentially, it is a faster process and requires lower memory  
186 consumption than other machine learning techniques such as Random Forests. Additionally, GBRT does not  
187 require the application of advanced normalization techniques on its inputs and enables a combination of different  
188 numerical and categorical data as input. Similarly to the development of other types of atmospheric models, this  
189 machine learning technique requires both independent variables and reference data to build the model. Particularly

190 in the machine learning vocabulary independent variables are named as features while the reference data is  
191 denoted as target. The variables used in this study will be detailed described in the next sections.

192 Figure 1 shows a flowchart that briefly describes the main steps of how an ensemble of trees is created by the  
193 GBRT algorithm. The ensemble consists of  $M$  trees built one-by-one. Thus, a first decision tree ( $Tree_1$ ) is trained  
194 using the feature matrix,  $X$  ( $ABLH_{CEIL}$  and meteorological variables), and the target variable  $y$  ( $ABLH_{MRW}$ ). The  
195 predictions of  $Tree_1$  ( $F_1(X)$ ) are used to determine the pseudo-residual errors ( $r_1$ ) of the training set applying the  
196 loss function  $L$  (Root Mean Square Error in our case). After that, a second decision tree ( $Tree_2$ ) is trained using  $X$   
197 and  $r_1$ , which is the new target variable, as inputs. From the  $Tree_2$  predictions ( $F_2(X)$ ) the new pseudo-residual  $r_2$   
198 are computed and used as input to build an improved third tree. Such a process is repeated  $M$  times until the  
199 residuals are minimized and the improvement between consecutive trees is negligible. Finally,  $F_M(X)$  is obtained  
200 as the combination of the predicted values provided by each m-tree:

$$201 \quad F_M(X) = F_0(X) + F_1(X) + \dots + F_{m-1}(X) + F_m(X) \quad (1)$$

202 From Fig. 1 it is possible to observe that as more trees are added to the model, there is a progressive tendency to  
203 reduce errors in predictions. A more detailed description of this process, including the most relevant mathematical  
204 aspects, is given in Appendix 1.

## 205 **3.2.- GBRT set up**

### 206 **3.2.1.- Inputs for the GBRT: features and target variables**

207 The features initially selected to build the GBRT algorithm have been the ABLH obtained from the aerosol vertical  
208 profiles measured with the ceilometer,  $ABLH_{CEIL}$ , and set of near-surface meteorological variables which  
209 influence on the ABLH as reported in previous works (e.g. Stull, 1988; Georgoulas et al., 2009; Granados-Muñoz  
210 et al., 2012; Haeffelin et al., 2012 Allabakash and Lim, 2020; Rey-Sanchez et al., 2021)).  $ABLH_{CEIL}$  have been  
211 obtained applying the gradient method (Flamant et al., 1997) on the 1-hour averaged range corrected signal ( $R\acute{C}S$ ).  
212 Considering the existence of an intense reduction in the aerosol load in the transition region between the ABL and  
213 the Free Troposphere (FT), this methodology estimates the ABLH as the height ( $z$ ) where the minimum in the  
214 gradient of the  $R\acute{C}S$  profile is detected (Moreira et al., 2020a). Rain cases were flagged by an empirical threshold  
215 and removed (Moreira et al., 2020a). This methodology has been widely applied to numerous ceilometers  
216 belonging to national or international networks such as E-PROFILE (Haeefe et al., 2016) or ICENET (Cazorla  
217 et al., 2017).

218 The initial near-surface meteorological dataset is composed of WS, T, P, RH, G and NR. On one hand, several  
219 authors have reported significant correlations between ABLH and near-surface values of WS, T, P and RH  
220 (Georgoulas et al., 2009; Wang et al., 2009; Allabakash and Lim, 2020; Krishnamurthy et al., 2021). On the other  
221 hand, G accounts for the total energy reaching the surface while NR is a proxy of the brightness temperature of  
222 the atmosphere, highly correlated with its composition. The solar zenith angle (SZA), the hour of the day (H) and  
223 the season (S), have been also included as inputs in order to account for the Sun position and possible daily and  
224 seasonal dependencies. Additionally, the clearness index (kt), estimated as the ratio between the solar radiation at  
225 the top of the atmosphere and the global solar irradiance on the Earth's surface, has been also initially considered  
226 as a proxy of atmospheric transmissivity and cloudiness, respectively. In addition to their influence of these

227 variables on the ABLH they have been chosen because of their wide availability through national and international  
228 meteorological and radiation networks as well as from reanalysis and satellite databases.

229 In this study, the reference values or target, also included as input in the GBRT algorithm, are the ABLH values  
230 obtained from the MWR ( $ABLH_{MWR}$ ). Such an ABLH is calculated from the potential temperature profile in an  
231 algorithm that combines gradient and parcel methods, for stable and convective situations, respectively. This  
232 technique has been previously validated with respect to co-located elastic lidar (Granados-Muñoz et al., 2012;  
233 Bravo-Aranda et al., 2017; Moreira et al. 2018) and Doppler lidar (Moreira et al. 2018; Moreira et al., 2020a)  
234 presenting in both comparisons reasonable correlations with a coefficient of determination,  $R^2$ , above 0.7. In a  
235 recent study, Bedoya-Velásquez et al. (2019) performed a validation of MWR data comparing them with 5 years  
236 of radiosonde data at Granada-Spain. Such analysis demonstrated a very low bias in MWR profiles respects  
237 radiosoundings, being this bias from 1.8 to  $-0.4$  K with and standard deviation of 1.1 K for the temperature profiles  
238 and from 3.0 to  $-4.0\%$  with and standard deviation around 135 for the humidity profiles, under all-weather  
239 conditions and below 2 km a.g.l..

240 Additionally, from the MWR potential temperature ( $\theta$ ) profiles, a feature to describe the atmospheric stability  
241 ( $A_tS_t$ ) has been defined. Using the comparison criterion presented in Moreira et al. (2020), where each  $\theta$  profile  
242 is classified as convective, the  $A_tS_t$  categorical feature has been obtained being  $A_tS_t = 0$  for convective situations  
243 and  $A_tS_t = 1$  for stable cases.

244 The initial Dataset is presented in Table 1. Hourly averages of all the relevant variables for the period 2015-2017  
245 have been obtained from their original database, except for the values of H and S which were included as  
246 categorical variables. Additionally, continuous variables have been normalized with respect to their mean values,  
247 in order to homogenize their ranges of variability. Although this is not a required process in GBRT, Krishnamurthy  
248 et al. (2021) have pointed out slight improvements in ABLH detection, mainly at nighttime, when this  
249 normalization is applied. This final dataset was splitted in two subsets: (1) a subset with measurements recorded  
250 in the period 2015-2016 that will be used for the model set-up and training, and (2) a validation subset, composed  
251 by measurements taken along 2017.

### 252 3.2.2 Feature selection

253 In order to verify the relevance of each feature and to avoid data redundancy, as well as excessive complexity in  
254 the model, a selection of the most relevant features from the initial dataset has been performed (Guyon and  
255 Elisseeff, 2003). To this aim, the importance of each feature has been analyzed from two criteria. A first criterion,  
256 namely the Boruta algorithm, estimates the importance of each feature by comparing its influence on the predicted  
257 value with that of its randomly shuffled copies (Kursa et al, 2010). The second criterion, known as Recursive  
258 Feature Elimination (RFE), trains a predetermined model starting with all features in the training dataset, and after  
259 each iteration discards the least important features and refits the model (Yu and Liu, 2003). In this study, the  
260 variables that after being discarded did not cause a 2% reduction in coefficient of determination ( $R^2$ ) were removed.

261 Both criteria have been applied on the entire database but also a specific feature importance analysis has been  
262 performed in order to account for possible differences in the feature relevance between day- and night-time  
263 situations. Figure 2 shows the relative importance of each feature, during day (a) and night (b), so that as higher  
264 the value obtained, greater is the influence of this variable on the results provided by the ML model. For daytime

265 ABLH<sub>CEIL</sub> and G appear as the most relevant features while T, RH, NR, WS, P and WS show a lower relevance  
266 and are sorted differently by each criteria. In the case of nighttime data, the most relevant feature is the hour (H),  
267 which explains how the model can identify nighttime situations, while the ABLH<sub>CEIL</sub> takes the second position  
268 and remains as one of the most important features for the model. On the opposite extreme A<sub>t</sub>S<sub>t</sub>, S, SZA, kt have  
269 been classified as irrelevant features. This result can be explained by the correlation of these variables with some  
270 of the features classified as relevant. Thus, i.e., all the near-surface meteorological features selected as relevant  
271 present some seasonal dependence making the use of the parameter S redundant. Similarly, A<sub>t</sub>S<sub>t</sub>, appears in both  
272 cases, nighttime and daytime, as one of the less relevant features. In the case of our location, this is explained  
273 because nighttime/daytime classification is mostly equivalent to a stable/convective classification, making the  
274 variable A<sub>t</sub>S<sub>t</sub> a redundant input. Thus, in a deep analysis of the entire database no stable cases during the daytime  
275 while the 95.5% of nighttime cases are convective. These irrelevant (A<sub>t</sub>S<sub>t</sub>, S, SZA, kt) features have not been  
276 included as input in the final GBRT model in order to avoid redundancy in the dataset.

### 277 3.2.3 Hyperparameters

278 GBRT algorithm requires a thorough setup of the so-called hyperparameters (parameters that cannot be updated  
279 during the training process) in order to avoid overfitting in the training dataset. The most relevant hyperparameters  
280 involved in the GBRT proposed in this study are: (1) the maximum depth of each tree, which represents the  
281 maximum number of leaves in each tree, (2) the maximum number of features, which indicate the maximum  
282 number of features inputted in each tree, (3) the learning rate, which indicates the influence of the previous  
283 decision-trees on its successors, and (4) the minimum sample leaf, which represents the minimum number of  
284 samples required to be at a leaf node in the tree.

285 In this study, the hyperparameters of the baseline model have been obtained from a large group of values randomly  
286 selected over our setup-training subset, over which a cross validation and Bayesian optimization processes  
287 (Frazier, 2018) have been applied using the Python library Scikit-learn (Pedregosa et al., 2011). Then, an empirical  
288 fine-tuning was performed in order to detect the values that provide the best results. From this analysis, the most  
289 suitable value for the maximum depth of each tree has been estimated as 5 while for the maximum number of  
290 features a value of 4 has been selected. These low values of the hyperparameters contribute to reducing the  
291 potential overfitting. A low value has been also obtained for the learning rate (0.0573), which ensures the  
292 improvement of the correction under ceilometer data during stable periods. The optimal minimum sample leaf  
293 value was indicated as 3, avoiding higher values of this parameter that can generate greater smoothing in the  
294 predicted values.

### 295 3.3 Model training

296 Once the inputs and hyperparameters have been determined, the GBRT algorithm has been trained (stage where  
297 the model is fitted) and tested (stage where the model performance is analyzed in terms of accuracy/precision).  
298 As indicated in Section 2, this training has been performed using a two-year dataset (2015-2016) with 5.153 cases.  
299 In order to reduce possible bias, the k-fold cross-validation methodology (James et al. 2013) has been applied. In  
300 this methodology, the dataset is randomly shuffled and divided into k parts, approximately equal. Then, k  
301 iterations are performed and, in each one of them, one group is selected as a test while the others k-1 are used for  
302 training. After k iterations, the chosen performance parameters obtained from each iteration and mean absolute  
303 error are averaged, and such values are considered as the performance parameters of the model. In this work k is



304 5 and, consequently, in each iteration an 80% and 20% of the data subset were employed for training and testing,  
305 respectively. Figure 3 illustrates this process.

306 In the training stage, the model reached a  $R^2$  of 0.97, which indicates a satisfactory performance and that the  
307 overfitting was avoided. The Mean Absolute Error (MAE) obtained was 127 m. During the test stage, although a  
308 reduction of around 20% in  $R^2$  (0.76) was observed, the variation of MAE was lower than -2%, resulting in 129  
309 m.

### 310 3.4 Analysis

311 The GBRT algorithm proposed in this study has been validated using data recorded in our station along the entire  
312 2017. Thanks to that, different aspects have been analyzed. On one hand, the general performance of the algorithm  
313 has been assessed analyzing the temporal and seasonal variability of the Mean Relative Error (MRE) among the  
314  $ABLH_{GBRT}$  and  $ABLH_{MRW}$  values. This statistic quantifies the mean relative deviation between the target value  
315 ( $ABLH_{MRW}$ ) and that one provided by the model ( $ABLH_{GBRT}$ ). The MRE has been estimated by the following  
316 equation:

$$317 \quad MRE_{GBRT}(\%) = 100 \cdot \sum \left( \frac{ABLH_{GBRT} - ABLH_{MRW}}{ABLH_{MRW}} \right) (2)$$

318 This statistic has been also calculated for the  $ABLH_{CEIL}$  values in order to assess the improvement of the algorithm  
319 proposed in this study with respect to the use of the ceilometer alone.

320 The statistical analysis has been completed with the estimations of the relative Root Mean Squared Error (rRMSE)  
321 defined as:

$$322 \quad rRMSE_{GBRT}(\%) = 100 \cdot \sqrt{\frac{1}{N} \sum \left( \frac{ABLH_{GBRT} - ABLH_{MRW}}{ABLH_{MRW}} \right)^2} (3)$$

323 where n is the number of samples.

324 In order to identify possible limitations of the proposed algorithm under different atmospheric conditions,  
325 cloudless, stable and convective situations have been differentiated and the MRE values for these situations have  
326 been analyzed. Day- and nighttime have been separated in terms of the solar zenith angle values (SZA), with SZA  
327  $< 80^\circ$  for daytime and SZA  $> 100^\circ$  for nighttime. As mentioned above, because of the results of the  
328 convective/stable analysis performed from the  $A_tS_t$  feature, in this study nighttime is equivalent to stable and  
329 daytime is equivalent to convective situations. Additionally, cloudy and cloudless conditions have differentiated.  
330 In this study, clouds have been detected from the intensity of the RCS measured by the ceilometer, which notably  
331 increases in presence of clouds over the instrument. Clouds are detected when the RCS reaches values above 107,  
332 which is the empirical threshold estimated for our station as representative of cloud presence (Moreira et al.,  
333 2020a). Day- and nighttime have been separated in terms of the solar zenith angle values (SZA), with SZA  $< 80^\circ$   
334 for daytime and SZA  $> 100^\circ$  for nighttime. As mentioned above, because of the results of the convective/stable  
335 analysis performed from the  $A_tS_t$  feature, in this study nighttime is equivalent to stable and daytime is equivalent  
336 to convective situations.

337 Moreover, to the MRE values, the analysis of these situations has been performed analyzing  $R^2$  with respect to  
338 the reference measurements and defined as:

$$339 \quad R^2 = 1 - \frac{\sum_{i=1}^n (x_i - \hat{x}_i)^2}{\sum_{i=1}^n (x_i - \bar{x})^2} \quad (4)$$

340 where  $n$  number of samples,  $x_i$  is the reference values ( $ABLH_{MWR}$ ),  $\hat{x}_i$  is the estimated value ( $ABLH_{GBRT}$ ) and,  $\bar{x}$   
341 is the average of the reference values ( $ABLH_{MWR}$ ).

342 Finally, the  $ABLH_{CEIL}$ ,  $ABLH_{GBRT}$  and  $ABLH_{MWR}$  were intercompared for three days endowed with specific  
343 atmospheric situations: a) cloudless day, b) low-cloud day, and c) a day under the influence of a Saharan dust  
344 outbreak. These situations have been chosen due to the limitations observed in the ceilometer estimations of the  
345  $ABLH$ , mainly under low-cloud scenarios (Coen et al., 2014) and decoupled aerosol layers (Caicedo et al., 2017),  
346 and will contribute to analyze the improvement of the methodology proposed in this study.

## 347 **4 Results**

### 348 **4.1 General performance**

#### 349 **4.1.1 Temporary and seasonal variability**

350 Figure 4 presents the MRE hourly-averaged  $ABLH_{CEIL}$  and  $ABLH_{GBRT}$  values for all analyzed cases. Both  
351  $ABLH_{GBRT}$  and  $ABLH_{CEIL}$  overestimate the  $ABLH_{MWR}$  values although with notably lower percentages in the case  
352 of the GBRT estimations (note the different scales in Figure 4). Thus, the  $MRE_{GBRT}$  values (black line) do not  
353 exceed 36% while  $MRE_{CEIL}$  (magenta line) always has values higher than 30%. In both cases, the MRE values  
354 present a diurnal pattern with their lowest values during the first hours in the afternoon (0% for  $MRE_{GBRT}$  vs. 30%  
355 for  $MRE_{CEIL}$ ) and their highest values during nighttime (around a 30% for  $MRE_{GBRT}$  and up to a 200% for  
356  $MRE_{CEIL}$ ). The higher differences between  $ABLH_{CEIL}$  and  $ABLH_{MWR}$ , observed during the night and early  
357 morning, occur because the  $ABLH_{MWR}$  estimates the SBLH, while the  $ABLH_{CEIL}$  detects the RLH (Moreira et al.,  
358 2020). From these results, it is possible to observe the possibility of estimating the SBLH from ceilometer data in  
359 combination to surface meteorological information. In addition, from the combination of gradient method and  
360 GBRT is possible to detect SBLH, RLH and CBLH.

361 Figure 5 presents a comparison among the hourly averaged  $ABLH_{GBRT}$  (black line),  $ABLH_{MWR}$  (red line), and  
362  $ABLH_{CEIL}$  (magenta line) values. These plots show the expected pattern with lower  $ABLH$  values from sunrise to  
363 sunset and higher values during daytime, following a delayed solar cycle pattern (Moreira et al., 2020a). For all  
364 seasons, the  $ABLH_{GBRT}$  and  $ABLH_{MWR}$  values present high similarity, especially between 09 to 18 UTC, being  
365 all  $ABLH_{MWR}$  values within the  $ABLH_{GBRT}$  error range (grey shadow). The  $R^2$  values between  $ABLH_{GBRT}$  and  
366  $ABLH_{MWR}$  in each season are always greater than or equal 0.88, in contrast to the seasonal  $R^2$  values between  
367  $ABLH_{CEIL}$  and  $ABLH_{MWR}$ , which are always lower than 0.30. Such values occur because during nighttime and  
368 early morning notable differences are observed between  $ABLH_{CEIL}$  and  $ABLH_{MWR}$  values because the methods  
369 based on the gradient of aerosol concentration tend to monitor the RLH in these situations. However, in the central  
370 hours of the day  $ABLH_{CEIL}$  and  $ABLH_{MWR}$  estimates the CBLH. On the other hand, the GBRT method is well  
371 trained to detect the SBLH, in a similar way as the  $ABLH_{MWR}$  detects it. As the central hours of the day approach,  
372 the difference is gradually reduced, being minimal at the point where the maximum height of the  $ABLH$  is reached.

373 Table 2 summarizes the rRMSE values of the GBRT for all cases, as well as for each season, for both day- and  
374 night-time (convective/stable) situations. These results confirm the good performance of the model proposed here  
375 with an average rRMSE of 20% for all cases. Summer is the season with the lowest values of rRMSE for both  
376 day- and night-time. The rest of the seasons show similar behavior with rRMSE ranging from a 14% for daytime  
377 in Spring and 26% for nighttime in Autumn.

378 The daily patterns of the hourly averaged  $MRE_{GBRT}$  and  $MRE_{CEIL}$  values, per season, are shown in Fig. 6. The  
379 scales evidence that in all cases  $MRE_{CEIL}$  are larger than  $MRE_{GBRT}$ , mainly during night and early morning, as  
380 expected, due to differences in ABLH definition considered by each algorithm. In the case of  $MRE_{GBRT}$  similar  
381 patterns for the different seasons have been found although with larger errors (in the range 15% to 45%) between  
382 19 - 08 UTC while lower errors ( $< 15\%$ ) occur between 09 to 18 UTC. The highest  $MRE_{GBRT}$  values are observed  
383 in autumn (Fig. 6d), while the lowest values are estimated in summer (Fig. 6c). On the other hand, the  $MRE_{CEIL}$   
384 values show a seasonal pattern, with values higher than 140% between 19 - to 08 UTC, for all seasons, excluding  
385 summer (Fig. 5c). A result that is associated with the detection of the RL top height by the ceilometer processing  
386 (Moreira et al., 2020a). Between 09 to 18 UTC (period predominantly convective), the  $MRE_{CEIL}$  has low values,  
387 underestimating the  $ABLH_{MWR}$  in some situations (13 to 14 UTC in summer and 14 UTC in autumn). The highest  
388  $MRE_{CEIL}$  values are observed in winter (Fig. 6a), while the lowest ones occur in summer (Fig. 6c).

#### 389 4.1.2 Dependence on atmospheric/meteorological conditions

390 Table 3 summarizes the  $R^2$  and  $MRE_{GBRT}$  values for cloudless, stable and convective situations. In general,  
391 cloudless cases present only a variation of around a 1% for the  $R^2$  and  $MRE_{GBRT}$  values with respect to the all-sky  
392 situations, indicating a low dependence of the GBRT algorithm on cloudiness. Such a result is in accordance with  
393 low relative importance of kt presented in section 3.2.2. When stable and convective cases are not differentiated,  
394 the GBRT model shows its highest values of  $R^2=0.91$ ) and  $MRE_{GBRT}$  values are around 20%. When convective  
395 and stable cases are differentiated, the highest  $R^2$  values (0.89) and the lowest values of  $MRE_{GBRT}$  (11%) were  
396 observed during the convective periods. In daytime situations, and mainly under cloudless conditions, the top of  
397 the aerosol layer coincides with the CBL height due to the absence of the RL (e.g. Eresma et al., 2006; Caicedo  
398 et al., 2017; Moreira et al., 2020a). Stable cases show a slightly lower performance, with  $R^2 = 0.75$  and  $MRE_{GBRT}$   
399 values around 28%, where the lower SBLH values are partially responsible of the rather large  $MRE_{GBRT}$ .

## 400 4.2 Case studies

### 401 4.2.1 Case 1: A clear-sky day (24<sup>th</sup> January 2017)

402 Figure 8 shows the evolution of the ABLH for a clear-sky day, characterized by the absence of low clouds and a  
403 thick and well-defined aerosol layer. It is observed that  $ABLH_{CEIL}$  (magenta stars) represents the RL, from the  
404 beginning of measurement, until around 09:00 UTC. Thus, as CBL begins to increase, the difference between  
405  $ABLH_{CEIL}$  and  $ABLH_{MWR}$  decreases, so that they are coincident at 10:00 UTC, and have a difference lower than  
406 350 m between 11:00 and 18:00 UTC. At 19:00 UTC the  $ABLH_{MWR}$  presents values clearly decoupled of the top  
407 of the aerosol layer ( $ABLH_{CEIL}$ ) detecting the SBLH, consequently the differences between  $ABLH_{CEIL}$  and  
408  $ABLH_{MWR}$  increase, reaching the maximum at 23:00 UTC (around 1200 m).

409 For its part, the  $ABLH_{GBRT}$  values (black stars) show a very similar behavior with respect to the  $ABLH_{MWR}$  values  
410 (red stars). Their higher agreement occurs between 04:00 to 06:00 UTC and 18:00 to 22:00 UTC, showing that

411 the GBRT model provides appropriate estimates of the SBLH in the presence of the RL. The highest differences  
412 between  $ABLH_{MWR}$  and  $ABLH_{GBRT}$  are observed between 10:00 and 17:00 UTC, nevertheless, they are always  
413 lower than 100 m.

#### 414 **4.3.2 Case 2: A day with presence of low clouds (7<sup>th</sup> February 2017)**

415 Figure 9 shows a case with the presence of low clouds (altitude < 2000 m), which can directly influence the ABLH  
416 detection when using the gradient method with the ceilometer data (Moreira et al., 2020). From 01:00 to 06:00  
417 UTC due to low RL height,  $ABLH_{MWR}$  and  $ABLH_{CEIL}$  present, in general, a similar behavior with differences  
418 lower than 300 m. At 07:00 UTC, when the first clouds appear, the gradient method tends to overestimate the  
419  $ABLH_{MWR}$  (which is situated at 410 m), increasing the  $ABLH_{CEIL}$  values up to 1500 m (cloud base). Due to the  
420 presence of low clouds throughout the day, the  $ABLH_{CEIL}$  is estimated at the cloud base overestimating the  
421  $ABLH_{MWR}$ , mainly during the stable period, where the difference between them reaches up to 2000 m at 23:00  
422 UTC. Similar results were observed by Coen et al. (2014) and Caicedo et al. (2017).

423 In the case of the  $ABLH_{GBRT}$  values, from 01:00 to 07:00 UTC  $ABLH_{GBRT}$  and  $ABLH_{MWR}$  are almost coincident  
424 (differences lower than 20 m). However, between 08:00 and 16:00 UTC the  $ABLH_{GBRT}$  overestimates the  
425  $ABLH_{MWR}$ , so that the maximum difference (300 m) is observed at 12:00 UTC. Due to the presence of clouds,  
426 radiative cooling occurs in the region near the base of the cloud, affecting the temperature profile and,  
427 consequently, decreasing the  $ABLH_{MWR}$ . On the other hand, the ML model is a combination of a group of  
428 variables, which are not totally affected by the clouds, therefore higher ABLH values are estimated. From 18:00  
429 to 22:00 UTC the  $ABLH_{GBRT}$  underestimates the  $ABLH_{MWR}$ , with maximum difference (-100 m) being observed  
430 at 20:00 UTC. Despite  $ABLH_{GBRT}$  values present differences between -100 and 300 m during the cloudy period  
431 compared to the MWR estimations, such results demonstrate a remarkable improvement in these situations in  
432 comparison  $ABLH_{CEIL}$ , which is strongly affected by low clouds.

#### 433 **4.3.3 Case 3: Sahara dust outbreak (21<sup>st</sup> February 2017)**

434 Estimating ABLH during dust outbreaks is a challenge to methods based on stand-alone vertical aerosol profiles,  
435 mainly when the dust layer is advected in the ABL region (e.g. Granados-Muñoz et al., 2012; Bravo-Aranda et  
436 al., 2017). In these situations, methods to estimate the ABLH based on stand-alone vertical aerosol profiles are  
437 unable to distinguish aerosol layering and the ABLH values tend to be overestimated (Granados-Muñoz et al.,  
438 2012), requiring the use of more sophisticated methods such as POLARIS based on depolarization measurements  
439 (Bravo-Aranda et al., 2017). However, due to the technical limitation of ceilometers (described previously in  
440 section 1), applications of techniques that require the use of more than one wavelength cannot be applied.  
441 Resulting in a lack of studies that address the detection of ABLH from ceilometer data during dust outbreaks.

442 Figure 10 presents the second day of an extreme Sahara dust outbreak registered over the Iberian Peninsula from  
443 20 to 23 February 2017, resulting in values of aerosol optical depth around 2.3 (at 675 nm) in Granada (Fernández  
444 et al., 2019). These values correspond to level 2.0 data provided by AERONET.

445 In this situation, notable problems can be observed in the  $ABLH_{CEIL}$  values. Thus, from 01:00 to 12:00 UTC,  
446  $ABLH_{CEIL}$  is estimated on the top of the dust layer due to the high gradient between this layer and FT.  
447 Consequently, the  $ABLH_{CEIL}$  is overestimated, mainly between 01:00 and 07:00 UTC. Between 13:00 and 14:00  
448 UTC, due to a reduction in the height of the aerosol layer,  $ABLH_{CEIL}$  is situated close to the  $ABLH_{MWR}$ ,

449 underestimating it by around 200 m. From 15:00 UTC until the end of day, the height of the aerosol layer increases  
450 again, so that  $ABLH_{CEIL}$  returns to overestimate the  $ABLH_{MWR}$ , resulting in a maximum difference of 2400 m at  
451 23:00 UTC.

452 Despite the complexity of the situation,  $ABLH_{GBRT}$  values present a very high agreement with respect to the  
453  $ABLH_{MWR}$ . A slight overestimation occurs from 02:00 to 14:00 UTC (less than 100 m) and after 19:00 UTC (with  
454 maximum at 22:00 UTC of 200 m). On the other hand,  $ABLH_{GBRT}$  underestimate the  $ABLH_{MWR}$  from 15:00 and  
455 18:00 UTC, so that the maximum difference (-100 m) is observed at 16:00 UTC.

456 These results confirm the possibility of estimating reliable ABLH during cases of dust outbreaks using a  
457 ceilometer combined with near-surface meteorological data as input of the machine learning algorithm proposed  
458 in this study.

## 459 5 Conclusions

460 A new methodology to estimate the Atmospheric Boundary Layer Height (ABLH), detecting the Stable Boundary  
461 Layer Height (SBLH) in stable cases, based on the machine learning algorithm known as Gradient Boosting  
462 Regression Tree (GBRT) has been proposed. This algorithm uses as features (independent variables) estimations  
463 of the ABLH derived applying the gradient method to a ceilometer signal ( $ABLH_{CEIL}$ ) and several surface  
464 meteorological variables. The target (reference) ABLH values in this study have been those estimated from a  
465 microwave radiometer ( $ABLH_{MWR}$ ). A detailed study of the features and the hyperparameters involved in the  
466 model set-up have been developed in order to avoid the model overfitting and guarantee its good performance  
467 during the training ( $R^2 = 0.97$ ;  $MAE = 127$  m) and test ( $R^2 = 0.76$ ;  $MAE = 129$  m) stage.

468 The proposed new algorithm has been validated using the entire year 2017. The model performance analysis has  
469 shown a daily pattern in the  $MRE_{GBRT}$  values, with their highest values during the night-time (stable situations)  
470 and their lower values along the day-time (convective situations). Minimum differences between  $ABLH_{GBRT}$  and  
471  $ABLH_{MRW}$  appears, during the central hours of the day and first hours in the afternoon, when the ABL presents is  
472 higher height. This pattern has been observed for all seasons with  $MRE_{GBRT}$  ranging between -5% and 35%. A  
473 remarkable improvement is observed with respect to the  $MRE_{CEIL}$  values, which show similar daily patterns but  
474 range between 36% and 190%.

475 The new model has been analyzed under different atmospheric conditions revealing no dependence of the  
476 algorithm on cloudiness conditions. Small differences have been observed between stable and convective  
477 situations. Thus, while  $MRE_{GBRT}$  is around 11% in convective situations, these values increase up to 28% in the  
478 case of stable situations. Nevertheless, for both cases  $R^2$  values are above 0.75 for stable and convective  
479 atmospheres and take a value of 0.91 when all conditions are considered. These results confirm the robustness of  
480 the GBRT algorithm presented in this study.

481 Three particular cases, namely a clear-sky day, a day with presence of low-clouds and dust outbreak event, have  
482 been chosen due to analyze and overcome the limitations observed in the  $ABLH_{CEIL}$ , particularly in the dust-  
483 outbreak events for which the gradient method is highly inefficient. In general, in these three particular situations  
484  $ABLH_{GBRT}$  shows very similar values and behavior than the  $ABLH_{MRW}$ , confirming the good model performance  
485 and a remarkable improvement with respect to the  $ABLH_{CEIL}$  in complex situations, and enabling the SBLH  
486 detection. Therefore, the combination of GBRT and gradient method enables the detection of SBLH, CBLH and

487 RLH from ceilometer data together with surface meteorological information. Such results can be easily applied to  
488 well-established ceilometers networks over the world, just adding low cost surface meteorological sensors, which  
489 typically are available in these stations.

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735 **Table 1.** Group of input variables initially considered along with the instrument used to measured them and the  
 736 range of variation of each variable during the period of study.

| Instrument/Algorithm           | Variable                                   | Range                        |
|--------------------------------|--|------------------------------|
| Ceilometer/Gradient Method     | ABLH <sub>CEIL</sub>                       | 200 m - 4500 m               |
| MWR/Gradient and Parcel Method | ABLH <sub>MWR</sub>                        | 200 m - 4500 m               |
| HMP60                          | Temperature (T)                            | 0 - 42 °C                    |
|                                | Hour (H)                                   | Categorical Variable         |
|                                | Season (S)                                 | Categorical Variable         |
|                                | Stability (A <sub>i</sub> S <sub>i</sub> ) | Categorical Variable (0-1)   |
| HMP60                          | Relative Humidity (RH)                     | 4.7 - 91 %                   |
| Barometer PTB110               | Pressure (P)                               | 920 - 952 hPa                |
| Anemometer 05103               | Wind Speed (WS)                            | 0 - 5 m/s                    |
| Pyranometer CM-11              | Global Radiation (G)                       | 0 - 1016 W/m <sup>2</sup>    |
| Pygeometer PIR                 | Net Radiation (NR)                         | -167 - (-1) W/m <sup>2</sup> |
| Blanco-Muriel et al. (2001)    | Solar Zenith Angle (SZA)                   | 14 - 165 °                   |
| Iqbal (1983)                   | Clearness Index (k <sub>t</sub> )          | 0 - 1                        |

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739 **Table2.** rRMSE of the GBRT for all cases, as well as for each season, for both day- and nigh-time  
 740 (convective/stable) situations.

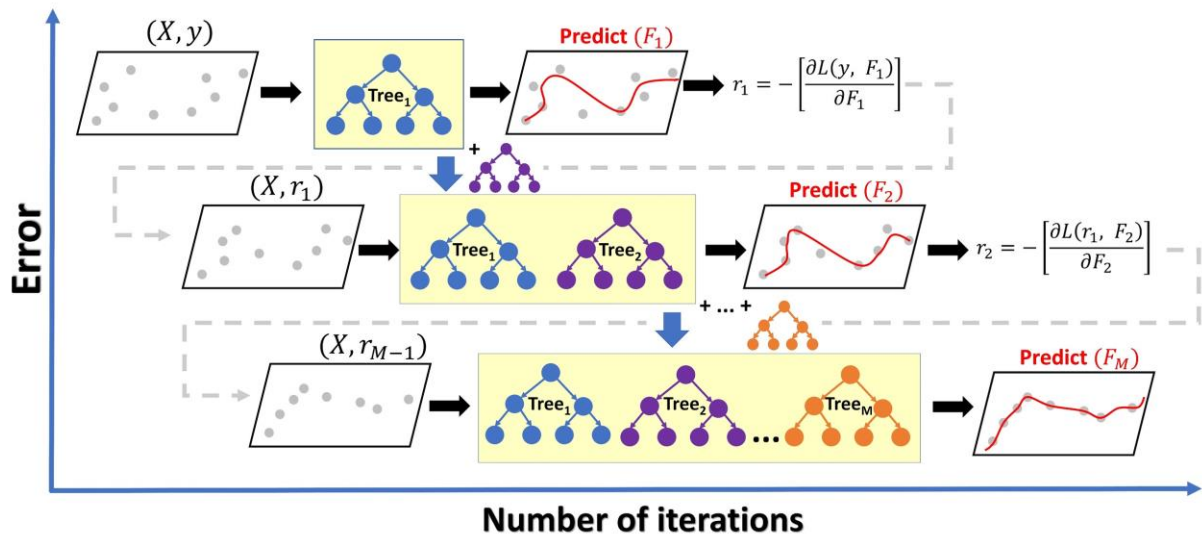
|                           | All cases |       | Winter |       | Spring |       | Summer |       | Autumn |       |
|---------------------------|-----------|-------|--------|-------|--------|-------|--------|-------|--------|-------|
|                           | Day       | Night | Day    | Night | Day    | Night | Day    | Night | Day    | Night |
| rRMSE <sub>GBRT</sub> (%) | 15        | 25    | 18     | 24    | 14     | 25    | 10     | 20    | 15     | 26    |

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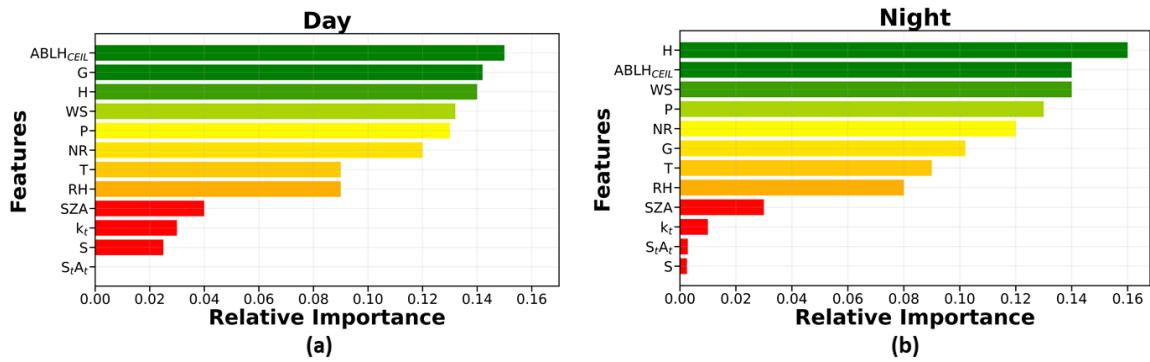
**Table 3.** MRE and R<sup>2</sup> of the GBRT algorithm under cloudless and all-cloud-type conditions. Additionally, for each category, stable, convective and all-stability conditions have been differentiated. Number of cases on each category have been included in order to prove their representativeness.

|                         | All Cases |            |           | Cloudless Cases |            |           |
|-------------------------|-----------|------------|-----------|-----------------|------------|-----------|
|                         | Stable    | Convective | All cases | Stable          | Convective | All cases |
| Number of cases         | 1284      | 1579       | 2863      | 398             | 600        | 998       |
| R <sup>2</sup>          | 0.75      | 0.89       | 0.90      | 0.75            | 0.89       | 0.91      |
| MRE <sub>GBRT</sub> (%) | 28.0      | 11.1       | 20.9      | 27.5            | 10.2       | 19.1      |

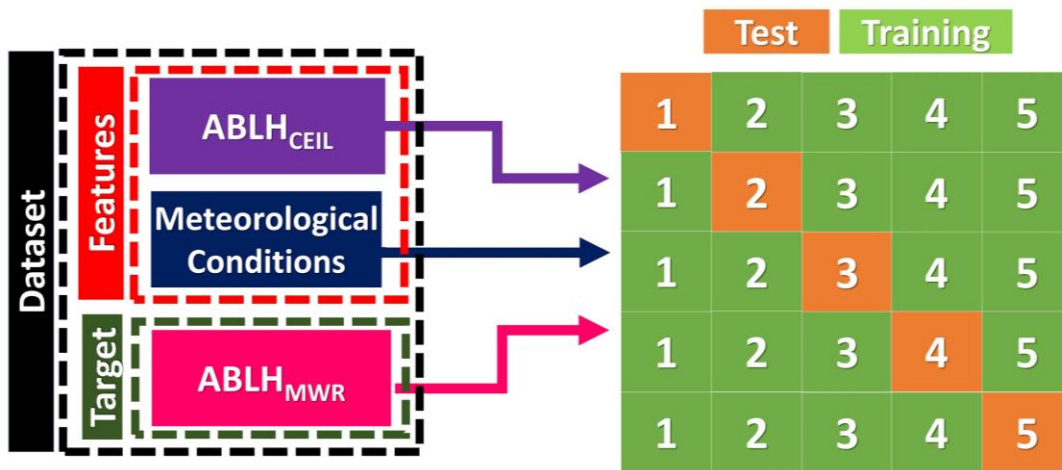
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 748 Figure 1 - GBRT flowchart.  $X$ ,  $y$ , and  $L$  represent the feature matrix, target variable, and loss-function,  
 749 respectively.  $r_N$  and  $F_N$  indicate the  $n$ -th pseudo-residual error and prediction.  
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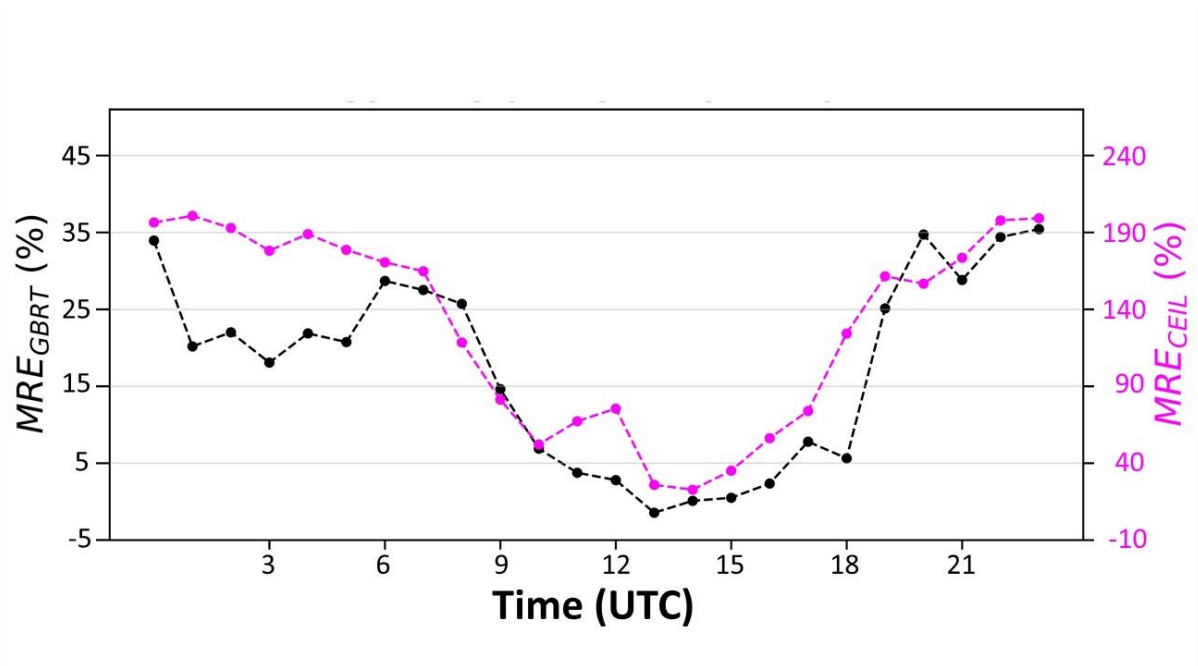


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 752 Figure 2 - Feature relative importance classification/ranking applying the Recursive Feature Elimination (RFE)  
 753 method, for day (a) and night (b) situations.  
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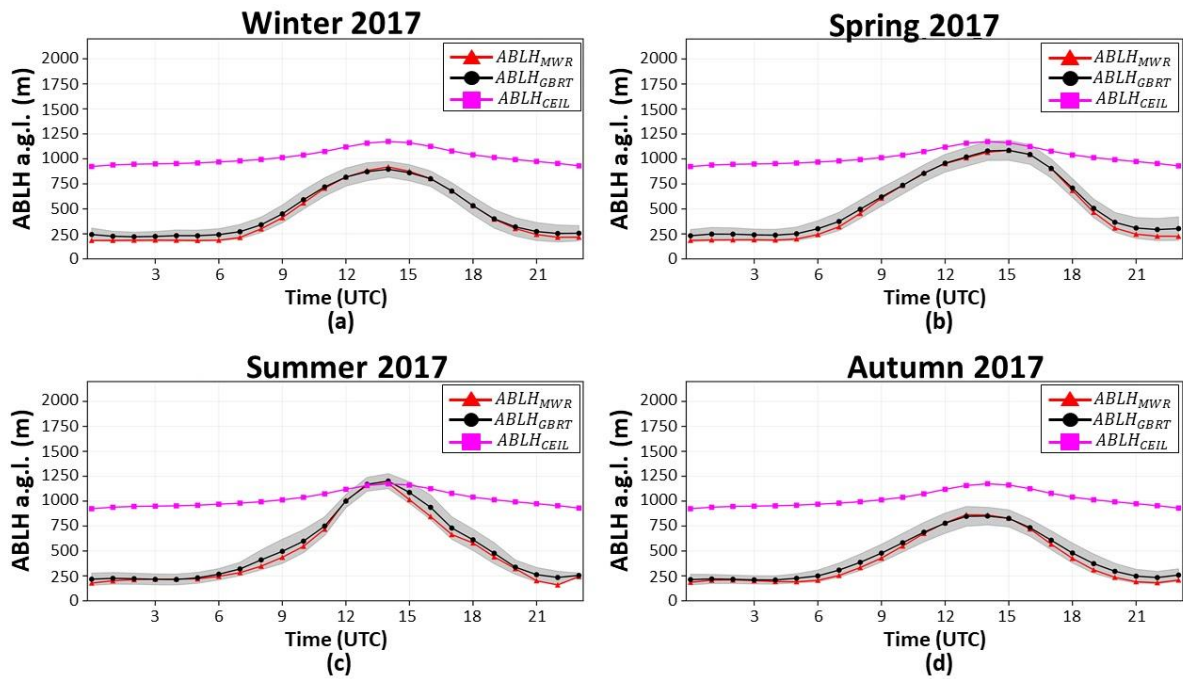
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Figure 3 - Scheme of input dataset (left) and k-fold cross-validation methodology (right).



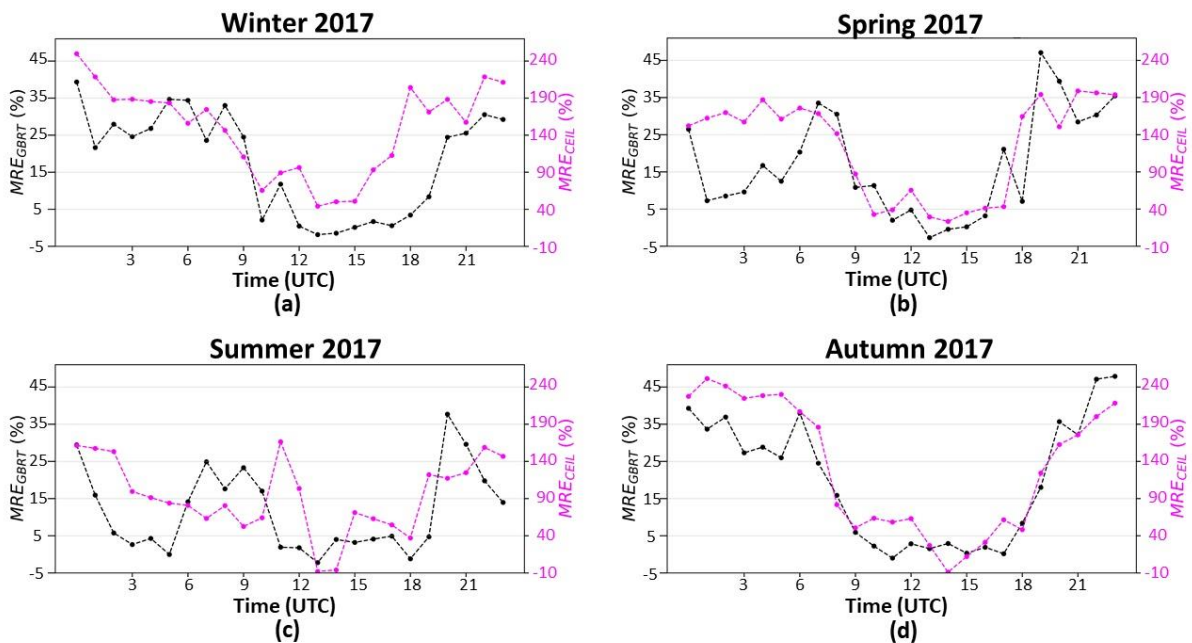
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Figure 4 – Hourly Mean Relative Error for all the analyzed cases applied in the GBRT algorithm (black) and the gradient method to the ceilometer data (pink). It should be highlighted the important difference between the scales required for each methodology.



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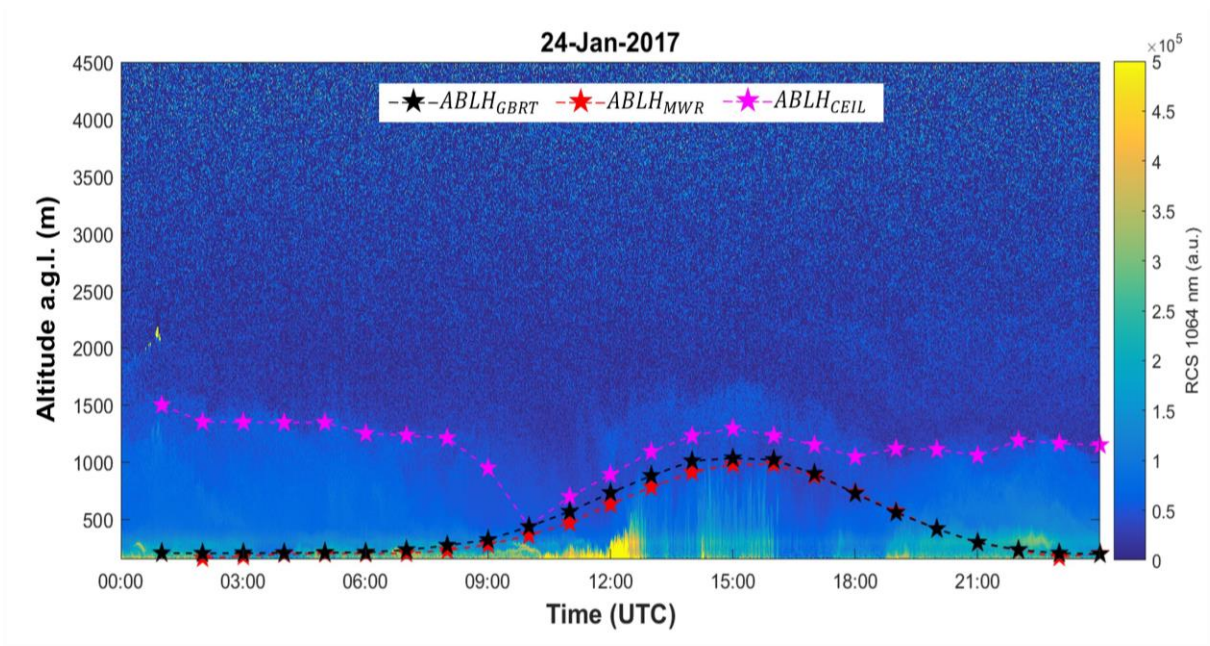
768 Figure 5 - Comparison between the hourly ABLH average measured (red line) and those predicted by the GBRT  
 769 algorithm (black line) and the ceilometer (pink) for (a) winter, (b) spring, (c) summer, and (d) autumn. The dark  
 770 shadow represents the GBRT model standard deviation.  
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773 Figure 6 - Hourly Mean Relative Error for all the analyzed cases applied in the GBRT algorithm (black) and the  
 774 gradient method to the ceilometer data (pink) during (a) winter, (b) spring, (c) summer, (d) autumn.  
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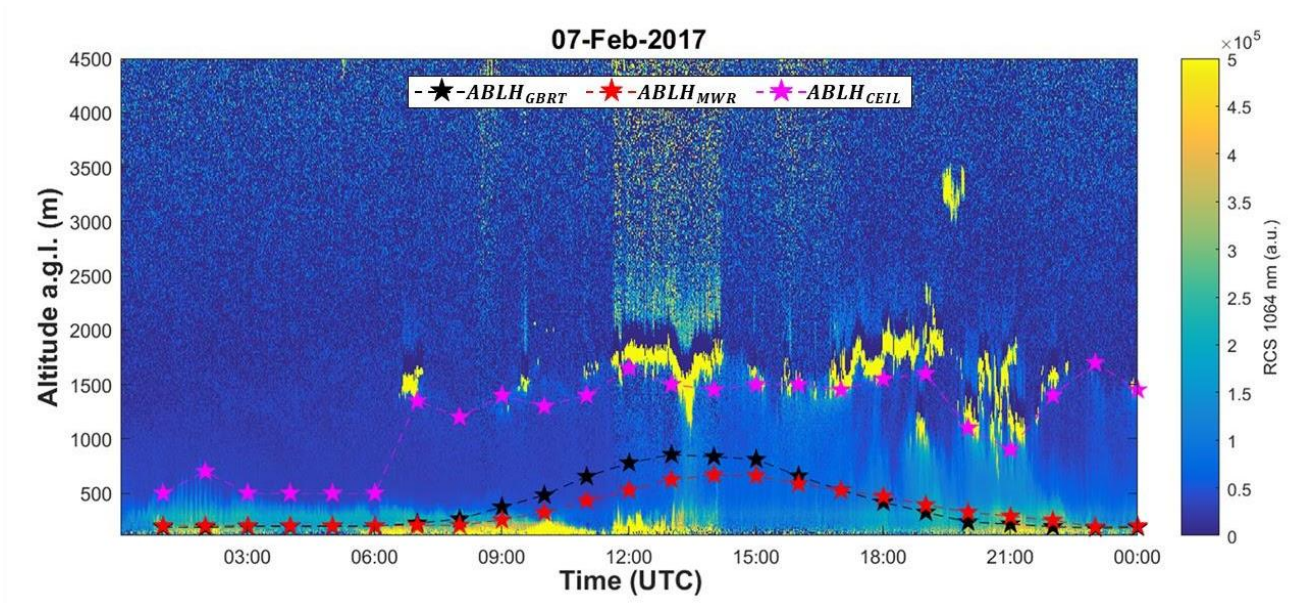


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779 Figure 8 - Comparison among the hourly values of  $ABLH_{GBRT}$  (black stars),  $ABLH_{MWR}$  (red stars) and of  
 780  $ABLH_{CEIL}$  (pink stars) at January 24, 2017.

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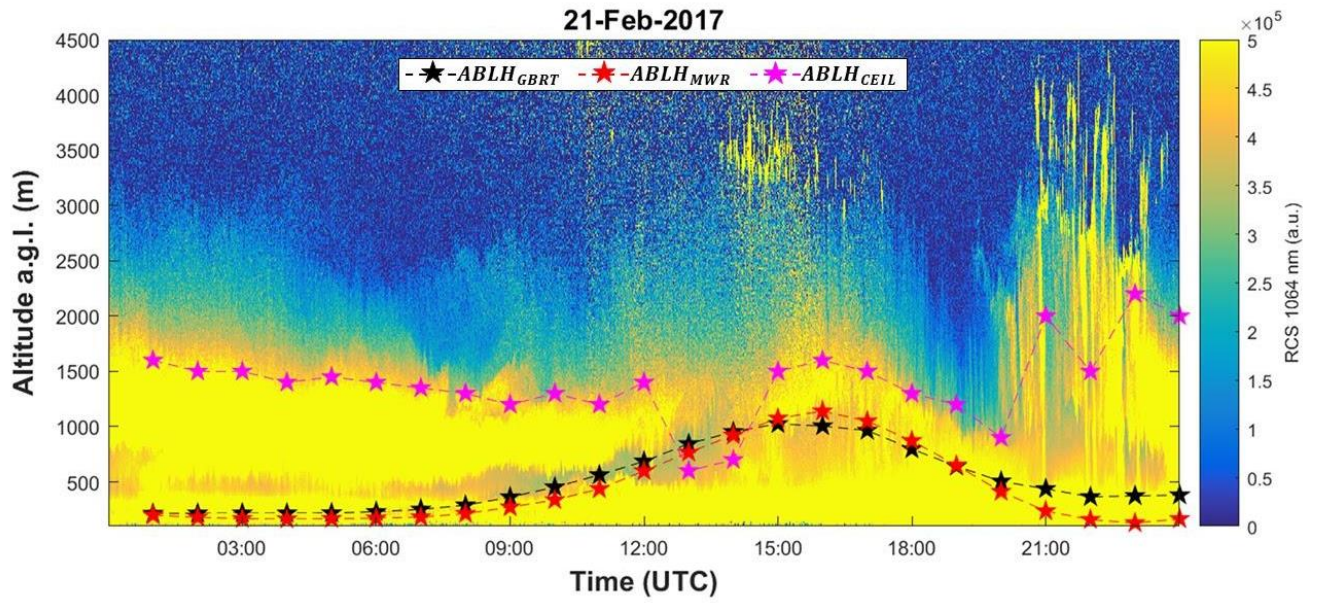
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784 Figure 9 - Comparison among the hourly values of  $ABLH_{GBRT}$  (black stars),  $ABLH_{MWR}$  (red stars) and  $ABLH_{CEIL}$   
 785 (pink stars) at February 7, 2017.

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788 Figure 10 - Comparison among the hourly values of ABLH<sub>GBRT</sub> (black stars), ABLH<sub>MWR</sub> (red stars) and ABLH<sub>CEIL</sub>  
 789 (pink stars) at February 21, 2017.

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