

Depth of maximum of air-shower profiles at the Pierre Auger Observatory. I. Measurements at energies above $10^{17.8}$ eV

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We report a study of the distributions of the depth of maximum, X_{\max} , of extensive air-shower profiles with energies above $10^{17.8}$ eV as observed with the fluorescence telescopes of the Pierre Auger Observatory. The analysis method for selecting a data sample with minimal sampling bias is described in detail as well as the experimental cross-checks and systematic uncertainties. Furthermore, we discuss the detector acceptance and the resolution of the X_{\max} measurement and provide parametrizations thereof as a function of energy. The energy dependence of the mean and standard deviation of the X_{\max} distributions are compared to air-shower simulations for different nuclear primaries and interpreted in terms of the mean and variance of the logarithmic mass distribution at the top of the atmosphere.

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I. INTRODUCTION

The mass composition of ultrahigh energy cosmic rays is one of the key observables in studies of the origin of these rare particles. At low and intermediate energies between 10^{17} and 10^{19} eV, precise data on the composition are needed to investigate a potential transition from galactic to extragalactic sources of the cosmic-ray flux (see, e.g., [1–4]). Furthermore, the evolution of the composition towards 10^{20} eV will help to understand the nature of the steepening of the flux of cosmic rays observed at around 4×10^{19} eV [5–7]. This flux suppression might either be caused by energy losses of extragalactic particles due to interactions with photons (cosmic microwave background in case of protons or extragalactic background light in case of heavy nuclei) [8,9], or it might signify the maximum of attainable energy in astrophysical accelerators, resulting in a rigidity-dependent change of the composition (see, e.g., [10–14]).

Due to the low intensity of cosmic rays at the highest energies, the primary mass cannot be measured directly but is inferred from the properties of the particle cascade initiated by a primary cosmic ray interacting with nuclei of the upper atmosphere. These extensive air showers can be observed with ground-based detectors over large areas. The mass and energy of the primary particles can be inferred from the properties of the longitudinal development of the cascade and the particle densities at the ground after making assumptions about the characteristics of high-energy interactions (see, e.g., [15] for a recent review).

The energy deposited in the atmosphere by the secondary air-shower particles is dominated by electron and positron contributions. The development of the corresponding *electromagnetic cascade* [16] is best described as a function of traversed air mass, usually referred to as the slant depth X . It is obtained by integrating the density of air along the direction of arrival of the air shower through the curved atmosphere,

$$X(z) = \int_z^\infty \rho(\mathbf{r}(z')) dz', \quad (1)$$

where $\rho(\mathbf{r}(z))$ is the density of air at a point with longitudinal coordinate z along the shower axis.

The depth at which the energy deposit reaches its maximum is the focus of this article. The *depth of shower maximum*, X_{\max} , is proportional to the logarithm of the mass A of the primary particle. However, due to fluctuations of the properties of the first few hadronic interactions in the cascade, the primary mass cannot be measured on an event-by-event basis but must be inferred statistically from the *distribution* of shower maxima of an ensemble of air showers. Given that nuclei of mass A_i produce a distribution $f_i(X_{\max})$, the overall X_{\max} distribution is composed of the superposition

$$f(X_{\max}) = \sum_i p_i f_i(X_{\max}), \quad (2)$$

where the fraction of primary particle of type i is given by p_i . The first two moments of $f(X_{\max})$, i.e., its mean and variance, $\langle X_{\max} \rangle$ and $\sigma(X_{\max})^2$ respectively, have been extensively studied in the literature [17–23]. They are to a good approximation linearly related to the first two moments of the distribution g of the logarithm of the primary mass A , which is given by the superposition

$$g(\ln A) = \sum_i p_i \delta(\ln A - \ln A_i), \quad (3)$$

where δ is the Dirac delta function.

The exact shape of $f_i(X_{\max})$ as well as the coefficients that relate the moments of $g(\ln A)$ to the ones of $f(X_{\max})$ depend on the details of hadronic interactions in air showers (see, e.g., [24–26]). On the one hand, this introduces considerable uncertainties in the interpretation of the X_{\max} distributions in terms of primary mass, since the modeling of these interactions relies on extrapolations of accelerator measurements to cosmic-ray energies. On the other hand, it implies that the X_{\max} distributions can be used to study properties of hadronic interactions at energies much larger than currently available in laboratory experiments. A recent example of such a study is the measurement of the proton-air cross section at $\sqrt{s} = 57$ TeV using the upper tail of the X_{\max} distribution [27].

Experimentally, the longitudinal profile of the energy deposit of an air shower in the atmosphere (and thus X_{\max})

can be determined by observing the fluorescence light emitted by nitrogen molecules excited by the charged particles of the shower. The amount of fluorescence light is proportional to the energy deposit [28,29] and can be detected by optical telescopes. The instrument used in this work is described in Sec. II and the reconstruction algorithms leading to an estimate of X_{\max} are laid out in Sec. III.

Previous measurements of X_{\max} with the fluorescence technique have concentrated on the determination of the mean and standard deviation of the X_{\max} distribution [30–33]. Whereas with these two moments the overall features of primary cosmic-ray composition can be studied, and composition fractions in a three-component model can even be derived, only the distribution contains the full information on composition and hadronic interactions that can be obtained from measurements of X_{\max} .

In this paper, we provide for the first time the measured X_{\max} distributions together with the necessary information to account for distortions induced by the measurement process. The relation between the true and observed X_{\max} distribution is

$$f_{\text{obs}}(X_{\max}^{\text{rec}}) = \int_0^{\infty} f(X_{\max}) \varepsilon(X_{\max}) R(X_{\max}^{\text{rec}} - X_{\max}) dX_{\max}, \quad (4)$$

i.e., the true distribution f is deformed by the detection efficiency ε and smeared by the detector resolution R that relates the true X_{\max} to the reconstructed one, X_{\max}^{rec} . For an ideal detector, ε is constant and R is close to a delta function. In Sec. IV, we describe the fiducial cuts applied to the data that guarantee a constant efficiency over a wide range of X_{\max} and the quality cuts that assure a good X_{\max} resolution. Parametrization of ε and R are given in Secs. V and VI.

Given f_{obs} , R and ε it is possible to invert Eq. (4) to obtain the true distribution $f(X_{\max})$. However, since f_{obs} is obtained from a limited number of events, its statistical uncertainties propagate into large uncertainties and negative correlations of the deconvoluted estimator of the true distribution, $\hat{f}(X_{\max})$. In practice, methods which reduce the uncertainties of $\hat{f}(X_{\max})$ by applying additional constraints to the solution exist (see, e.g., [34]), but these constraints introduce biases that are difficult to quantify. Therefore we choose to publish f_{obs} together with parametrizations of R and ε . In Sec. VII it is demonstrated how to derive $\langle X_{\max} \rangle$ and $\sigma(X_{\max})$ from f_{obs} , R and ε . The systematic uncertainties in the measurement of f_{obs} are discussed in Sec. VIII and validated in Sec. IX. In Sec. X the measured X_{\max} distributions will be shown in bins of energy reaching from $E = 10^{17.8}$ eV to $> 10^{19.5}$ eV together with a discussion of their first two moments.

II. THE PIERRE AUGER OBSERVATORY

In this paper we present data from the Pierre Auger Observatory [35]. It is located in the province of Mendoza, Argentina, and consists of a surface-detector array (SD) [36] and a fluorescence detector (FD) [37]. The SD is equipped with over 1600 water-Cherenkov detectors arranged in a triangular grid with a 1500 m spacing, detecting photons and charged particles at ground level. This 3000 km² array is overlooked by 24 fluorescence telescopes grouped in units of 6 at four locations on its periphery. Each telescope collects the light of air showers over an aperture of 3.8 m². The light is focused on a photomultiplier (PMT) camera with a 13 m² spherical mirror. Corrector lenses at the aperture minimize spherical aberrations of the shower image on the camera. Each camera is equipped with 440 PMT pixels, whose field of view is approximately 1.5°. One camera covers 30° in azimuth and elevations range from 1.5° to 30° above the horizon. The FD allows detection of the ultraviolet fluorescence light induced by the energy deposit of charged particles in the atmosphere and thus measures the longitudinal development of air showers. Whereas the SD has a duty cycle near 100%, the FD operates only during dark nights and under favorable meteorological conditions leading to a reduced duty cycle of about 13%.

Recent enhancements of the Observatory include a subarray of surface-detector stations with a spacing of 750 m and three additional fluorescence telescopes with a field of view from 30° to 60° co-located at one of the "standard" FD sites [38,39]. These instruments are not used in this work, but they will allow us to extend the analysis presented here to lower energies ($E \sim 10^{17}$ eV) [40].

In addition to the FD and SD, important prerequisites for a precise measurement of the energy and X_{\max} of showers are devices for the calibration of the instruments and the monitoring of the atmosphere.

The calibration of the fluorescence telescopes in terms of photons at aperture per ADC count in the PMTs is achieved by approximately yearly absolute calibrations with a Lambertian light source of known intensity and nightly relative calibrations with light-emitting diodes illuminating the FD cameras [41–43]. The molecular properties of the atmosphere at the time of data taking are obtained as the 3-hourly data tables provided by the global data assimilation system (GDAS) [44], which have been extensively cross-checked with radio soundings on site [45]. The aerosol content of the atmosphere during data taking is continuously monitored [46]. For this purpose, the vertical aerosol optical depth (VAOD) is measured on an hourly basis using laser shots provided by two central laser facilities [47,48] and cross-checked by lidars [49] operated at each FD site. Finally, clouds are detected via observations in the infrared by cameras installed at each FD site [50] and data from the Geostationary Operational Environmental Satellites (GOES) [51,52].

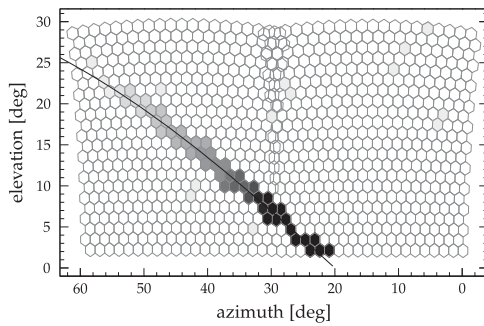
III. EVENT RECONSTRUCTION

The reconstruction of the data is performed within the off-line framework of the Pierre Auger Observatory [53]. Firstly, all PMT pixels belonging to the shower image on the camera are identified using a Hough transformation and subsequently fitted to reconstruct the plane spanned by the axis of the incoming shower and the telescope position. Within this plane a three-dimensional reconstruction of the shower-arrival direction is achieved by determining the geometry from the arrival times of the shower light as a function of viewing angle [54] and from the time of arrival of the shower front at ground level as measured by the surface-detector station closest to the shower axis. This leads to a *hybrid* estimate of the shower geometry with a precision of typically 0.6° for the arrival direction of the primary cosmic ray [55–57]. An example of the image of a shower in an FD camera is shown in Fig. 1(a) and the reconstructed geometry is shown in Fig. 1(b).

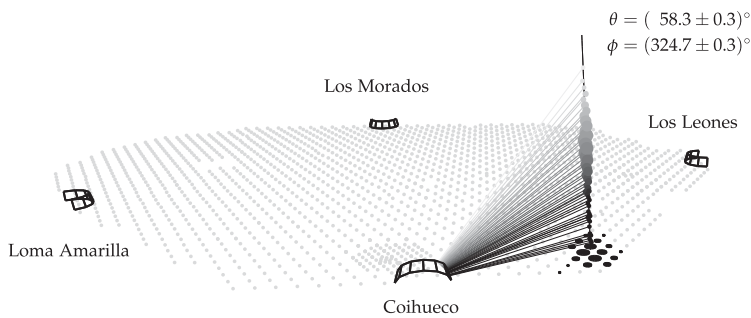
The detected signals in the PMTs of the telescope cameras as a function of time are then converted to a time trace of light at the aperture using the calibration of the absolute and relative response of the optical system. At

each time t_i , the signals of all PMTs with pointing directions within an opening angle ζ_{opt} with respect to the corresponding direction towards the shower are summed up. ζ_{opt} is determined on an event-by-event basis by maximizing the ratio of the collected signal to the accumulated noise induced by background light from the night sky. The average ζ_{opt} of the events used in this analysis is 1.3° , reaching up to 4° for showers detected close to the telescope. The amount of light outside of ζ_{opt} due to the finite width of the shower image [58,59] and the point spread function of the optical system [60,61] is corrected for in later stages of the reconstruction and multiply scattered light within ζ_{opt} is also accounted for [62–64].

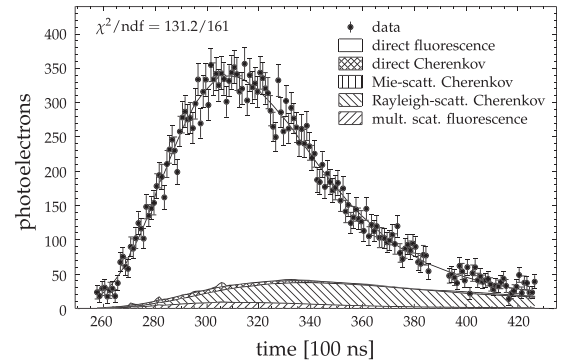
With the help of the reconstructed geometry, every time bin is projected to a piece of path length $\Delta\ell_i$ on the shower axis centered at height h_i and slant depth X_i . The latter is inferred by integrating the atmospheric density through a curved atmosphere. Given the distance to the shower, the light at the aperture can be projected to the shower axis to estimate the light emitted by the air-shower particles along $\Delta\ell_i$, taking into account the attenuation of light due to Rayleigh scattering on air and Mie scattering on aerosols.



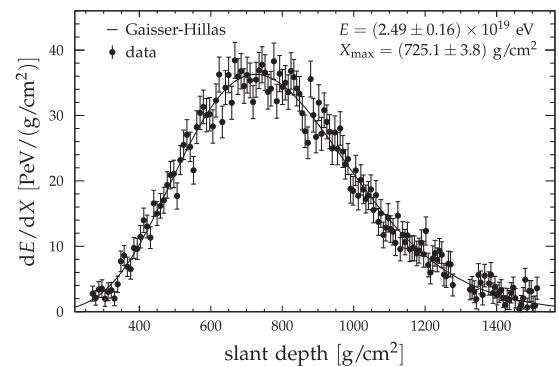
(a) Camera view. The timing of the pixel pulses is denoted by shades of gray (early = light, late = dark). The line shows the shower detector plane.



(b) Event geometry. Pixel viewing angles are shown as shaded lines and the shower light and surface detector signals are illustrated by markers of different size in logarithmic scale.



(c) Detected photoelectrons (dots) and the fitted contributions from components of the shower light (open and hatched areas).



(d) Longitudinal profile (dots) and Gaisser-Hillas function (line).

FIG. 1. Reconstruction of event 15346477.

The light from the shower is composed of fluorescence and Cherenkov photons. The production yield of the former is proportional to the energy deposited by the shower particles within the volume under study, and the latter depends on the number of charged particles above the energy threshold for Cherenkov emission. Due to the universality of the energy spectra of electrons and positrons in air showers [65–68], the energy deposit and the number of particles are proportional, and therefore an exact solution for the reconstruction of the longitudinal profile of either of these quantities exists [69]. An example of a profile of the reconstructed energy deposit can be seen in Fig. 1(d) and the contributions of the different light components to the detected signal are shown in Fig. 1(c). The Cherenkov light production is calculated following [67] and for the fluorescence-light emission along the shower we use the precise laboratory measurements of the fluorescence yield from [70,71].

In the final step of the reconstruction, the shower maximum and total energy are obtained from a log-likelihood fit of the number of photoelectrons detected in the PMTs using the Gaisser-Hillas function [72], f_{GH} , as a functional description of the dependence of the energy deposit on slant depth,

$$f_{\text{GH}}(X) = \left(\frac{dE}{dX} \right)_{\text{max}} \left(\frac{X - X_0}{X_{\text{max}} - X_0} \right)^{\frac{X_{\text{max}} - X_0}{\lambda}} e^{-\frac{X_{\text{max}} - X}{\lambda}}. \quad (5)$$

The two shape parameters X_0 and λ are constrained to their average values to allow for a gradual transition from a two- to a four-parameter fit depending on the amount of slant depth observed along the track and the number of detected photons from the respective event, cf. [69]. The constraints are set to the average values found in the ensemble of events for which an unconstrained fit with four parameters is possible. They are given by $\langle X_0 \rangle = -121 \text{ g/cm}^2$ and $\langle \lambda \rangle = 61 \text{ g/cm}^2$, and the observed standard deviations of these sample means are 172 and 13 g/cm^2 , respectively. An example of a Gaisser-Hillas function that has been obtained by the log-likelihood fit to the detected photoelectrons in Fig. 1(c) is shown in Fig. 1(d).

The calorimetric energy of the shower is obtained by the integration of f_{GH} and the total energy is derived after correcting for the “invisible” energy, carried away by neutrinos and muons. This correction has been estimated from hybrid data [73] and is of the order of 10% to 15% in the energy range relevant for this study.

IV. DATA SELECTION

The analysis presented in this paper is based on data collected by the Pierre Auger Observatory from the 1st of December 2004 to the 31st of December 2012 with the four standard FD sites. The initial data set consists of about 2.6×10^6 shower candidates that met the requirements of the four-stage trigger system of the data acquisition. Since

TABLE I. Event selection criteria, number of events after each cut and selection efficiency with respect to the previous cut.

Cut	Events	ϵ [%]
<i>Pre-selection:</i>		
Air-shower candidates	2573713	...
Hardware status	1920584	74.6
Aerosols	1569645	81.7
Hybrid geometry	564324	35.9
Profile reconstruction	539960	95.6
Clouds	432312	80.1
$E > 10^{17.8} \text{ eV}$	111194	25.7
<i>Quality and fiducial selection:</i>		
$P(\text{hybrid})$	105749	95.1
X_{max} observed	73361	69.4
Quality cuts	58305	79.5
Fiducial field of view	21125	36.2
Profile cuts	19947	94.4

only very loose criteria need to be fulfilled at a trigger level (basically a localized pattern of four pixels detecting a pulse in a consecutive time order), a further selection of the events is applied off-line as shown in Table I and explained in more detail in the following section.

A. Pre-selection

In the first step, a pre-selection is applied to the air-shower candidates resulting in a sample with minimum quality requirements suitable for subsequent physics analysis.

Only time periods with good data-taking conditions are selected using information from databases and results from off-line quality-assurance analyses. Concerning the status of the FD telescopes, a high-quality calibration of the gains of the PMTs of the FD cameras is required and runs with an uncertain relative timing with respect to the surface detector are rejected using information from the electronic logbook and the slow-control database. Furthermore, data from one telescope with misaligned optics are not used prior to the date of realignment. In total, this conservative selection based on the hardware status removes about 25% of the initial FD triggers. Additional database cuts are applied to assure a reliable correction of the attenuation of shower light due to aerosols: events are only accepted if a measurement of the aerosol content of the atmosphere is available within one hour of the time of data taking. Periods with poor viewing conditions are rejected by requiring that the measured VAOD, integrated from the ground to 3 km, is smaller than 0.1. These two requirements reduce the event sample by 18%.

For an analysis of the shower maximum as a function of energy, a full shower reconstruction of the events is needed. The requirement of a reconstructed hybrid geometry is fulfilled for about 36% of the events that survived the cuts on hardware status and atmospheric conditions. This relatively low efficiency is partially due to meteorological

events like sheet lightning at the horizon that pass the FD trigger criteria but are later discarded in the event reconstruction. Moreover, below $E = 10^{17.5}$ eV the probability for at least one triggered station in the standard 1.5 km grid of the surface detector drops quickly [74]. Therefore, a fit of the geometry using hybrid information is not possible for the majority of the showers of low energy that trigger the data-acquisition system of the FD.

A full reconstruction of the longitudinal profile, including energy and X_{\max} , is possible for most of the events with a hybrid geometry. Less than 5% of the events cannot be reconstructed, because too few profile points are available and/or their statistical precision is not sufficient. This occurs for either showers that are far away from the telescopes and close to the trigger threshold or for geometries pointing towards the telescope for which the trace of light at the camera is highly time compressed.

A possible reflection or shadowing of the light from the shower by clouds is excluded by combining information from the two laser facilities, the lidars and the cloud monitoring devices described in Sec. II. Events are accepted if no cloud is detected along the direction to the shower in either the telescope projection (cloud camera) or ground-level projection (GOES). Furthermore, events are accepted if the base height of the cloud layer as measured by both the lidars and lasers is above the geometrical field of view or 400 g/cm² above the fiducial field of view. The latter variable is explained in the next section. When none of these requirements are met, events are rejected if either the cloud camera or GOES indicates the presence of clouds in their respective projections. When no data from these monitors are available, the event is accepted if during the data taking the average cloud fraction as reported by lidars is below 25%, otherwise the event is not used. In that way, about 80% of the events are labeled as cloud-free.

In the final step of the pre-selection, we apply the lower energy threshold of this analysis, $E > 10^{17.8}$ eV, which reduces the data set by another 75% to 1.1×10^5 events available for further analysis.

B. Quality and fiducial selection

After the pre-selection described above, the remaining part of the analysis is focused on defining a subset of the data for which the distortion of the X_{\max} distribution is minimal, i.e., to achieve a good X_{\max} resolution via quality cuts and a uniform acceptance to showers in a large range of possible X_{\max} values.

Before giving the technical details of the selection below, it is instructive to discuss first some general considerations about the sampling of the X_{\max} distribution with fluorescence detectors. The position of the shower maximum can only be determined reliably if the X_{\max} point itself is observed within the field of view of the telescopes. The inference of X_{\max} from only the rising or falling edge of the

profile would introduce a large dependency of the results on the functional form of the profile (e.g., Gaisser-Hillas function) and the constraints on the shape parameters. The standard telescopes of the Pierre Auger Observatory are used to observe shower profiles within elevation angles from 1.5° to 30°. This *geometrical field of view* sets an upper and lower limit on the range of detectable shower maxima for a given arrival direction and core location, as illustrated in Fig. 2 for three example geometries. Nearby showers with an axis pointing away from the detector have the smallest acceptance for shallow showers [geometry (A)], whereas vertical showers cannot be used to sample the deep tail of the X_{\max} distribution for depths larger than the vertical depth of the ground level, which is about 860 g/cm² for the Malargüe site [geometry (B)]. Ideal conditions for measuring a wide range of X_{\max} are realized by a geometry that intercepts the upper field of view at low slant depths and by inclined arrival directions, for which the slant depth at the ground is large [geometry (C)]. The true distribution considered for all three cases is identical and indicated as a solid line. If the frequencies of shower maxima detected with all occurring geometries are collected in one histogram, then the resulting observed distribution will be under-sampled in the tails at small and large depths, as illustrated by the (A + B + C) distribution in the lower right of Fig. 2.

In addition to these simple geometrical constraints, the range of viewable depths is limited by the following two factors. Firstly, showers cannot be observed to arbitrary distances, but for a given energy the maximum viewing distance depends on background light from the night sky (as a function of elevation) and the transmissivity of the atmosphere. Therefore, even if shower (C) has a large geometrical field of view, in general X_{\max} will not be detectable at all depths along the shower axis. Secondly, if quality cuts are applied to the data, the available range in depth depends on the selection efficiency and therefore the corresponding *effective field of view* will usually be a complicated function of energy, elevation and distance to the shower maximum.

In this work, we follow a data-driven approach to minimize the deformation of the X_{\max} distributions caused by the effective field-of-view boundaries. As will be shown in the following, a fiducial selection can be applied to the data to select geometries preferentially with a large accessible field of view as in the case of the example geometry (C) resulting in an acceptance that is constant over a wide range of X_{\max} values. The different steps of the quality and fiducial selection are explained in the following.

1. Hybrid probability

After the pre-selection, only events with at least one triggered station of the SD remain in the data set. The maximum allowed distance of the nearest station to the reconstructed core is 1.5 km. For low energies and large

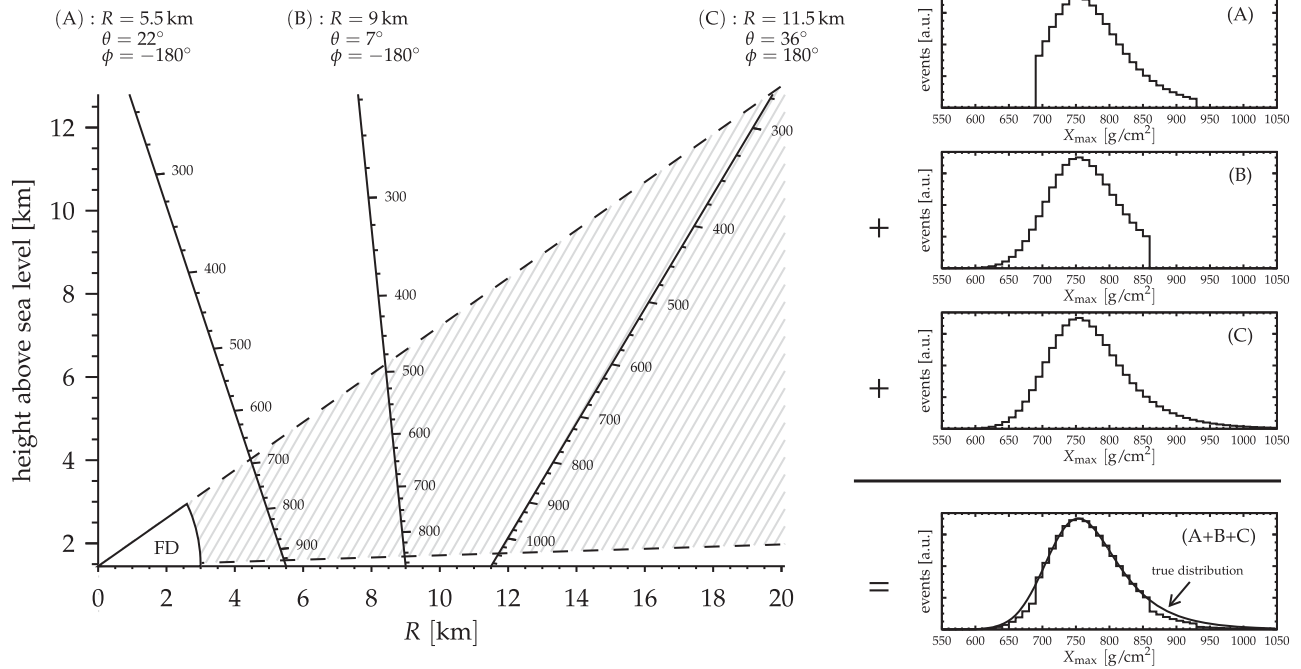


FIG. 2. Illustration of the influence of the FD field of view on the sampling of the X_{max} distribution. The slant-depth axes in g/cm^2 are shown on the left panel for three different examples of event geometries (A), (B) and (C) with different ground distances R , zenith angle θ and azimuthal angle ϕ . The FD field of view is indicated by the hatched area inside the dashed lines. Examples of correspondingly truncated X_{max} distributions are shown on the right panel together with their sum. For the purpose of this illustration, the same number of events for each geometry has been assumed.

zenith angles, the array is not fully efficient at these distances. To avoid a possible mass-composition bias due to the different trigger probabilities for proton- and iron-induced showers, events are only accepted if the average expected SD trigger probability is larger than 95%. The probability is estimated for each event given its energy, core location and zenith angle (cf. [75]). This cut removes about 5% of events, mainly at low energies.

2. X_{max} observed

It is required that the obtained X_{max} is within the observed profile range. Events where only the rising and/or falling edge of the profile has been observed are discarded, since in such cases the position of X_{max} cannot be reliably estimated. As can be seen in Table I, about 30% of the events from the tails of the X_{max} distribution are lost due to the limited field of view of the FD telescopes.

3. Quality cuts

Faint showers with a poor X_{max} resolution are rejected based on the *expected* precision of the X_{max} measurement, $\hat{\sigma}$, which is calculated in a semianalytic approach by expanding the Gaisser-Hillas function around X_{max} and then using this linearized version to propagate the statistical uncertainties of the number of photoelectrons at the PMT to an uncertainty of X_{max} . Only showers with $\hat{\sigma} < 40$ g/cm^2

are accepted. Moreover, geometries for which the shower light is expected to be observed at small angles with respect to the shower axis are rejected. Such events exhibit a large contribution of direct Cherenkov light that falls off exponentially with the observation angle. Therefore, even small uncertainties in the event geometry can change the reconstructed profile by a large amount. We studied the behavior of $\langle X_{\text{max}} \rangle$ as a function of the minimum observation angle, α_{min} , and found systematic deviations below $\alpha_{\text{min}} = 20^\circ$, which is therefore used as a lower limit on the allowed viewing angle. About 80% of the events fulfill these quality criteria.

4. Fiducial field of view

The aim of this selection is to minimize the influence of the effective field of view on the X_{max} distribution by selecting only type (C) geometries (cf. Fig. 2).

The quality variables $\hat{\sigma}$ and α_{min} are calculated for different X_{max} values in steps of 10 g/cm^2 along the shower axis within the geometrical field-of-view boundaries. In that way, the effective slant-depth range for high-quality showers can be exactly defined and it is given by the interval in slant depth for which both $\hat{\sigma} < 40$ g/cm^2 and $\alpha_{\text{min}} > 20^\circ$. The shower is accepted if this interval is *sufficiently large* to accommodate the bulk of the X_{max} distribution. The true X_{max} distribution is unfortunately not

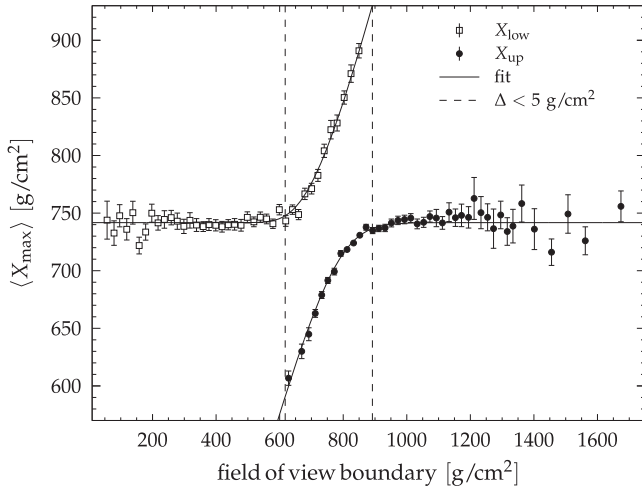


FIG. 3. $\langle X_{\max} \rangle$ for showers binned in X_l and X_u in the energy interval $10^{18.1}$ to $10^{18.2}$ eV. The solid line shows a fit with the truncated mean of an exponential function folded with a Gaussian [76], and the dashed line indicates the field-of-view value at which this function deviates by more than 5 g/cm^2 from its asymptotic value.

known at this stage of the analysis and therefore we study the differential behavior of $\langle X_{\max} \rangle$ on the lower and upper field-of-view boundary, X_l and X_u , for different energy intervals using data. An example is shown in Fig. 3. Once the field of view starts truncating the X_{\max} distribution, the observed $\langle X_{\max} \rangle$ deviates from its asymptotically unbiased value. We set the fiducial field-of-view boundaries at the values of X_l and X_u where a deviation of $\Delta > 5 \text{ g}/\text{cm}^2$ occurs to ensure that the overall sampling bias on $\langle X_{\max} \rangle$ is smaller than this value. The energy dependence of these boundaries is then parametrized as

$$X_{\text{fid}}^{l,u}(E) = \begin{cases} p_1 & ; \lg(E) > p_3, \\ p_1 + p_2(\lg(E) - p_3)^2 & ; \text{otherwise,} \end{cases} \quad (6)$$

with parameters $\mathbf{p}^u = (892, -186, 18.2)$ and $\mathbf{p}^l = (696, -34.6, 19.8)$ for the upper and lower boundary in slant depth, respectively. p_1 and p_2 are given in units of g/cm^2 and E is in eV. The requirement that $X_l \leq X_{\text{fid}}^l$ and $X_u \geq X_{\text{fid}}^u$ removes about 64% of all the remaining events.

5. Profile quality

In the last step of the selection, three more requirements on the quality of the profiles are applied. Firstly, events with gaps in the profile that are longer than 20% of its total observed length are excluded. Such gaps can occur for showers crossing several cameras, since the light in each camera is integrated only within the PMTs that are more than ζ_{opt} away from the camera border [see, e.g., the gap at around 1300 g/cm^2 in the profile shown in Fig. 1(d)]. Secondly, residual cloud contamination and horizontal nonuniformities of the aerosols may cause distortions of

the profile which can be identified with the goodness of the Gaisser-Hillas fit. We apply a standard-normal transformation to the χ^2 of the profile fit, $z = (\chi^2 - \text{ndf})/\sqrt{2\text{ndf}}$, and reject showers in the non-Gaussian tail at $> 2.2\sigma$. Finally, a minimum observed track length of $> 300 \text{ g}/\text{cm}^2$ is required. These cuts are not taken into account in the calculation of the effective view, but since the selection efficiency is better than 94%, the procedure explained in the last paragraph still yields a good approximation of the field-of-view boundaries.

In total, the quality and fiducial selection has an efficiency of 18%. This number is dominated by low-energy showers, where the profiles are faint and only a small phase space in distance and arrival direction provides a large effective field of view. Nevertheless, as shown in Sec. IX A, the efficiency of the quality and fiducial selection reaches close to 50% at high energies.

C. Final data set

After the application of all selection cuts, 19947 events from the four standard FD sites remain. Air showers that have been observed and selected at more than one FD site are combined by calculating the weighted average of X_{\max} and energy. This leads to 19759 independent air-shower events used for this analysis. Their X_{\max} and energy values are shown as a scatter plot in Fig. 4.

V. X_{\max} ACCEPTANCE

Even following the event selection described above, the probability to detect and select an air shower is not uniform for arbitrary values of X_{\max} . The corresponding X_{\max} acceptance needs to be evaluated to correct for residual distortions of the X_{\max} distribution. For this purpose we use a detailed, time-dependent simulation [74] of the

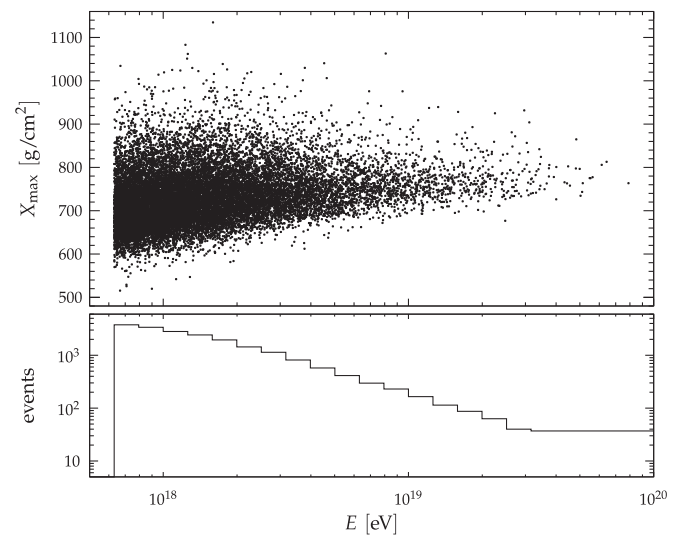


FIG. 4. Upper panel: X_{\max} and energy of the events used in this paper. Lower panel: Number of events in bins of energy.

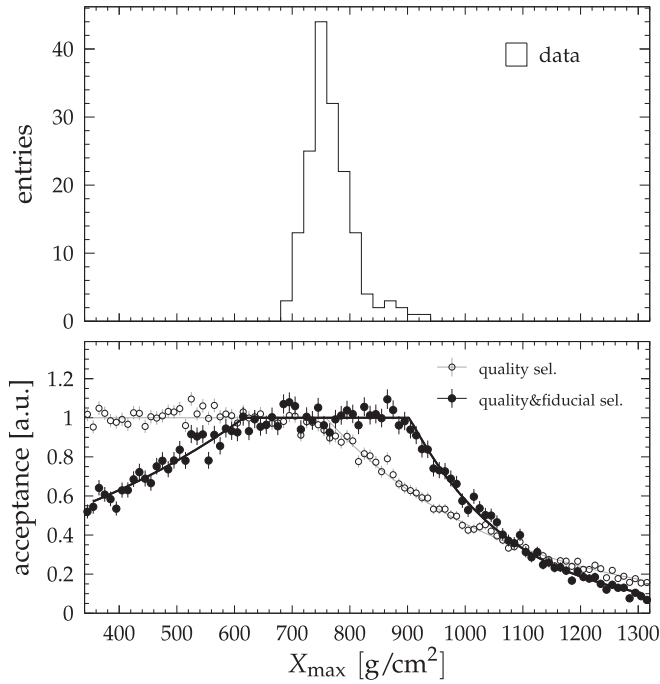


FIG. 5. Upper panel: Measured X_{\max} distribution [full selection, $19.0 < \lg(E/\text{eV}) < 19.1$]. Lower panel: Relative acceptance after quality cuts only (open markers) and after quality and fiducial cuts (filled markers). The parametrizations with Eq. (7) are indicated by lines.

atmosphere, the fluorescence and surface detector. The simulated events are reconstructed with the same algorithm as the data and the same selection criteria are applied. The acceptance is calculated from the ratio of selected to generated events.

The shape of the longitudinal energy-deposit profiles of air showers at ultrahigh energies is, to a good approximation, universal, i.e., it does not depend on the primary-particle type or details of the first interaction [77]. Therefore, after marginalizing over the distances to the detector and the arrival directions of the events, the acceptance depends *only* on X_{\max} and the calorimetric energy, but *not* on the primary mass or hadronic interaction model. For practical reasons, and since the calorimetric energies of different primaries with the same total energy are predicted to be within $\pm 3.5\%$ [78], we studied the acceptance as a function of total energy and X_{\max} .

In the lower panel of Fig. 5 an example of the acceptance with and without fiducial field-of-view cuts is shown. Since for the purpose of the measurement of the X_{\max} distribution only the shape of the acceptance is important, the curves have been normalized to give a maximum acceptance of 1. For comparison, the distribution of X_{\max} after the full selection is shown in the upper panel of the figure. As can be seen, the acceptance after application of fiducial cuts is constant over most of the range covered by the selected events. The acceptance without fiducial selection exhibits a constant part too, but it does not match the range of

measured events well because it starts to depart from unity already at around the mode of the measured distribution.

Numerically, the X_{\max} acceptance can be parametrized by an exponentially rising part, a central constant part and an exponentially falling part,

$$\varepsilon_{\text{rel}}(X_{\max}) = \begin{cases} e^{+\frac{X_{\max}-x_1}{\lambda_1}} & ; X_{\max} \leq x_1, \\ 1 & ; x_1 < X_{\max} \leq x_2, \\ e^{-\frac{X_{\max}-x_2}{\lambda_2}} & ; X_{\max} > x_2, \end{cases} \quad (7)$$

with energy-dependent parameters $(x_1, \lambda_1, x_2, \lambda_2)$ that are listed in Table II. The uncertainties given in this table are a combination of statistical and systematic uncertainties. The former are due to the limited number of simulated events and the latter are an estimate of the possible changes of the acceptance due to a mismatch of the optical efficiency, light production and atmospheric transmission between data and simulation. The energy scale uncertainty of 14% [61] gives an upper limit on the combined influence of these effects and therefore the systematic uncertainties have been obtained by reevaluating the acceptance for simulated events with an energy shifted by $\pm 14\%$.

VI. THE RESOLUTION OF X_{\max}

Besides the acceptance, another important ingredient in the measurement equation, cf. Eq. (4), is the X_{\max} resolution which determines the broadening of the original distribution by the statistical fluctuations of X_{\max}^{rec} around the true X_{\max} . The energy evolution of the X_{\max} resolution is shown in Fig. 6 where the band denotes its systematic uncertainty. As can be seen, the total X_{\max} resolution is better than 26 g/cm^2 at $10^{17.8} \text{ eV}$ and decreases with energy to reach about 15 g/cm^2 above $10^{19.3} \text{ eV}$. In the following we briefly discuss the individual contributions to the X_{\max} resolution.

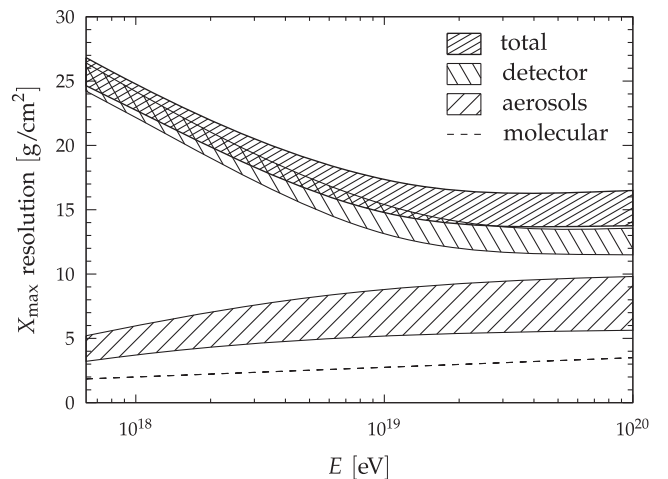


FIG. 6. X_{\max} resolution as a function of energy. Bands denote the estimated systematic uncertainties.

A. Detector

The largest contribution to the X_{\max} resolution originates from the overall performance of the detector system (including the atmosphere) to collect the light produced by air showers. The statistical uncertainty of the determination of the shower maximum from the Gaisser-Hillas fit, Eq. (5), is determined by the Poissonian fluctuations of the number of photoelectrons detected for each shower. Moreover, the uncertainty of the reconstruction of the arrival direction of a shower adds another statistical component to the resolution due to the conversion from the height of the shower maximum to its slant depth X_{\max} . These two contributions can be reliably determined by a full simulation of the measurement process, including optical efficiencies and transmission through the atmosphere [74,79]. For this purpose we use showers generated with Conex [80] and Sibyll2.1 [81] for proton and iron primaries and reweight the simulated events to match the observed X_{\max} distribution. Since high-energy showers are brighter than low-energy ones, the number of detected photoelectrons increases with energy and, correspondingly, the resolution improves. At $10^{17.8}$ eV, the simulations predict a resolution of about 25g/cm^2 that decreases to 12g/cm^2 towards the highest energies. The systematic uncertainty of these numbers is of the order of a few g/cm^2 and has been estimated by shifting the simulated energies by $\pm 14\%$ (as previously explained in the acceptance section).

Another detector-related contribution to the resolution originates from the uncertainties in the alignment of the telescopes. These are estimated by comparing the X_{\max} values from two reconstructions of the data set with different alignment constants. One set of constants has been obtained using the traditional technique of observing tracks of UV stars (see, e.g., [82]) and the other one used shower geometries from events reconstructed with the surface detector for a cross-calibration. The latter are the default constants in the standard reconstruction. Averaged over all 24 telescopes, the ΔX_{\max} values between events from the two reconstructions are found to be compatible, but systematic alignment differences are present on a telescope-by-telescope basis giving rise to a standard deviation of ΔX_{\max} that amounts to $s = (5 + 1.1 \lg(E/\text{EeV})) \text{g/cm}^2$. This is used as an estimate of the contribution of the telescope alignment to the X_{\max} resolution by adding $s/2 \pm s/2(\text{sys})$ to the previously discussed statistical part of the detector resolution in quadrature.

Finally, uncertainties in the relative timing between the FD and the SD can introduce additional X_{\max} uncertainties, but even for jitters of the time stamps provided by the Global Positioning System as large as 100 ns the effect on the X_{\max} resolution is $\lesssim 3\text{g/cm}^2$ and can thus be neglected.

The estimated overall contribution of the detector-related uncertainties to the X_{\max} resolution is shown as a back-slashed band in Fig. 6.

B. Aerosols

Two sources of statistical uncertainty of the aerosol measurements contribute to the X_{\max} resolution. Firstly, the measurement itself is affected by fluctuations of the night sky background and the number of photons received from the laser as well as by the time variability of the aerosol content within the one-hour averages. The sum of both contributions is estimated using the standard deviation of the quarter-hourly measurements [48,83] of the VAOD and propagated to the X_{\max} uncertainty during reconstruction. Secondly, nonuniformities of the aerosol layers across the array are estimated using the differences of the VAOD measurements from different FD sites and propagated to an X_{\max} uncertainty [46].

The quadratic sum of both sources is shown as the lowest of the dashed bands in Fig. 6, where the systematic uncertainty given by the width of the band is due to the uncertainty of the contribution from the horizontal non-uniformity.

C. Molecular atmosphere

Finally, the precision to which the density profiles as a function of height are known gives another contribution to the X_{\max} resolution. It is estimated from the spread of differences between shower reconstructions using the density profile from GDAS and shower reconstructions using actual balloon soundings, which are available for parts of the data (see Fig. 14 in [45]). This contribution is shown as a dashed line in Fig. 6.

D. Parametrization of the resolution

The statistical part of the detector resolution arises from the statistical uncertainty in the determination of X_{\max} and from the statistical uncertainty caused by the conversion from the height of the maximum in the atmosphere to the corresponding depth of X_{\max} . Simulations of these two contributions show that they are well described by the sum of two Gaussian distributions. The remaining component to the resolution term of Eq. (4) is also Gaussian and describes the contributions from the calibration of the detector and from the influence of the atmosphere. The overall resolution of X_{\max} can therefore be parametrized as

$$R(X_{\max}^{\text{rec}} - X_{\max}) = fG(\sigma_1) + (1-f)G(\sigma_2) \quad (8)$$

where $G(\sigma)$ denotes a Gaussian distribution with mean zero and width σ . The three parameters f , σ_1 and σ_2 are listed in Table III as a function of energy together with their systematic uncertainties.

VII. X_{\max} MOMENTS

The parametrized acceptance and resolution together with the measured X_{\max} distributions provide the full information on the shower development for any type of physics analysis. However, the first two moments of the

distribution, $\langle X_{\max} \rangle$ and $\sigma(X_{\max})$, provide a compact way to characterize the main features of the distribution. In this section we describe three methods that have been explored to derive the X_{\max} moments from our data.

A. Event weighting

In this approach each selected shower is weighted according to the acceptance corresponding to the position of the shower maximum. Events in the region of constant acceptance are assigned a weight of one. The underrepresentation of the distribution in the nonflat part is compensated for by assigning the inverse of the relative acceptance as a weight to showers detected in this region, $w = 1/\varepsilon_{\text{rel}}(X_{\max})$, cf. (7). The unbiased moments can be reconstructed using the equations for the weighted moments (cf. A 1). $\sigma(X_{\max})$ is then estimated by subtracting the X_{\max} resolution in quadrature from the weighted standard deviation.

B. Λ_η method

The tail of the X_{\max} distribution at large values is related to the distribution of the first interactions of the primary particles in the atmosphere (see, e.g., [84]). Therefore, it is possible to describe the true distribution of deep showers by an exponential function. We subdivide the measured distribution into three regions: the central part with a constant acceptance, where the distribution can be measured without distortions, and the shallow and deep regions where the relative acceptance departs from unity. Here, for the purpose of calculating the first two moments of the distribution, the data are replaced by an exponential function that has been fitted to the two tails of the distribution, taking the acceptance into account (see A 2). A fraction η of the events in the tail is fitted to obtain the slope Λ_η , similar to the method that has been used previously to estimate the interaction length of proton-air collisions [27,85]. The mean and standard deviation of the distribution are then calculated by combining the moments of the undistorted region with the exponential prolongation in the tails. In practice, since the X_{\max} distributions have a steep rising edge, the low- X_{\max} part is almost fully contained within the fiducial field of view and only the exponential tail at deep X_{\max} values contributes to a correction with respect to the moments calculated without taking into account the acceptance. In the final step, $\sigma(X_{\max})$ is obtained by subtracting the X_{\max} resolution in quadrature from the variance derived with this procedure.

C. Deconvolution

As a third method we investigated the possibility to solve Eq. (4) for the true X_{\max} distribution $f(X_{\max})$ and to subsequently determine the mean and variance of the solution. For this purpose, Eq. (4) can be transformed into a matrix equation by a piecewise binning in X_{\max} and then

be solved by matrix inversion. To overcome the well-known problem of large variances and negative correlations inherent to this approach (see, e.g., [34]), we applied two different deconvolution algorithms to the data, namely regularized unfolding using singular value decomposition (SVD) of the migration matrix [86] and iterative Bayesian deconvolution [87].

D. Comparison

Each of these three methods has its own conceptual advantages and disadvantages. The main virtue of the event weighting is that it is purely data driven. However, with the help of simulated data it was found that this approach has the largest statistical variance of the three methods, resulting from large weights that inevitably occur when a shower is detected in a low-acceptance region.

The estimators of the moments resulting from the Λ_η method are also mainly determined by the measured data since the fiducial field of view ensures that only the small part of the distribution outside the range of constant acceptance needs to be extrapolated. The description of the tail of the distribution with an exponential function has a sound theoretical motivation. Obviously, this method is not applicable when the main part of the distribution is affected by distortions from the acceptance.

Deconvolution is in principle the most mathematically rigorous method to correct the measured distributions for the acceptance and resolution. However, in order to cope with the large variance of the exact solution, unfolding algorithms need to impose additional constraints to the data (such as minimal total curvature [88] in case of the SVD approach), that are less physically motivated than, e.g., an exponential prolongation of the distribution.

In the following we will use the Λ_η method as the default way to estimate the moments of the X_{\max} distribution. A comparison with the results of the other methods will be discussed in Sec. IX. It is worthwhile noting that the moments calculated without taking into account the acceptance are close to the ones estimated by the three methods described above, i.e., in the range of $[0, +3]$ g/cm² for $\langle X_{\max} \rangle$ and $[0, +5]$ g/cm² for $\sigma(X_{\max})$. Assuming a perfect X_{\max} resolution would change $\sigma(X_{\max})$ by $[-5, -3]$ g/cm². Thus, the estimates of $\langle X_{\max} \rangle$ and $\sigma(X_{\max})$ are robust with respect to uncertainties on the acceptance and resolution.

VIII. SYSTEMATIC UNCERTAINTIES

A. X_{\max} scale

The systematic uncertainty of the X_{\max} scale, i.e., the precision with which the absolute value of X_{\max} can be measured, is shown in Fig. 7. As can be seen, this uncertainty is ≤ 10 g/cm² at all energies. At low energies, the scale uncertainty is dominated by the uncertainties in the event reconstruction and at high energies the atmospheric uncertainties prevail. The different contributions to

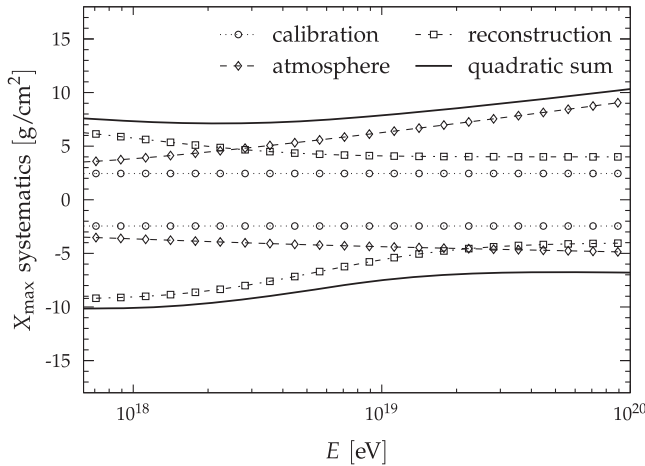


FIG. 7. Systematic uncertainties in the X_{\max} scale as a function of energy.

the X_{\max} scale uncertainty are discussed in the following. The full covariance matrix of the X_{\max} scale uncertainty is available at [89].

f. Detector calibration The uncertainties in the relative timing between the FD sites and SD stations, the optical alignment of the telescopes and the calibration of the absolute gains of photomultipliers of the cameras have been found to give only a minor contribution to the X_{\max} scale uncertainty. Their overall contribution is estimated to be less than 3 g/cm² by evaluating the stability of the X_{\max} reconstruction under a variation of the relative timing by its uncertainty of ± 100 ns [90], using different versions of the gain calibration and by application of an independent set of alignment constants (cf. Sec. VI A).

g. Reconstruction The reconstruction algorithms described in Sec. III are tested by studying the average difference between the reconstructed and generated X_{\max} for simulated data. The X_{\max} bias is found to be less than 3.5 g/cm² and is corrected for during data analysis. The dependence of the results on the particular choice of function fitted to the longitudinal profile has been checked by replacing the Gaisser-Hillas function from Eq. (5) by a Gaussian distribution in shower age $s = 3X/(X + 2X_{\max})$, yielding compatible results within 4 g/cm² for either of the variants proposed in [91] and [92]. Furthermore, we tested the influence of the constraints $\langle X_0 \rangle$ and $\langle \lambda \rangle$ used in the Gaisser-Hillas fit by altering their values by the standard deviations given in Sec. III, which changes the X_{\max} on average by less than 3.7 g/cm². Since the values obtained in these three studies (bias of simulated data, Gaussian in age and variation of constraints) are just different ways of assessing the same systematic effect, we do not add them in quadrature but assign the maximum deviation of 4 g/cm² as an estimate of the X_{\max} scale uncertainty originating from the event reconstruction.

In addition to this validation of the reconstruction of the longitudinal shower development, we have also studied our

understanding of the lateral distribution of fluorescence and Cherenkov light and its image on the FD cameras. For this purpose, the average of the light detected outside the collection angle ζ_{opt} in data is compared to the amount of light expected due to the point spread function of the optical system and the lateral distribution of the light from the shower. We find that the fraction of light outside ζ_{opt} is larger in data than in the expectation and that the ratio of observed-to-expected light depends on shower age. The corresponding correction of the data during the reconstruction leads to a shift of X_{\max} of +8.3 g/cm² at 10^{17.8} eV which decreases to +1.3 g/cm² at the highest energies. Since the reason for the mismatch between the observed and expected distribution of the light on the camera is not understood, the full shift is included as a one-sided systematic uncertainty. With the help of simulated data we estimated the precision with which the lateral-light distribution can be measured. This leads to a total uncertainty from the knowledge of the lateral-light distribution of $+4.7$ g/cm² at 10^{17.8} eV and $+2.1$ g/cm² at the highest energies.

h. Atmosphere The absolute yield of fluorescence-light production of air showers in the atmosphere is known with a precision of 4% [71]. The corresponding uncertainty of the relative composition of fluorescence and Cherenkov light leads to an uncertainty on the shape of the reconstructed longitudinal profiles and an X_{\max} uncertainty of 0.4 g/cm². Moreover, the uncertainty in the wavelength dependence of the fluorescence yield introduces an X_{\max} uncertainty of 0.2 g/cm². The amount of multiply scattered light to be taken into account during the reconstruction depends on the shape and size of the aerosols in the atmosphere. In [93] the systematic effect on the X_{\max} scale has been estimated to be ≤ 2 g/cm². The systematic uncertainty of the measurement of the aerosol concentration and its horizontal uniformity are discussed in [46,48,83]. They give rise to an energy-dependent systematic uncertainty of X_{\max} , since high-energy showers can be detected at large distances and have a correspondingly larger correction for the light transmission between the shower and the detector. Thus, at the highest energies the X_{\max} scale uncertainty is dominated by uncertainty of the atmospheric monitoring, contributing $+7.8$ g/cm² in the last energy bin.

B. X_{\max} moments

The systematic uncertainties of $\langle X_{\max} \rangle$ and $\sigma(X_{\max})$ are dominated by the X_{\max} scale uncertainty and by the uncertainty of the X_{\max} resolution, respectively, which have been discussed previously (Secs. VIII and VI).

In addition, the uncertainties of the parameters of the X_{\max} acceptance, Eq. (7), are propagated to obtain the corresponding uncertainties of the moments leading to ≤ 1.5 g/cm² and ≤ 2.7 g/cm² for $\langle X_{\max} \rangle$ and $\sigma(X_{\max})$, respectively.

Finally, we have also studied the possible bias of the moments originating from the difference in invisible energy between heavy and light primaries. In the energy reconstruction, the *average* invisible energy is corrected for. If the primary flux is composed of different nuclei, then the energy of heavy nuclei will be systematically underestimated and the one of light nuclei will be overestimated on an event-by-event basis. As a consequence, the single-nuclei spectra as a function of reconstructed energy will be shifted with respect to each other and the fraction of nuclei in a bin of reconstructed energy will be biased. To study consequences of this fraction bias on the moments, we consider the extreme case of a mixture of proton and iron primaries and an invisible energy as predicted by the Epos-LHC model. The observed energy spectrum after selection follows, to a good approximation, a power law with a spectral index $\gamma = -1.76 - 0.44 \lg(E/E\text{eV})$. The potential bias of the moments due to the invisible-energy correction is then found to be $\delta\langle X_{\text{max}} \rangle \leq +1.2 \text{ g/cm}^2$ and $\delta\sigma(X_{\text{max}}) \leq +0.5 \text{ g/cm}^2$ which we add as a one-sided systematic uncertainty of the estimated moments.

IX. CROSS-CHECKS

The systematic uncertainties estimated in the previous section have been carefully validated by performing numerous cross-checks on the stability of the results and the description of the data by the detector simulation. In the following we present a few of the most significant studies.

A. Selection efficiency

A potential bias from the quality and fiducial selection can be checked by comparing its efficiency as a function of

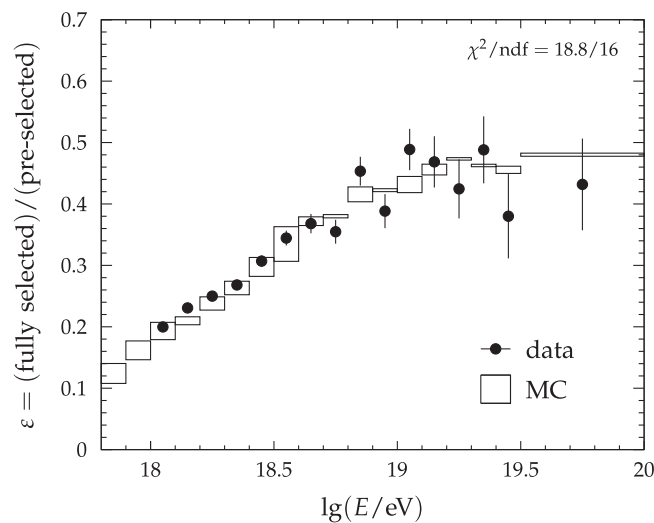


FIG. 8. Efficiency of the quality and fiducial selection for data and Monte Carlo simulation (MC). The χ^2 of the sum of the (data-MC) residuals is quoted on the top right.

energy for data and simulated events. For this purpose, we use the independent measurement of air showers provided by the SD and measure the fraction of events surviving the quality and fiducial cuts out of the total sample of pre-selected events. This estimate of the selection efficiency is shown in Fig. 8 as a function of SD energy above 10^{18} eV . Below that energy, the SD trigger efficiency drops below 50%. The comparison to the simulated data shows a good overall agreement and we conclude that the selection efficiency is fully described by our simulation.

B. Detector resolution

The understanding of the detector resolution is checked with the help of showers that had been detected by more than one FD site. The distribution of the differences in X_{max} as reconstructed for each site independently gives an estimate of the X_{max} resolution. As can be seen in Fig. 9, the distribution of the data and its standard deviation agrees well with the one obtained for simulated air showers.

C. Analysis of simulated data

The full analysis chain can be validated by applying it to simulated data and comparing the estimated X_{max} moments to the ones at generator level. This test has been performed in two variants. In the first test, we re-evaluated the fiducial field-of-view cuts from the simulated data to obtain the optimal boundaries with the algorithm described in Sec. IV B. Furthermore, we also tested the performance when applying the range of the fiducial fields of view derived from the real data [cf. Eq. (6)]. This second test is more conservative as it validates the ability of the analysis

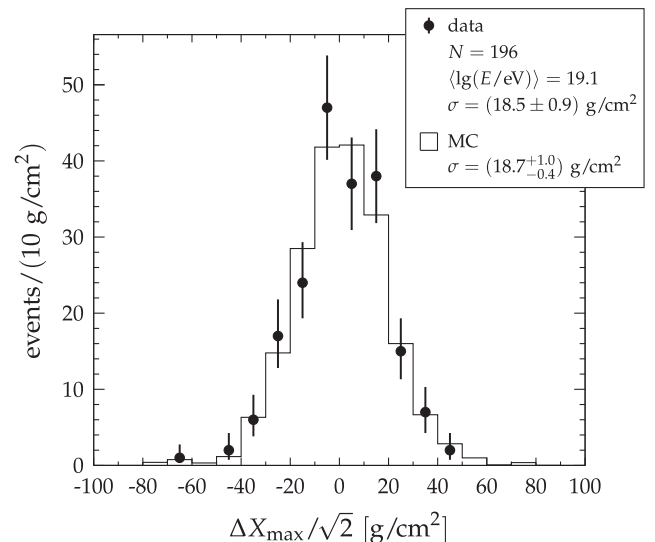


FIG. 9. Distribution of X_{max} differences for events measured by more than one FD station. The quoted uncertainties for the standard deviation σ are statistical for data and systematic for MC. The latter are dominated by the uncertainty in the contribution of the alignment and aerosols to the resolution (cf. Sec. VI).

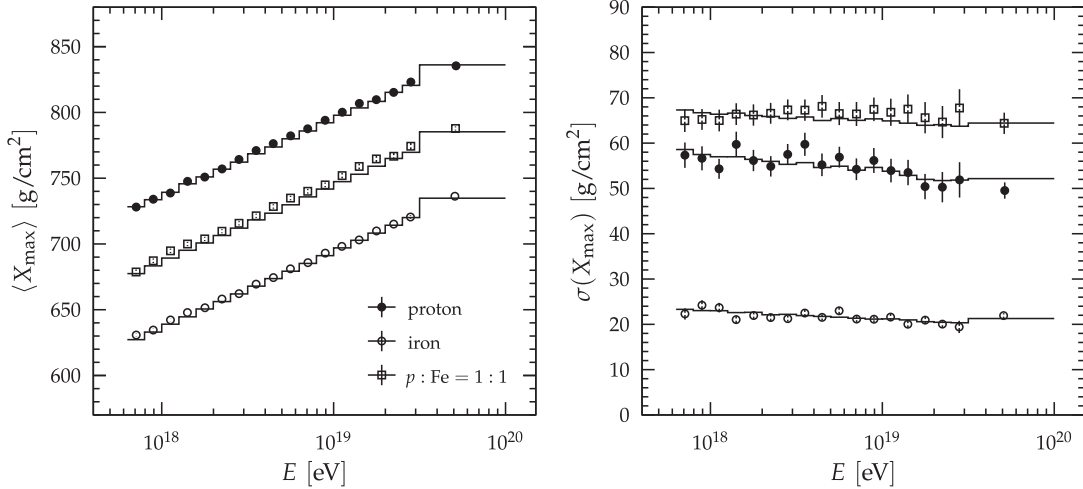


FIG. 10. Reconstructed $\langle X_{\max} \rangle$ and $\sigma(X_{\max})$ (symbols) obtained from simulated data for different compositions using the SIBYLL2.1 interaction model. The moments of the generated events before detector simulation are shown as solid lines.

chain to recover the true moments of input distributions it has not been optimized for. This is an important feature needed for the comparison of the data to X_{\max} distributions that differ from the observed ones, e.g., for fitting different composition hypotheses to the data (cf. [94]).

In both cases, the moments of the input distribution can be reproduced well. The results from the test using the field-of-view cuts from Eq. (6) are shown in Fig. 10. As can be seen, the simulated measurements of $\langle X_{\max} \rangle$ and $\sigma(X_{\max})$ agree within 2 g/cm² with the generated values in case of a pure-proton or pure-iron composition. Slightly larger biases are visible for a mixed composition with 50% proton and 50% iron where $\langle X_{\max} \rangle$ deviates by about +4 g/cm² from the generated value. This bias can be partially attributed to the systematic uncertainty of the acceptance correction and the application of the average invisible-energy correction during the reconstruction (cf. Sec. VIII B). We conclude that the analysis chain performs well, even for the case where the cuts of the fiducial fields of view are not reoptimized to the input distributions.

D. FD sites

The moments of the X_{\max} distribution can be measured for each of the four FD sites separately to check for possible differences due to misalignment or systematic differences in the PMT calibration. Moreover, the four sites (denoted as LL, LM, LA and CO in the following) are located at different altitudes with a maximum difference between LL at 1416.2 m and CO at 1712.3 m above sea level. Correspondingly, the aerosols, which have usually their largest concentration near ground level, are less important for CO than for the other sites. The results can be seen in Fig. 11(a), where the differences of the individual $\langle X_{\max} \rangle$ and $\sigma(X_{\max})$ with respect to the results from the full data sample are shown. A χ^2 test of the compatibility with zero

yields 42.7 and 46.5 for $\Delta\langle X_{\max} \rangle$ and $\Delta\sigma(X_{\max})$, respectively. Taking into account that the comparison is done with the mean of the data, the number of degrees of freedom is 45 in each case and it can therefore be concluded that the measurements at the individual sites are indeed statistically independent estimates of the same quantity. Averaging the Δ values over energy for each station, the maximum deviation from zero is found to be 2.5 ± 1 g/cm² for the $\langle X_{\max} \rangle$ measured in CO, which is well within the systematic uncertainties for calibration and aerosols listed in Sec. VIII.

E. Zenith angle

The electromagnetic part of an air shower develops as a function of traversed air mass. Therefore, the position of the shower maximum expressed in slant depth does not depend on the zenith angle of the arrival direction of the cosmic-ray particle. Accordingly, $\langle X_{\max} \rangle$ and $\sigma(X_{\max})$ are also expected to be independent of the zenith angle.

However, showers at different zenith angles reach their maximum at different heights above the ground and in different regions of the detector acceptance. Therefore, the study of a possible zenith-angle dependence of the moments of the X_{\max} distribution provides an important end-to-end cross-check of the understanding of the atmosphere and the detector.

For the purpose of this check, the data set is divided into two subsamples of approximately equal size at the median zenith angle $(\cos\theta)_{\text{med}} = 0.795 - 0.092 \lg(E/E_{\text{TeV}})$ and the acceptance and resolution are reevaluated for these samples. This yields estimates of the X_{\max} moments for the “near-vertical” and “inclined” data and their difference is shown in Fig. 11(b). No significant difference is found over the whole energy range for $\langle X_{\max} \rangle$. At low energies, the near-vertical $\sigma(X_{\max})$ is smaller by about 5 ± 2 g/cm² than the inclined one. Assuming that either one of the two

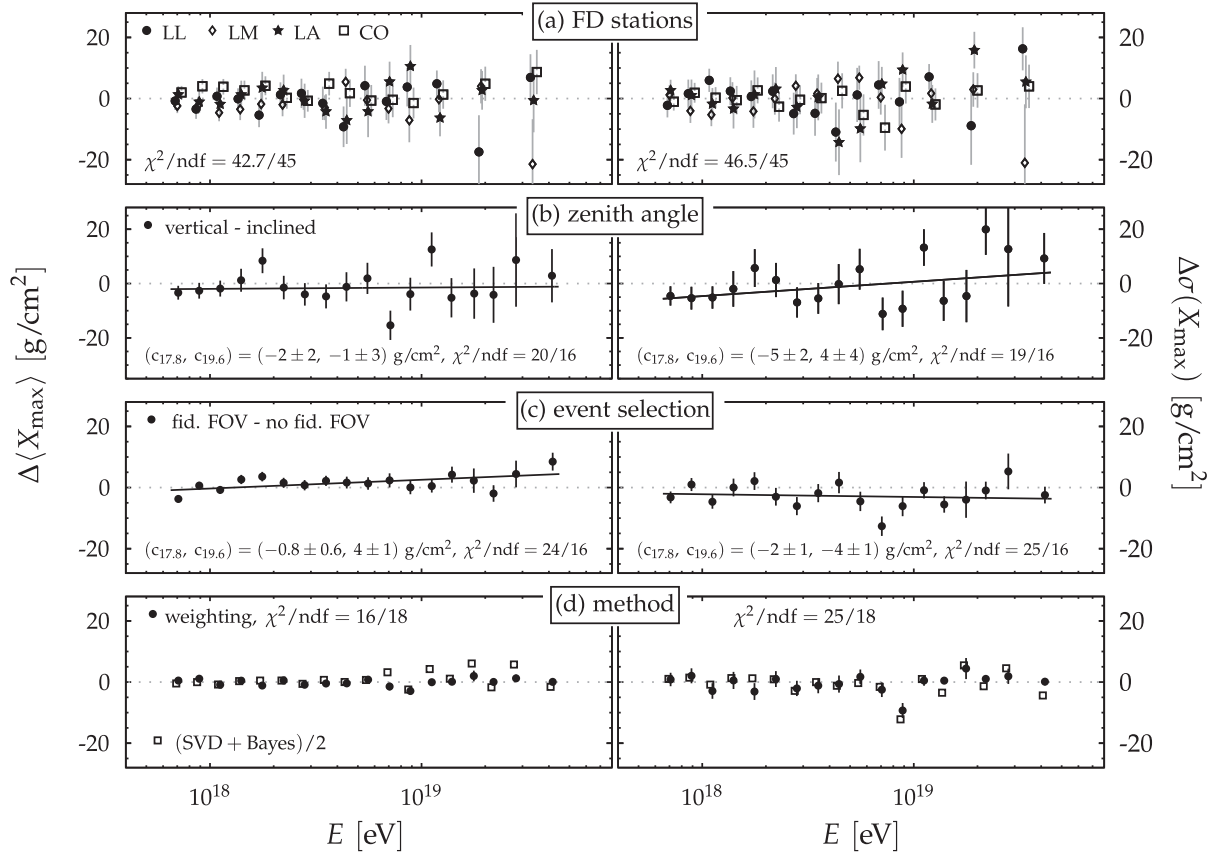


FIG. 11. Cross-checks. (a) Difference of moments obtained from each FD site separately to the results using data from all sites. The global χ^2/ndf with respect to zero is given. (b) Subdivision of the data set in showers with near-vertical and inclined arrival directions. Parameters of a linear fit in $\lg(E)$ are shown with supporting points $c_{17.8}$ and $c_{19.6}$ at the centers of the first and last bin of $10^{17.85}$ and $10^{19.62}$ eV. (c) Difference of results with and without fiducial field-of-view selection. Parameters are the same as in panel (b). (d) Comparison of different methods to estimate $\langle X_{\text{max}} \rangle$ and $\sigma(X_{\text{max}})$. The difference from the default method is shown. The average from the two deconvolution methods (SVD and Bayesian) is shown without error bars (see text). For the weighting method, the χ^2/ndf with respect to zero is given.

subsamples gives a fair estimate of the true width, the corresponding bias of the full data sample would be 2.2 ± 1 g/cm², which is compatible with the systematic uncertainty of the combined $\sigma(X_{\text{max}})$ at low energies.

F. Event selection

The dependence of the results on details of the fiducial field of view as well as on the acceptance and resolution is studied by completely removing the fiducial field-of-view selection. The data selected in this way is then corrected with the appropriate acceptance and resolution using the event weighting method. The difference from the default moments is shown in Fig. 11(c), where the error bars take into account the correlation between the results due to the fact that they partially share the same events. As can be seen, the differences are within 4 g/cm² on average for both, $\langle X_{\text{max}} \rangle$ and $\sigma(X_{\text{max}})$. Due to the larger importance of the acceptance correction in the case of estimating the moments without fiducial cuts, it is expected that the

corresponding systematic uncertainties are larger than the ones discussed in Sec. VIII. Moreover, the X_{max} resolution of this selection is worse than the default discussed in Sec. VI. Given these differences, we conclude that the two results are in good overall agreement.

G. Analysis method

The different methods for the estimation of the X_{max} moments that were introduced in Sec. VII are compared in Fig. 11(d). The event weighting yields results that are very similar to the Λ_η method. The presented statistical uncertainties account for the correlation of the two estimates which use exactly the same data set. The results of the two methods are found to be compatible with a χ^2/ndf of 0.9 and 1.4 for $\langle X_{\text{max}} \rangle$ and $\sigma(X_{\text{max}})$, respectively.

The moments calculated from the deconvoluted X_{max} distributions using either the Bayesian or SVD method were found to be compatible within 1 g/cm². Therefore, in Fig. 11(d) the differences from the default result are shown

for the arithmetic average of the two. As can be seen, they scatter around zero with no visible systematic trend. The statistical uncertainties of these differences have not been evaluated, but an estimate of their variances can be obtained by assuming proportionality to the statistical uncertainties of the default results. A χ^2/ndf of 1 is obtained when uncertainties are assumed to be 59% and 90% of those given in Table IV for $\langle X_{\text{max}} \rangle$ and $\sigma(X_{\text{max}})$, respectively. Therefore, it can be concluded that the moments obtained

by deconvolution agree with the default results within the statistical uncertainties of the latter.

X. RESULTS AND DISCUSSION

In the following we present the results of this analysis in energy bins of $\Delta \lg(E/\text{eV}) = 0.1$. Above $10^{19.5}$ eV an integral bin is used. The highest-energy event in this data sample had been detected by all four FD sites and its reconstructed energy and shower maximum are

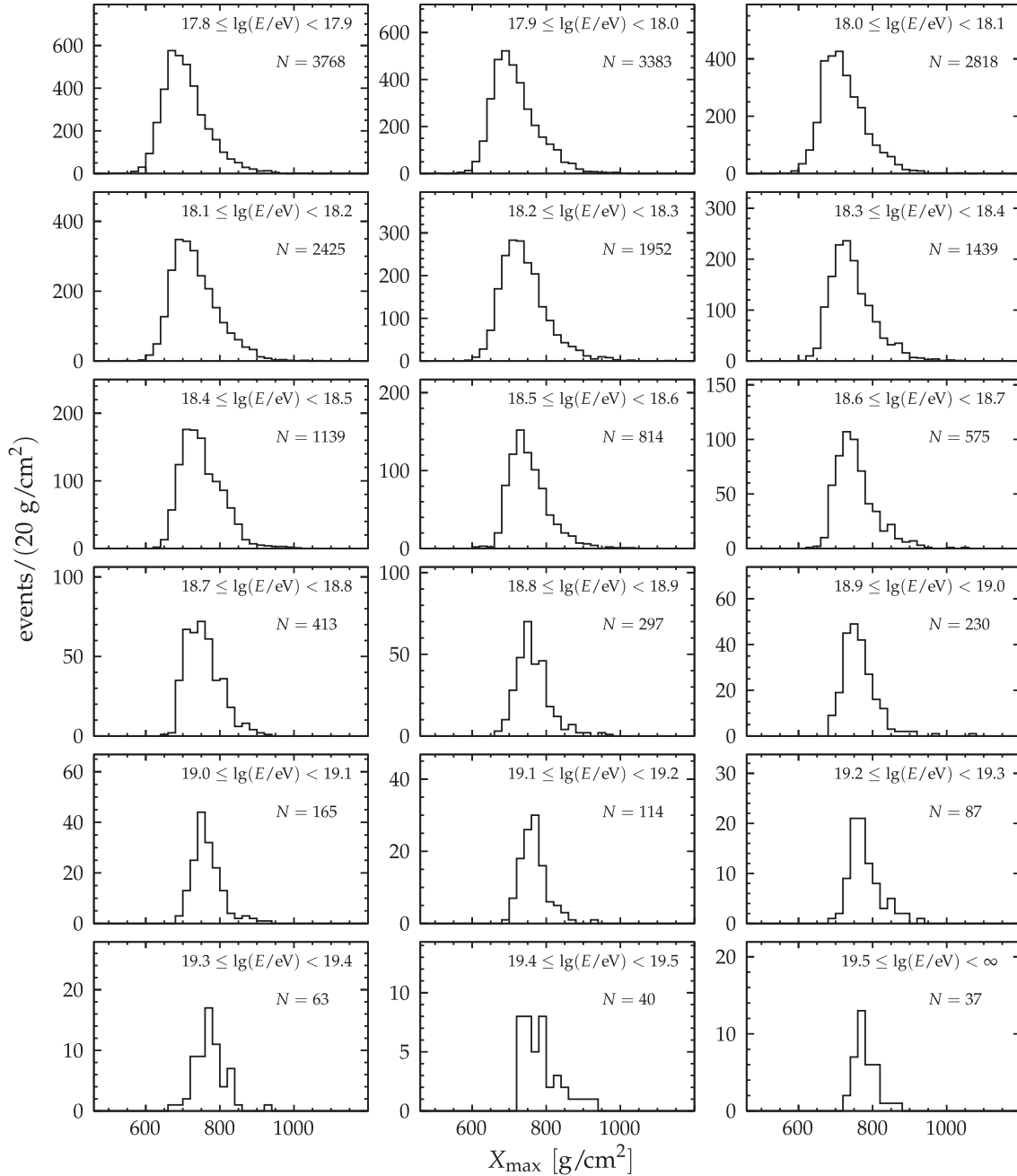


FIG. 12. X_{max} distributions for different energy intervals.

$E = (7.9 \pm 0.3) \times 10^{19}$ eV and $X_{\max} = 762 \pm 2$ g/cm², respectively, where the uncertainties are statistical only.

The X_{\max} distributions after event selection are shown in Fig. 12. These are the “raw” distributions [$f_{\text{obs}}(X_{\max}^{\text{rec}})$ in Eq. (4)] that still include effects of the detector resolution and the acceptance. Electronically readable tables of the distributions, as well as the parameters of the resolution and acceptance, are available at [89]. A thorough discussion of the distributions can be found in an accompanying paper [94], where a fit of the data with simulated templates for different primary masses is presented.

In this paper we will concentrate on the discussion of the first two moments of the X_{\max} distribution, $\langle X_{\max} \rangle$ and $\sigma(X_{\max})$, which are listed in Table IV together with their statistical and systematic uncertainties. The statistical uncertainties are calculated with the parametric bootstrap method. For this purpose, the data are fitted with Eq. (4) assuming the functional form suggested in [76] as $f(X_{\max})$. Given this parametric model of the true X_{\max} distribution, realizations of the measurement are repeatedly drawn from Eq. (4) with the number of events being equal to the ones observed. After application of the Λ_{η} analysis described in Sec. VII B, distributions of X_{\max} and $\sigma(X_{\max})$ are obtained from which the statistical uncertainties of the measured moments are estimated.

A comparison of the predictions of the moments from simulations for proton- and iron-induced air showers to the data is shown in Fig. 13. The simulations have been performed using the three contemporary hadronic interaction models that were either tuned to recent LHC data (QGSJetII-04 [95,96], Epos-LHC [97,98]) or found in good agreement with these measurements (Sibyll2.1 [81], see [99]). It is worth noting that the energy of the first data

point in Fig. 13 corresponds to a center-of-mass energy that is only four times larger than the one currently available at the LHC ($\sqrt{s} = 8$ TeV). Therefore, unless the models have deficiencies in phase-space regions that are not covered well by LHC measurements, the uncertainties due to the extrapolation of hadronic interactions to the lower energy threshold of this analysis should be small. On the other hand, the last energy bin at $\langle \lg(E/\text{eV}) \rangle = 19.62$ corresponds to a center-of-mass energy that is a factor of about 40 higher than the LHC energies and the model predictions have to be treated more carefully.

Comparing the energy evolution of $\langle X_{\max} \rangle$ for data and simulations in Fig. 13 it can be seen that the slope of the data is different than what would be expected for either a pure-proton or pure-iron composition. The change of $\langle X_{\max} \rangle$ with the logarithm of energy is usually referred to as *elongation rate* [17–19],

$$D_{10} = \frac{d\langle X_{\max} \rangle}{d \lg(E/\text{eV})}. \quad (9)$$

Within the superposition model, where it is assumed that a primary nucleus of mass A and energy E can be to a good approximation treated as a superposition of A nucleons of energy $E' = E/A$, the elongation rate is expected to be the same for any type of primary. Any deviation of an observed elongation rate from this expectation \hat{D}_{10} can be attributed to a change of the primary composition,

$$D_{10} = \hat{D}_{10} \left(1 - \frac{d\langle \ln A \rangle}{d \ln(E/\text{eV})} \right). \quad (10)$$

A single linear fit of $\langle X_{\max} \rangle$ as a function of $\lg(E)$ does not describe our data well ($\chi^2/\text{ndf} = 138.4/16$). Allowing

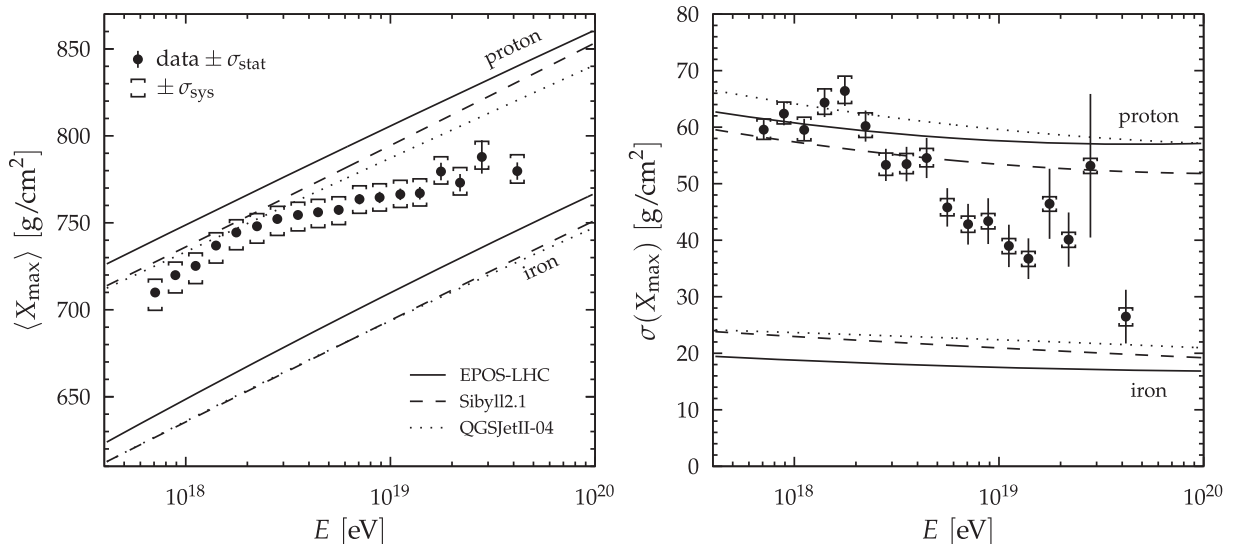


FIG. 13. Energy evolution of the first two central moments of the X_{\max} distribution compared to air-shower simulations for proton and iron primaries [80,81,95–98].

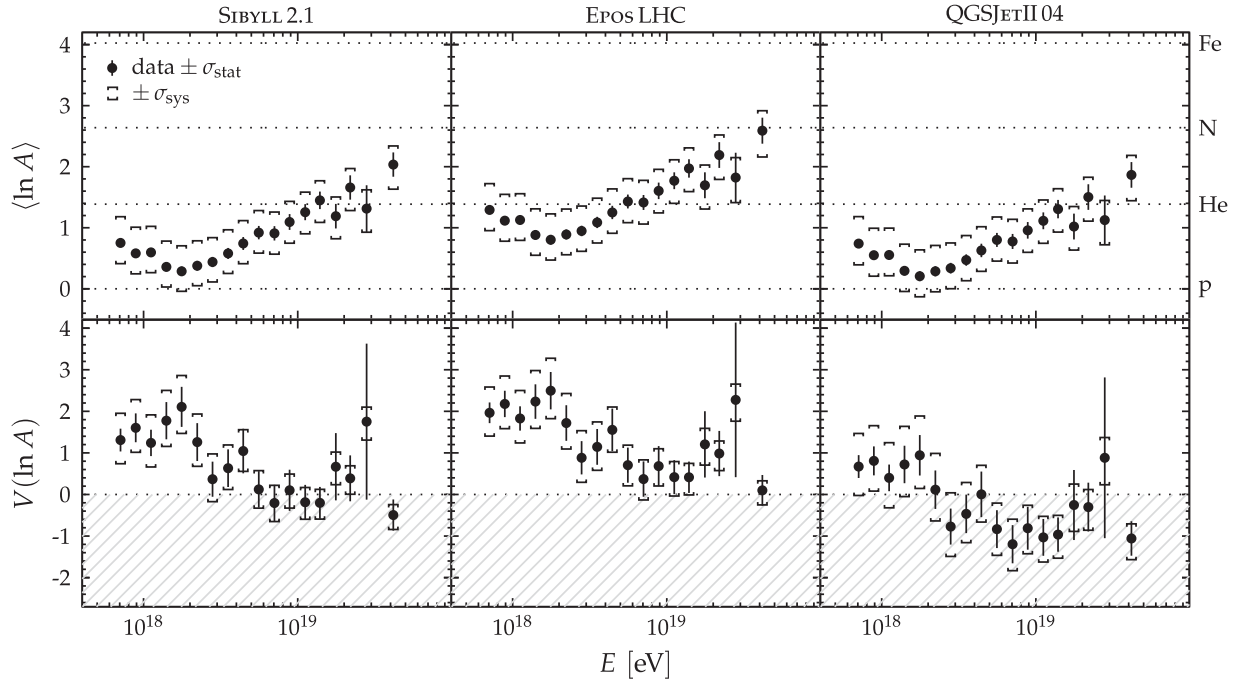


FIG. 14. Average of the logarithmic mass and its variance estimated from data using different interaction models. The nonphysical region of negative variance is indicated as the gray dashed region.

for a change in the elongation rate at a break point $\lg(E_0)$ yields a good χ^2/ndf of 8.2/14 with an elongation rate of

$$D_{10} = 86.4 \pm 5.0(\text{stat})^{+3.8}_{-3.2}(\text{sys}) \text{ g/cm}^2/\text{decade} \quad (11)$$

below $\lg(E_0/\text{eV}) = 18.27 \pm 0.04(\text{stat})^{+0.06}_{-0.07}(\text{sys})$ and

$$D_{10} = 26.4 \pm 2.5(\text{stat})^{+7.0}_{-1.9}(\text{sys}) \text{ g/cm}^2/\text{decade} \quad (12)$$

above this energy. The average shower maximum at E_0 is $746.8 \pm 2.1(\text{stat})^{+6.6}_{-10.0}(\text{sys}) \text{ g/cm}^2$. Here the systematic uncertainties on D_{10} have been obtained by varying the individual contributions of the systematic uncertainties on $\langle X_{\text{max}} \rangle$ separately.

The elongation rates predicted by air-shower simulations for a constant composition range from 54 to 64 $\text{g/cm}^2/\text{decade}$. Together with the results in Eqs. (11) and (12) we can therefore deduce that

$$\frac{d\langle \ln A \rangle}{d \lg(E/\text{eV})} = -1.07 \pm 0.20(\text{stat})^{+0.15}_{-0.13}(\text{sys})^{+0.26}_{-0.31}(\text{model}) \quad (13)$$

below E_0 and

$$\frac{d\langle \ln A \rangle}{d \lg(E/\text{eV})} = +1.23 \pm 0.10(\text{stat})^{+0.07}_{-0.27}(\text{sys})^{+0.09}_{-0.10}(\text{model}) \quad (14)$$

above this energy. This implies that there is an evolution of the average composition of cosmic rays towards lighter nuclei up to energies of $10^{18.27} \text{ eV}$. Above this energy, the trend reverses and the composition becomes heavier.

A similar behavior is visible for the width of the X_{max} distribution in the right panel of Fig. 13, where it can be seen that the $\sigma(X_{\text{max}})$ gets narrower towards high energies, as it would be expected for showers induced by heavy nuclei.

For a more quantitative study of the evolution of the composition, $\langle X_{\text{max}} \rangle$ and $\sigma(X_{\text{max}})$ are converted to the first two moments of the $\ln A$ distribution [cf. Eq. (3)] following the method described in [100,101]. The mean and variance of $\ln A$ are shown in Fig. 14 using air-shower simulations with three interaction models. As can be seen for all three cases, the composition is lightest at around $10^{18.3} \text{ eV}$ and the different features of hadronic interactions implemented in the three models give rise to differences in $\langle \ln A \rangle$ of about ± 0.3 . The interpretation with Epos-LHC leads to the heaviest average composition that is compatible with the $\ln A$ of nitrogen at the highest energies. The variance of $\ln A$ derived with Epos-LHC and Sibyll2.1 suggests that the flux of cosmic rays is

composed of different nuclei at low energies and that it is dominated by a single type of nucleus above $10^{18.7}$ eV where the variance, $V(\ln A)$, is close to zero. The interpretation with QGSJetII-04 leads to unphysical variances ($V(\ln A) < 0$) above $10^{18.4}$ eV and therefore this model is disfavored by our data, unless one allows for a systematic bias that is twice as large as the uncertainties estimated in Sec. VIII.

XI. CONCLUSIONS

In this paper, we presented the measurement of the distribution of the depth of shower maximum of ultrahigh energy cosmic-ray air showers. We described the data selection which allows for a nearly unbiased measurement of the distributions and discussed the residual effects of acceptance and resolution. The data set is the largest sample of X_{\max} measurements hitherto collected by a cosmic-ray detector. We provide computer-readable tables of the distributions and detector parameters that make it possible to interpret the measurements without the need of additional software to simulate the detector response. This approach will also facilitate the comparison with measurements of X_{\max} from other experiments [102]. Here we cannot provide such a comparison, since for these data neither the detector bias is controlled for using fiducial cuts, nor are the resolution and acceptance publicly available.

An interpretation in terms of mass composition of the moments of the X_{\max} distribution was given using air-shower simulations with contemporary hadronic interaction models. Assuming that the modeling of hadronic interactions gives a fair representation of the actual processes in air showers at ultrahigh energies, our data suggest that the flux of cosmic rays is composed of predominantly light nuclei at around $10^{18.3}$ eV and that the fraction of heavy nuclei is increasing up to energies of $10^{19.6}$ eV. Estimates of the fractions of groups of nuclei contributing to the cosmic-ray flux can be derived by interpreting the full distributions. Such an analysis can be found in an accompanying paper [94].

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APPENDIX A: CALCULATION OF X_{\max} MOMENTS

1. Weighted events

One possibility to correct for the acceptance as a function of X_{\max} is to assign to each event a weight $w_i = 1/\varepsilon_{\text{rel}}(X_{\max,i})$. The average shower maximum of events weighted by the inverse of the acceptance is given by

$$\langle X_{\max} \rangle = \left(\sum_i w_i X_{\max,i} \right) / \sum_i w_i. \quad (\text{A1})$$

The second noncentral moment is

$$\langle X_{\max}^2 \rangle = \left(\sum_i w_i (X_{\max,i})^2 \right) / \sum_i w_i \quad (\text{A2})$$

with which

$$\sigma(X_{\max})^2 = k(\langle X_{\max}^2 \rangle - \langle X_{\max} \rangle^2) \quad (\text{A3})$$

where

$$k = \left(\sum_i w_i \right)^2 / \left(\left(\sum_i w_i \right)^2 - \sum_i w_i^2 \right) \quad (\text{A4})$$

giving us the usual factor of $k = N/(N-1)$ when all weights are equal to one.

2. Λ_η method

When the shower maxima of the events in the tails of the X_{\max} distribution follow an exponential distribution,

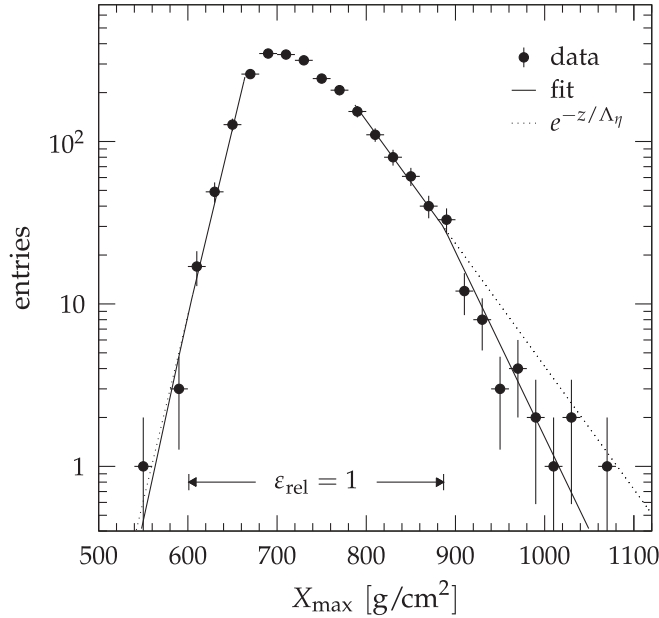


FIG. 15. Fit to the tails of the X_{\max} distribution [$18.1 < \lg(E/\text{eV}) < 18.2$]. The region of constant acceptance $\varepsilon_{\text{rel}} = 1$ is indicated by arrows.

damped by an exponential acceptance above a certain depth [cf. Eq. (7)], then the resulting distribution of the upper tail is given by

$$f(z) = ke^{-\frac{z}{\Lambda_\eta}} \begin{cases} 1 & ; z < z_0, \\ e^{-\frac{z-z_0}{\lambda}} & ; \text{otherwise,} \end{cases} \quad (\text{A5})$$

and a similar formula describes the lower tail, where z denotes the distance to the start point of the fit and z_0 is the distance above which the acceptance decreases exponentially with decay constant λ . The normalization is given by

$$k = \Lambda_\eta \left(1 + e^{-\frac{z_0}{\Lambda_\eta}} \left[\frac{\lambda}{\lambda + \Lambda_\eta} - 1 \right] \right). \quad (\text{A6})$$

The fraction of events in the tail is denoted by η . Following [27] we use $\eta = 0.20$ for the tail at large X_{\max} and the leading edge of the X_{\max} distribution is fitted using $\eta = 0.15$.

The unbinned likelihood for N events in the tail is

$$-\log \mathcal{L} \propto N \log k(\Lambda_\eta) + \frac{1}{\Lambda_\eta} \sum_{i=1}^N z_i, \quad (\text{A7})$$

where terms independent of Λ_η have been omitted.

An illustration of a fit of the upper and lower tail of the X_{\max} distribution is shown in Fig. 15. The fitted damped exponential is shown as the solid line and the range of constant acceptance is indicated by arrows. For the purpose of calculating the moments, the data distribution is replaced by the exponential functions (shown as dashed lines) outside of the $\varepsilon_{\text{rel}} = 1$ range.

APPENDIX B: DATA TABLES

TABLE II. Parameters of $\varepsilon_{\text{rel}}(X_{\max})$ [Eq. (7)] in g/cm^2 .

$\lg E$ range	x_1	λ_1	x_2	λ_2
[17.8,17.9)	586 ± 6	109 ± 17	881 ± 8	95 ± 7
[17.9,18.0)	592 ± 9	133 ± 17	883 ± 8	101 ± 7
[18.0,18.1)	597 ± 11	158 ± 19	885 ± 8	107 ± 7
[18.1,18.2)	601 ± 14	182 ± 21	887 ± 8	113 ± 7
[18.2,18.3)	604 ± 17	206 ± 24	888 ± 8	119 ± 7
[18.3,18.4)	605 ± 20	230 ± 28	890 ± 8	125 ± 7
[18.4,18.5)	605 ± 23	253 ± 32	892 ± 8	131 ± 7
[18.5,18.6)	604 ± 27	276 ± 38	894 ± 9	137 ± 8
[18.6,18.7)	602 ± 30	299 ± 44	896 ± 9	143 ± 8
[18.7,18.8)	599 ± 33	321 ± 51	898 ± 9	150 ± 8
[18.8,18.9)	594 ± 36	344 ± 59	899 ± 9	156 ± 8
[18.9,19.0)	588 ± 39	365 ± 67	901 ± 9	162 ± 8
[19.0,19.1)	581 ± 43	386 ± 77	903 ± 9	168 ± 8
[19.1,19.2)	573 ± 46	407 ± 86	905 ± 9	174 ± 8
[19.2,19.3)	563 ± 49	428 ± 98	907 ± 9	180 ± 8
[19.3,19.4)	553 ± 52	447 ± 109	908 ± 9	186 ± 8
[19.4,19.5)	540 ± 56	468 ± 122	910 ± 9	192 ± 8
[19.5, ∞)	517 ± 62	502 ± 146	913 ± 10	203 ± 9

TABLE III. Parameters of the X_{\max} resolution [Eq. (8)]. σ_1 and σ_2 are in g/cm^2 . The uncertainties are systematic and fully correlated between σ_1 and σ_2 .

$\lg E$ range	σ_1	σ_2	f
[17.8,17.9)	17.5 ± 0.7	33.7 ± 1.4	0.62
[17.9,18.0)	16.7 ± 0.7	32.9 ± 1.4	0.63
[18.0,18.1)	15.9 ± 0.7	31.9 ± 1.4	0.63
[18.1,18.2)	15.1 ± 0.7	31.0 ± 1.4	0.64
[18.2,18.3)	14.4 ± 0.7	30.0 ± 1.4	0.65
[18.3,18.4)	13.8 ± 0.7	29.1 ± 1.5	0.66
[18.4,18.5)	13.3 ± 0.7	28.1 ± 1.6	0.67
[18.5,18.6)	12.8 ± 0.8	27.1 ± 1.6	0.68
[18.6,18.7)	12.3 ± 0.8	26.3 ± 1.7	0.69
[18.7,18.8)	12.0 ± 0.8	25.4 ± 1.8	0.70
[18.8,18.9)	11.7 ± 0.9	24.7 ± 1.9	0.70
[18.9,19.0)	11.5 ± 0.9	24.1 ± 1.9	0.71
[19.0,19.1)	11.3 ± 0.9	23.6 ± 1.9	0.72
[19.1,19.2)	11.2 ± 0.9	23.3 ± 2.0	0.73
[19.2,19.3)	11.1 ± 0.9	23.1 ± 2.0	0.74
[19.3,19.4)	11.1 ± 1.0	23.1 ± 2.0	0.75
[19.4,19.5)	11.1 ± 1.0	23.2 ± 2.0	0.76
[19.5, ∞)	11.2 ± 1.0	23.7 ± 2.1	0.77

TABLE IV. First two moments of the X_{\max} distributions. Energies are in [eV] and $\langle X_{\max} \rangle$ and $\sigma(X_{\max})$ are given in [g/cm^2] followed by their statistical and systematic uncertainties. The number of selected events in each energy bin is given in the third column.

$\lg E$ range	$\langle \lg E \rangle$	N	$\langle X_{\max} \rangle$	$\sigma(X_{\max})$
[17.8,17.9)	17.85	3768	$709.9 \pm 1.2^{+7.6}_{-10.2}$	$59.6 \pm 1.7^{+1.9}_{-1.7}$
[17.9,18.0)	17.95	3383	$719.9 \pm 1.4^{+7.5}_{-10.2}$	$62.4 \pm 2.1^{+2.1}_{-1.8}$
[18.0,18.1)	18.05	2818	$725.2 \pm 1.5^{+7.4}_{-10.2}$	$59.5 \pm 2.0^{+2.2}_{-1.9}$
[18.1,18.2)	18.15	2425	$736.9 \pm 1.8^{+7.3}_{-10.1}$	$64.3 \pm 2.6^{+2.4}_{-2.1}$
[18.2,18.3)	18.25	1952	$744.5 \pm 2.0^{+7.3}_{-9.9}$	$66.4 \pm 2.6^{+2.6}_{-2.2}$
[18.3,18.4)	18.35	1439	$748.0 \pm 2.0^{+7.3}_{-9.7}$	$60.2 \pm 2.8^{+2.3}_{-2.0}$
[18.4,18.5)	18.45	1139	$752.2 \pm 2.1^{+7.3}_{-9.4}$	$53.3 \pm 2.9^{+2.1}_{-1.8}$
[18.5,18.6)	18.55	814	$754.5 \pm 2.2^{+7.3}_{-9.1}$	$53.5 \pm 3.0^{+1.9}_{-1.7}$
[18.6,18.7)	18.65	575	$756.1 \pm 2.7^{+7.4}_{-8.8}$	$54.5 \pm 3.5^{+1.7}_{-1.6}$
[18.7,18.8)	18.75	413	$757.4 \pm 2.8^{+7.5}_{-8.5}$	$45.8 \pm 3.4^{+1.5}_{-1.5}$
[18.8,18.9)	18.85	297	$763.6 \pm 2.9^{+7.7}_{-8.1}$	$42.8 \pm 3.6^{+1.4}_{-1.4}$
[18.9,19.0)	18.95	230	$764.6 \pm 3.2^{+7.8}_{-7.8}$	$43.4 \pm 4.1^{+1.3}_{-1.4}$
[19.0,19.1)	19.05	165	$766.4 \pm 3.3^{+8.0}_{-7.6}$	$39.0 \pm 3.8^{+1.3}_{-1.4}$
[19.1,19.2)	19.14	114	$767.0 \pm 3.6^{+8.2}_{-7.4}$	$36.7 \pm 3.6^{+1.3}_{-1.4}$
[19.2,19.3)	19.25	87	$779.5 \pm 5.1^{+8.5}_{-7.2}$	$46.4 \pm 6.2^{+1.2}_{-1.3}$
[19.3,19.4)	19.34	63	$773.1 \pm 5.0^{+8.7}_{-7.1}$	$40.1 \pm 4.8^{+1.3}_{-1.4}$
[19.4,19.5)	19.45	40	$787.9 \pm 9.6^{+8.9}_{-7.0}$	$53.2 \pm 12.7^{+1.3}_{-1.4}$
[19.5, ∞)	19.62	37	$779.8 \pm 5.0^{+9.4}_{-6.9}$	$26.5 \pm 4.8^{+1.5}_{-1.6}$

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