

Study of the planetary boundary layer by microwave radiometer, elastic lidar and Doppler lidar estimations in Southern Iberian Peninsula

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Abstract

The Planetary Boundary Layer (*PBL*) is a relevant part of the atmosphere with a variable extension that clearly plays an important role in fields like air quality or weather forecasting. Passive and active remote sensing systems have been widely applied to analyze *PBL* characteristics. The combination of different remote sensing techniques allows obtaining a complete picture on the *PBL* dynamic. In this study, we analyze the *PBL* using microwave radiometer, elastic lidar and Doppler lidar data. We use co-located data simultaneously gathered in the framework of SLOPE-I (Sierra Nevada Lidar aerOsol Profiling Experiment) campaign at Granada (Spain) during a 90- day period in summer 2016. Firstly, the *PBL* height (*PBLH*) obtained from microwave radiometer data is validated against *PBLH* provided by analyzing co-located radiosondes, showing a good agreement. In a second stage, active remote sensing systems are used for deriving the *PBLH*. Thus, an extended Kalman filter method is applied to data obtained by the elastic lidar while the vertical wind speed variance method is applied to the Doppler lidar. *PBLH*'s derived by these approaches are compared to *PBLH* retrieved by the microwave radiometer. The results show a good agreement among these retrievals based on active remote sensing in most of the cases, although some discrepancies appear in instances of intense *PBL* changes (either growth and/or decrease).

1 Introduction

The Planetary Boundary Layer (*PBL*) is defined as the “*part of the troposphere that is directly influenced by the presence of the Earth’s surface, and responds to surface forcings with a time scale of about an hour or less*” (Stull, 1988). This layer has high variability, being characterized by a daily cycle and presence of turbulent processes. In an ideal situation, some instants after the sunrise the ground surface temperature begins to increase, due to positive net radiative flux. Then, the air masses situated close to the ground get warmer and a convective process starts due to the buoyancy of these air masses that transport heat to the upper atmospheric layers. According to Stull et al., 1988 this process originates an unstable layer

39 denominated Convective Boundary Layer (*CBL*) or Mixing Layer (*ML*). Close to sunset, the reduction of
40 incidence of solar radiation causes gradual suppression of the convective processes, resulting in a weak and
41 sporadic turbulence. Then, the *CBL* becomes two different layers: an stably stratified shallow boundary
42 layer called Stable Boundary Layer (*SBL*), and the Residual Layer (*RL*), which still remains with the
43 features from previous day's *CBL* and above the *SBL*. This cyclical process will start again with the next
44 sunrise.

45 The *PBL* Height (*PBLH*) is an important parameter for a wide set of studies, which include pollutant
46 dispersion, weather forecasting, meteorological modeling and air quality (Li et al., 2017). Although the
47 *PBLH* cannot be measured directly, some atmospheric variables (e.g., potential temperature (θ), vertical
48 wind speed (w), relative humidity (*RH*) and aerosol distribution) have characteristic profiles due to
49 turbulent vertical processes that enable its detection (Stull, 1988). In addition, surface variables also can be
50 used as proxy for *PBLH* detection, e.g. sensible heat flux (Haeffelin, et al., 2012). The use of radiosounding
51 is by practical and historical issues the most widespread method in *PBLH* detection along years (Seidel et
52 al., 2010). However, the high variability of *PBL* during its daily cycle requires systems endowed with high
53 temporal resolution for continuous monitoring, which is not covered when launching radiosondes. In this
54 scenario, remote sensing systems had risen as an important tool in *PBL* studies, providing detailed and
55 long-term observational *PBLH* information (e.g. He et al., 2006; Granados-Muñoz et al., 2012; Di Giuseppe
56 et al., 2012; Haman et al., 2012; Pal et al., 2013; Coen et al., 2014; Korhonen et. al, 2014; Pal et al., 2015).

57 In the last two decades, elastic lidar (*EL*) systems have been widely applied in *PBL* studies (Flamant et al.,
58 1997; Menut et al., 1999; Davis et al., 2000; Brooks et al., 2003; Morille et al., 2007; Münkel, et al., 2007;
59 Baars et al., 2008; Pal et al., 2010; De Tomasi et al., 2011; Haeffelin et al., 2012; Wang et al., 2012;
60 Granados-Muñoz et al., 2012; Lange et al., 2014; Fedele et al., 2015; Banks et al., 2016; Bravo-Aranda et
61 al., 2017; Liu et al., 2018, Zhu et al., 2018). The detection of the *PBLH* using *EL* ($PBLH_{elastic}$) is based on
62 the definition provided by Deardorff et al. (1980) for this variable: “the altitude where there are equals
63 areas of clear air below and particulates above”, e.g. considering an ideal lidar return the *PBLH* is at the
64 midpoint where an inflexion occurs and the areas below and above the lidar return curve are equal (Kovalev
65 and Eichinger, 2004). Thus, when *PBL* is fully developed the height of *CBL* ($PBLH_{elastic}^{CBL}$) is detected,
66 otherwise the *RL* Height ($PBLH_{elastic}^{RL}$) is observed instead. However, it is not easy to find this midpoint by
67 the use of real *EL* signals due to either low signal-to-noise ratio or complex vertical distribution of the
68 atmospheric aerosols such as the presence of aerosol multilayers or clouds (Kovalev and Eichinger, 2004).
69 To solve this issue, mathematical methods are applied to the *EL* signal to reduce ambiguities in analyzed
70 signals. The traditional algorithms applied in $PBLH_{elastic}$ detection are the Gradient Method (Menut, et al.
71 1999; Martucci et al., 2007; Baars et al., 2008; Li et al., 2017; Zhu et al., 2018), Variance or Centroid
72 Method (Hooper and Eloranta, 1986; Menut et al., 1999; Martucci et al., 2007), Threshold Method (Melfi
73 et al., 1985; Kovalev and Eichinger, 2004), Fit Method (Eresma et al., 2006; Li et al., 2017) and Wavelet
74 Covariance Transform (Davis et al., 2000; Granados-Muñoz et al., 2012; Lopes et al., 2014). However,
75 these methods can still overestimates $PBLH_{elastic}$ on the mentioned complex situations. Lange et al. (2014),
76 Bravo-Aranda et al. (2017) and Liu et al. (2018) proposed algorithms to overcome these situations, using a
77 method based on Extended Kalman Filter, information from depolarization lidar channels and combination

78 between aerosol color ratio and depolarization ratio, respectively, the drawback however is obvious as not
79 as lidar systems are polarization-sensitive. Another shortcoming of the detection of *SBL* technique is the
80 high range for full overlap of some systems, which for azimuth pointing systems can be considered altitude
81 dependent, what might prevent a correct detection of the *SBL* that is typically found at lower heights.

82 Doppler lidars (*DL*) have been also used for *PBL* studies (Avolio et al., 2017; Das et al., 2018), mainly in
83 *PBLH* detection ($PBLH_{Doppler}$), so that the most applied algorithms with these systems are based on either
84 *ML* definition or turbulence threshold. The methods that use *ML* definition are the same *EL* methods
85 mentioned above using the backscattered signal (Shukla et al, 2014), however the carrier-to-noise ratio
86 (*CNR*) profile also can be applied in some algorithms, e.g. variance method (Moreira et. al, 2015). In these
87 cases, similarly to *EL*, when *PBL* is fully developed the height of *CBL* ($PBLH_{Doppler}^{CBL}$) is detected, otherwise
88 the height *RL* ($PBLH_{Doppler}^{RL}$) is observed. The main methods based on turbulence threshold are the variance
89 of vertical wind speed (σ_w^2) (Barlow et al., 2011; Schwenn et al., 2014), low-level jets detection (Moreira
90 et al., 2015), turbulent energy dissipation rate (O'Connor et al., 2010) and spectrum of horizontal wind
91 component (Marques et al., 2017). In these cases during nighttime stable situations the top of the *SBL*,
92 $PBLH_{Doppler}^{SBL}$, is detected and under convective situations the *CBL*, $PBLH_{Doppler}^{CBL}$, is the one selected.

93 Based on characteristics of potential temperature profile ($\theta(z)$, where *z* is the altitude above the ground) in
94 *PBL*, some authors (Granados- Muñoz et al., 2012; Wang et al., 2012; Coen et al., 2014) proposed to detect
95 the *PBLH* from temperature profiles provided by Microwave Radiometer (*MWR*) data ($PBLH_{MWR}$). Cimini
96 et al. (2013) estimated $PBLH_{MWR}$ from brightness temperatures that are directly obtained from *MWR*. An
97 advantage of this kind of systems is that its operation is little affected by rain or cloud covers (Kim et al.,
98 2015). Such characteristics combined with the absence of incomplete overlap issues in the near range allows
99 estimating the $PBLH_{MWR}$ in continuous mode with high recovery rate, so that both unstable (convective)
100 and stable cases are observed, $PBLH_{MWR}^{CBL}$ and $PBLH_{MWR}^{SBL}$ respectively.

101 According to the previous paragraphs, different remote sensing methods provide complementary
102 information on the *PBL* structure, with the characterization of its different layers. In this work we check
103 the feasibility of applying *MWR*, *EL* and *DL* for the characterization of the *PBLH* structure in simple and
104 complex situations. Firstly the $PBLH_{MWR}$ is validated against the *PBLH* obtained from radiosonde data
105 ($PBLH_{Radiosonde}$). Then, three study cases and a statistical analysis extended to the experimental period of
106 SLOPE-I campaign are presented in order to show how *DL*, *EL* and *MWR* can offer a picture of the complex
107 *PBL* dynamics during the whole daily period, i.e., daytime and nighttime. Special care is paid to the
108 limitations of each instrument in the characterization of the *PBL*.

109 This paper is then organized as follows. The site and the experimental setup are described in section 2. The
110 applied methodologies are introduced in section 3. The analysis of case studies and the statistical
111 comparison are performed in section 4. Conclusions are given in section 5.

112 **2 Experimental site and Instrumentation**

113 **2.1 IISTA-CEAMA and SLOPE-I campaign**

114 The measurement campaign was carried out at the Andalusian Institute of Earth System Research (IISTA-
115 CEAMA). This station is located at the city of Granada, a medium sized non-industrialized city in the
116 Southeastern Spain (Granada, 37.16°N, 3.61°W, 680 m a.s.l.). Granada is surrounded by mountains and
117 dominated by Mediterranean-continental conditions, which are responsible for large seasonal temperature
118 differences, providing cool winters and hot summers. The most humid period goes from late autumn to
119 early spring. The rest of the year is characterized by rain scarcity. Granada is predominantly affected by
120 aerosol particles coming from Europe and mineral dust particles from the African continent and the heavy
121 traffic along all year (Lyamani et al., 2006a, b, 2010; Córdoba-Jabonero et al, 2011; Titos et al., 2012, 2014;
122 Navas-Guzmán et al., 2013; Valenzuela et al., 2014). Main local sources are road traffic, domestic-heating
123 and biomass burning (mostly in winter time) (Titos et al., 2017). Transported smoke principally from North
124 America, North Africa and the Iberian Peninsula can also affect the study area (Alados-Arboledas et al.,
125 2011; Navas-Guzmán et al., 2013; Preißler et al., 2013; Ortiz-Amezcuca et al., 2014, 2017).

126 The field campaign Sierra Nevada Lidar aerOsol Profiling Experiment I (SLOPE I) was held from May to
127 September 2016 in South-Eastern Spain in the framework of the European Research Infrastructure for the
128 observation of Aerosol, Clouds, and Trace gases (ACTRIS). This campaign aimed to perform a closure
129 study by comparing remote sensing system (located at IISTA-CEAMA) and in-situ measurements, which
130 were performed in different heights in the slope of Sierra Nevada at 20 km away from IISTA-CEAMA.

131 **2.2 Instrumentation**

132 The biaxial ground-based Elastic-Raman lidar system MULHACEN (customized version of LR331D400,
133 Raymetrics S.A.), is deployed at IISTA-CEAMA and is part of the EARLINET (Pappalardo et al, 2014)
134 and SPALINET (Sicard et al, 2009) networks. MULHACEN operates with a pulsed Nd:YAG laser,
135 frequency doubled and tripled by Potassium Dideuterium Phosphate crystals. It emits at the wavelengths
136 355, 532 and 1064 nm with output energies per pulse of 60, 65 and 110 mJ, respectively. It has three elastic
137 channels, which are 355, 532 (parallel and perpendicular polarization) and 1064 nm, and three Raman-
138 shifted channels, which are 387 (from N₂), 408 (from H₂O) and 607 nm (from N₂). MULHACEN has a
139 nominal spatial resolution of 7.5 m. The overlap is complete at 90% between 520 and 820 m a.g.l. for all
140 the wavelengths and full overlap is reached around 1220 m a.g.l (Navas-Guzmán et al., 2011; Guerrero-
141 Rascado et al., 2010). Further technical details are given by Guerrero-Rascado et al. (2008, 2009).

142 The coherent *DL* (Halo Photonics) model Stream Line is operating in continuous and automatic mode since
143 May 2016. This system uses heterodyne detection to measure the Doppler shift of backscattered light. It
144 operates an eye-safe laser transmitter vertically pointing to zenith emitting at 1.5 μm with pulse energy and
145 repetition rate of 100 μJ and 15 KHz, respectively. The *DL* records the backscattered signal with 300 gates,

146 where the range gate length is 30 m and its first gate is located at 60 m. The data acquisition is performed
147 in Stare mode (only the vertical wind speed is measured) with a time resolution of 2 s

148 The ground-based passive microwave radiometer (RPG-HATPRO G2, Radiometer Physics GmbH) is part
149 of MWRnet (Rose et al., 2005; Caumont et al., 2016). This system operates in automatic and continuous
150 mode since November 2011. It measures the sky brightness temperature with a radiometric resolution
151 between 0.3 and 0.4 K root mean square error at 1s integration time. It operates with direct detection
152 receivers within two bands: 22-31 GHz (water vapor - K band) and 51-58 GHz (oxygen - V band), from
153 which ones is possible to derive relative humidity and temperature profiles, respectively. Both profiles are
154 obtained by inversion algorithms described in Rose et al. (2005). The vertical resolution varies between
155 10 and 200 m in the first 2Km. From 2 to 10 Km, such resolution varies between 200 and 1000 m (Navas-
156 Guzmán et al., 2014).

157
158 During this campaign, twenty-three radiosondes were also available, so that nineteen were launched during
159 the convective period (between 17:00 and 18:00 h -local time) and four were launched during stable period
160 (between 21:00 and 22:00 h – local time). The data were acquired with lightweight weather radiosondes
161 (DFM-06, GRAW Radiosondes), which provides profiles of temperature (resolution 0.01°C and accuracy
162 0.2°C), pressure (resolution 0.1 hPa, accuracy 0.5 hPa), humidity (resolution 1%, accuracy 2%) and wind
163 speed (resolution 0.1 m/s, accuracy 0.2 m/s). Data processing were accomplish by the Grawmet5 software
164 and a GS-E ground station from the same manufacturer (Granados-Muñoz et al., 2012).The surface
165 temperature was obtained from a meteorological station (HMP60, Vaisala), with a temporal resolution of 2
166 minutes and an accuracy and precision of 0.6° C and 0.01° C, respectively.

167 **3 Methodology**

168 **3.1 Temperature Method**

169 The algorithm combines two approaches, namely the Parcel Method (*PM*) (Holzworth, 1964) and
170 Temperature Gradient Method (*TGM*) (Coen, 2014), estimating the *PBLH* from *MWR* and Radiosonde
171 data ($PBLH_{MWR}$ and $PBLH_{Radiosonde}$, respectively) under convective ($PBLH^{CBL}$) and stable situations
172 ($PBLH^{SBL}$). The discrimination between stable and convective situations is based on the differences in
173 vertical profiles of potential temperature under stable and unstable conditions (see Stull, 1988). Thus we
174 propose a methodology where the surface potential temperature ($\theta(z_0)$, which is obtained from the
175 meteorological station co-located with the MWR) is compared with all points in $\theta(z)$ profile below 5 km
176 a.g.l, where z_0 and z represent, respectively, the surface and the range of heights above the ground. If all
177 points have values larger than $\theta(z_0)$, the situation is labelled as stable and TGM is used. Otherwise, the
178 situation is considered as unstable and the PM is applied. The choice of 5 km guarantees that we check the
179 full range that could cover the PBL at Granada.

180 The *PM* estimates the $PBLH^{CBL}$ at height (z) where $\theta(z)$ is equal to $\theta(z_0)$, because this is the altitude
 181 where an air parcel with an ambient temperature T can adiabatically rise from the ground by convection
 182 (Holzworth, 1964). The *TGM* provides the $PBLH^{SBL}$ from two definitions: surface-based temperature
 183 inversion (*SBTI*) (the first height where T increases as function of altitude) and top of stable boundary layer
 184 (*TSBL*) (the first height above *SBTI* where $d\theta/dz = 0$), therefore, firstly *SBTI* is detected from $T(z)$,
 185 then from this height is identified the *TSBL* in the $\theta(z)$. If *SBTI* or *TSBL* are not detected the $PBLH^{SBL}$ is
 186 labelled as “not identified”.

187 The potential temperature profile used in this algorithm is obtained from the temperature vertical profile,
 188 assuming that the surface pressure is 1000 mb and thus using the definition of potential temperature by
 189 applying the following formula:

$$190 \quad \theta(z) = T(z) + 0.0098 * z \quad (1) \text{ (Stull, 2011)}$$

191 where $T(z)$ [K] is the temperature profile, z is the height above the ground level, 0.0098 [K/m] is the dry
 192 adiabatic temperature gradient, and the atmosphere is considered as standard. For the computation of
 193 $PBLH_{MWR}$, the profiles of $\theta(z)$ were 30-min averaged in order to reduce the noise, providing 30-min $PBLH$
 194 estimations.

195 3.2 Variance threshold method

196 The variance of vertical wind speed (σ_w^2) is used to estimate the vertical size of convective cells growing
 197 due to homogeneous turbulent movement. Therefore, this variable is applied as an indicator of the mixing
 198 layer height, corresponding to $PBLH_{Doppler}^{SBL}$ in stable cases and $PBLH_{Doppler}^{CBL}$ in unstable cases.
 199 $PBLH_{Doppler}$ is adopted as the first height where σ_w^2 has a value lower than a predetermined threshold
 200 (th_{var}). Although different studies use distinct th_{var} values ranging from $th_{var} = 0.09 \text{ m}^2/\text{s}^2$ (Pearson et
 201 al., 2010) to $0.16 \text{ m}^2/\text{s}^2$ (Träumner et. al 2009, Schween et al. 2014), Schween et al., 2014 demonstrated
 202 that a variation of 25% in th_{var} value causes a deviation around 7% in $PBLH$ detection. We adopted the
 203 threshold value of $0.16 \text{ m}^2/\text{s}^2$ that is extendedly used, being obtained from the semi-theoretical profile of
 204 σ_w proposed by Lenschow et al. (1980). This value of th_{var} also was confirmed with Doppler lidar
 205 measurements and mathematical modelling by Large Eddy Simulations (*LES*) (Lenschow et al., 2012). In
 206 our case σ_w^2 is calculated using time intervals of 30 minutes.

207 3.3 Extended Kalman Filter (*EKF*) method

208 The Extended Kalman Filter (*EKF*) method (Lange et al., 2014; Banks et al. 2016) estimates the
 209 $PBLH_{elastic}$ based on an adaptive approach by extended Kalman Filter, which generates a simplified erf-
 210 like curve (Gauss error function (Abramowitz and Stegun, 1965)) model h (fig. 1) from the *EL* range
 211 corrected signal (*RCS*) and four time-adaptive coefficients as follows:

$$212 \quad h(R; R_{bl}, d, A, c) = \frac{A}{2} \left\{ 1 - \operatorname{erf} \left[\frac{d}{\sqrt{2}} (R - R_{bl}) \right] \right\} + c \quad (2)$$

213 where R_{bl} is an initial guess to $PBLH_{elastic}$, d is a scaling factor to entrainment zone thickness, A is the
 214 amplitude of the erf transition, and c is the average value of molecular signal (Banks et al. 2016). The
 215 successful use of this method strongly depends on the correct initialization of the *EKF* state vector that
 216 requires a priori statistical covariance information. This is obtained from the state vector noise and a priori
 217 error covariance matrices. Further details are given by Lange et al., 2014. In this work the *RCS* profiles of
 218 wavelength 532 nm are utilized. Such profiles were averaged in packages of 30 minutes in order to reduce
 219 the noise and provide *PBLH* estimation with this same time resolution

220 3.4 Statistical Parameters

221 The statistical comparison performed in section 4 is based on following parameters:

- 222 • Pearson coefficient of correlation (R): It indicates the level (and direction) of correlation
 223 performed between two group of data:

$$224 \quad R = \frac{\sum_{i=1}^n (PBLH_{x_i} - \overline{PBLH}_x)(PBLH_{Reference_i} - \overline{PBLH}_{Reference})}{\sqrt{\sum_{i=1}^n (PBLH_{x_i} - \overline{PBLH}_x)^2} \sqrt{\sum_{i=1}^n (PBLH_{Reference_i} - \overline{PBLH}_{Reference})^2}} \quad (3)$$

226 The absolute values of R can varies from 0 to 1, the closer the absolute values of R to 1, the larger
 227 correlation between the analyzed variables.
 228

- 230 • Index of agreement (D) (Willmont, 1981): D , often applied in comparison of models, presents the
 231 level of agreement between a given set of values ($PBLH_{x_i}$) and the reference values
 232 ($PBLH_{Reference_i}$):

$$233 \quad D = 1 - \frac{\sum_{i=1}^n (PBLH_{Reference_i} - PBLH_{x_i})^2}{\sum_{i=1}^n (|PBLH_{x_i} - \overline{PBLH}_{Reference}| - |PBLH_{Reference_i} - \overline{PBLH}_{Reference}|)^2} \quad (4)$$

234 D ranges from 0 to 1, higher values of D indicating better agreement between $PBLH_{Reference}$ and
 235 the $PBLH_x$.

- 236 • Root Mean Square Error (*RMSE*): Such variable demonstrates how concentrated the data
 237 ($PBLH_x$) are around the line of the best fit obtained from reference data ($PBLH_{Reference}$):

$$238 \quad RMSE = \sqrt{\frac{\sum_{i=1}^n (PBLH_{Reference_i} - PBLH_{x_i})^2}{n}} \quad (5)$$

- 239 • Percentage change ($\Delta PBLH_{x-Reference}$): This variable represents the relative percentage change
 240 between $PBLH_x$ and the $PBLH_{Reference}$:

$$241 \quad \Delta PBLH_{x-Reference} = \frac{PBLH_x - PBLH_{Reference}}{PBLH_{Reference}} \quad (6)$$

242 In all equations demonstrated above $PBLH_x$ and \overline{PBLH}_x represent the $PBLH$ value and its average value
243 respectively, where the subscribed index x indicates the instrument applied in $PBLH$ detection (MWR ,
244 DL [*Doppler*] or EL [*Elastic*]). In the same way $PBLH_{Reference}$ and $\overline{PBLH}_{Reference}$ represent the $PBLH$
245 value used as reference and its average value, respectively, so that the subscribed index $Reference$ indicate
246 the instrument used as reference in $PBLH$ detection (MWR or Radiosonde as will be described in section
247 4.1).

248 **4 Results**

249 **4.1 MWR and radiosonde PBL intercomparison**

250 This sub-section presents a statistical comparison of $PBLH$ retrieved from MWR data ($PBLH_{MWR}$) and the
251 estimations obtained applying similar methodology (Section 3.1) to the radiosonde profiles
252 ($PBLH_{Radiosonde}$). $PBLH_{MWR}$ and $PBLH_{Radiosonde}$ present very similar results with high level of
253 correlations (R) and index of agreement (D) under convective and stable atmospheric conditions
254 ($R_{Convective} = 0.96$, $D_{Convective} = 0.89$, $R_{Stable} = 0.97$, $D_{Stable} = 0.98$). The percentage difference between
255 $PBLH_{MWR}$ and $PBLH_{Radiosonde}$ ($\Delta PBLH_{MWR-Radiosonde}$) in convective cases (-0.6%) is smaller than the
256 corresponding relative difference observed in stable cases (8.1%), when the MWR always overestimate the
257 $PBLH$ derived from the radiosonde. This overestimation probably occurs because of the limited and smaller
258 vertical resolution of MWR in comparison with radiosonde (in the first 350 m $\theta_{Radiosonde}(z)$ has around
259 12 levels, while $\theta_{MWR}(z)$ has 3 levels), what requires further interpolations during the process of $PBLH_{MWR}$
260 detection. The Root Mean Square Error ($RMSE$) values observed in both situations are small (190 and 50
261 m in convective and stable cases, respectively). The largest value of $RMSE$ occurs under convective
262 conditions because of the average value of $PBLH$ obtained in unstable conditions is around 68% higher
263 than the average values in stable conditions.

264 Based on these results, we can conclude that, although the vertical temperature profile derived from MWR
265 has lower vertical resolution than that derived from the radiosondes, the values of $PBLH_{MWR}$ obtained by
266 the methodology described in section 3.1 are equivalents to $PBLH_{Radiosonde}$, retrieved by an equivalent
267 algorithm applied over the radiosonde temperature profiles.

268 As mentioned before, the $PBLH$ detection based on radiosonde data is the most accepted methodology for
269 deriving the CBL and SBL . Therefore, due to good agreement between $PBLH_{MWR}$ and $PBLH_{Radiosonde}$,
270 and the high temporal resolution of MWR , $PBLH_{MWR}$ is adopted as standard procedure for deriving the
271 height for the CBL and the SBL . In this way a continuous $PBLH$ detection is performed thus providing an
272 insight on the PBL dynamics along the day.

273 4.2 Study cases

274 As aforementioned in Section 1, the complexity of the *PBL* characterization is linked to the complexity of
275 its structure that changes along the day. In this section, we present three case studies in increasing level of
276 complexity to analyze how *MWR*, *EL* and *DL* determine the *PBL* structure under different situations. The
277 three scenarios are: 1) well-defined *PBL* (the simplest case); 2) presence of clouds (complicated situation
278 mainly for lidar systems, e.g. Hennemuth and Lammert, 2006), and (iii) Saharan dust outbreak (very
279 complicated and typical situation over the city of Granada, e.g., Bravo-Aranda et al., 2017).

280 4.2.1 Well-defined PBL case

281 A well-defined *PBL* case was detected on 19th May 2016 with *MWR* and *DL* measuring continuously, and
282 MULHACEN operating from 08:20 until 18:00 UTC. Figure 2 shows the temporal evolution of the *EL RCS*
283 at 532 nm and the retrieved $PBLH_{MWR}$, $PBLH_{Doppler}$ and $PBLH_{elastic}$. The last one only can be observed
284 after 10:00 UTC, because the *CBL* was below the full-overlap height of MULHACEN. From 08:20 until
285 10:00 UTC the *RCS* temporal evolution suggest the presence of the *RL* over the *CBL*. Also there are some
286 aerosol layers over the *CBL* between 13:00 and 18:00 UTC with altitudes around 2.3 km a.g.l.

287 Figure 3 presents the temporal evolution of the relative differences in percentage $\Delta PBLH_{Doppler-MWR}$ (blue
288 bars) and $\Delta PBLH_{Elastic-MWR}$ (orange bars), evaluated in 30-min intervals. Due to the small height for full
289 overlap of the *DL*, it is feasible to perform the comparison between *DL* and *MWR* during all the convective
290 period (06:00–18:00 UTC). From the first hours until 15:00 UTC, $|\Delta PBLH_{Doppler-MWR}|$ varies between 4
291 and 8%. The largest values of $\Delta PBLH_{Doppler-MWR}$ (above 10%) are observed in the last hours when *PBL*
292 begins to decrease. This is caused by the different *PBLH* tracers used in each method. Unlike the moments
293 of intense convection where both algorithms detect the height of *CBL* ($PBLH_{MWR}^{CBL} \sim PBLH_{Doppler}^{CBL}$), when
294 *PBL* stability is changing the variance threshold method detects the *ML* height, while Temperature method
295 detects the *TSBL*. Resulting in the higher values of $\Delta PBLH_{Doppler-MWR}$.

296 When *CBL* grows or decrease rather fast (10:00-11:30 UTC and 16:00 – 18:00 UTC), high values of
297 $|\Delta PBLH_{Elastic-MWR}|$ are observed (between 8 and 15%). Although, in this period, *EKF* and Temperature
298 methods detect the height of *CBL*, the different tracers used are subject to distinct interferences. While the
299 temperature profile varies directly by thermodynamic phenomena, aerosols are affected by these
300 phenomena and also can be influenced by others like emission rate from the ground and/or inertia, resulting
301 in the differences observed in figure 3. When *CBL* is fully developed (between 12:00 and 15:30 UTC) its
302 height does not show great differences among different methods, thus, under these conditions, the different
303 tracers agree in the determination of the *PBLH*. Therefore the smaller values of $\Delta PBLH_{MWR-elastic}$ are
304 detected under fully developed convective columns (~1%). This high agreement between *PBLH* estimated
305 from different tracers when *CBL* is fully developed was also observed by Schwenn et al. (2014) during the
306 long-term comparisons between *PBLH* obtained from Doppler lidar and ceilometer data at
307 Forschungszentrum Jülich (Germany).

309 4.2.2 Cloudy case

310 The second study case corresponds to 16th May 2016, where measurements with *MWR* and *DL* were
 311 continually performed while MULHACEN was operated from 10:36 until 16:30 UTC. This situation is
 312 more complex than in the previous case, due to presence of clouds between 1.8 and 2.8 km a.g.l. (12:30 to
 313 16:30 UTC –) and lofted aerosol layers between 2.5 and 3.5 km a.g.l.. Figure 4 shows the *EL RCS* temporal
 314 evolution together with $PBLH_{elastic}$, $PBLH_{MWR}$, and $PBLH_{Doppler}$.

315 Figure 5 presents the percentage differences of $\Delta PBLH_{elastic-MWR}$ and $\Delta PBLH_{Doppler-MWR}$ for the whole
 316 period of measurements. The behavior of $\Delta PBLH_{Doppler-MWR}$ in this case is similar to that observed in the
 317 study case I, small and almost constant values when *CBL* does not varies too much and large values in the
 318 periods when there are intense and fast variation of *PBLH*. During the cloudy periods,
 319 $|\Delta PBLH_{Doppler-MWR}|$ values increase (around 15%), because the *DL* and Temperature methods to detect
 320 the *PBLH* under cloudy conditions establishes the *PBLH* at the cloud base (Schween et al., 2014) and at
 321 the cloud center, respectively.

322 In a similar way as $\Delta PBLH_{Doppler-MWR}$, $\Delta PBLH_{elastic-MWR}$ presents a pattern similar to that encountered
 323 in the study case I, with values close to 5% around noon, and values close to 10% at the moments of high
 324 convective activity. High values of $\Delta PBLH_{MWR-elastic}$ are observed during the cloudy period because,
 325 similarly at *DL* method, *PBLH* it is established at the cloud base.

326 4.2.3 Saharan dust case

327 This case illustrates the Saharan dust outbreak over Granada on 22th July 2017 detected by *MWR*, *DL* and
 328 *EL* (from 04:47 until 12:32 UTC). Figure 6 shows the *EL RCS* temporal evolution together with $PBLH_{MWR}$,
 329 $PBLH_{Doppler}$ and $PBLH_{elastic}$. At the start time of the *EL* measurement the dust layer is coupled with *RL*.
 330 In such cases *PBLH* detection is very complicated for methods that use the atmospheric aerosol as a tracer,
 331 and many of them often overestimate the *PBLH*. Bravo-Aranda et al. (2017) proposed the utilization of
 332 lidar depolarization measurements to distinguish between mineral dust and anthropogenic aerosol layers in
 333 order to estimate the height only of the last one and adopt it as *PBLH*.

334 $PBLH_{Doppler}$ detection is not affected by presence of dust layer, because it is based on the level of mixing.
 335 Although there is a mineral dust layer coupled with other anthropogenic aerosol layers, the level of mixing
 336 observed in the first meters of *PBL* exceeds the threshold selected, therefore $PBLH_{Doppler}^{CBL}$ is detected at
 337 this region. In contrast, the presence of mineral dust layer, due to absorption of infrared radiation, changes
 338 the potential temperature profile, so that $PBLH_{MWR}^{CBL}$ is registered in upper layers in comparison with
 339 $PBLH_{Doppler}^{CBL}$. These detections of distinct phenomena result in higher values of $\Delta PBLH_{Doppler-MWR}$ in
 340 comparison with the other study cases previously discussed (reaching 60%). However, the values of

341 $\Delta PBLH_{Doppler-MWR}$ reduce as the PBL becomes more homogeneous, reaching about 38% in the last hours
342 of measurement (Fig. 7).

343 During the first hours of this measurement, $PBLH_{elastic}$ probably would be affected by dust layer due to
344 impossibility of differentiating the coupled layers. At 11:00 UTC the dust layer is displaced (Fig. 6) and
345 does not affect the $PBLH_{elastic}$ detection. Although the fast PBL growth and the existence of different
346 influences acting on the distinct tracers result in high values of $\Delta PBLH_{MWR-elastic}$ in comparison with other
347 situations (reaching 32%). However, these values decrease as the growth rate reduces, reaching 11% in the
348 last hour of measurements. Banks et al. (2015) found similar results when they compared the $PBLH_{elastic}$
349 obtained from EKF with $PBLH$ estimated from radiosonde data by bulk Richardson number.

350 4.3 Statistical analysis

351 The statistical study of the comparison of the $PBLH$ retrieved by the three remote sensing methods used
352 during all SLOPE-I campaign is presented in this section. The comparison between $PBLH_{MWR}$ and
353 $PBLH_{Doppler}$ was performed over 24 hours of all days of campaign. This allows the evaluation of the DL
354 retrieval, $PBLH_{Doppler}$, both under stable and convective situations. Nevertheless, the comparison between
355 $PBLH_{elastic}$ and $PBLH_{MWR}$ is not extended for the whole day because, as a result of the relatively large full
356 overlap height of MULHACEN, in the morning and at night the $PBLH_{elastic}^{RL}$ is detected (Bravo-Aranda,
357 2017), while Temperature method detects the $PBLH_{MWR}^{CBL}$. Therefore, to ensure that both instruments detect
358 the same variable, EKF method was applied only when the reference $PBLH_{MWR}$ exceeded 700 meters a.g.l.,
359 therefore between 09:00 and 19:00 UTC

360 Figure 8 demonstrated the comparison among the average daily $PBLH$ values of MWR (\overline{PBLH}_{MWR}), DL
361 ($\overline{PBLH}_{Doppler}$) and EL ($\overline{PBLH}_{Elastic}$). Both profiles have similar behaviors with differences smaller than
362 300 m. $\overline{PBLH}_{Elastic}$ presents the lowers differences with relation to \overline{PBLH}_{MWR} . $\overline{PBLH}_{Doppler}$ is
363 overestimated when compared to the reference values along almost the whole profile, however the such
364 values do not exceed the standard deviation of \overline{PBLH}_{MWR} .

365 Figure 9 shows the daily pattern, of the statistics describing the comparison between $PBLH_{MWR}$ and
366 $PBLH_{Doppler}$, with a temporal resolution of 30 minutes. It is evident that the absolute average value of
367 $\Delta PBLH_{Doppler-MWR}$ does not exceed 20%. The higher values are observed between 21:00 and 22:00 UTC,
368 00:00 and 01:00 UTC, 08:30 and 10:30 UTC, 16:30 and 18:30 UTC. The last two intervals are characterized
369 by intense $PBLH$ changes, thus being justified in the terms argued in the discussion of the study cases. The
370 lowest differences are concentrated in central region of day and in some moments associated to the SBL
371 (around 3%). Most of the time $PBLH_{Doppler}$ overestimates the $PBLH_{MWR}$, however the higher values of
372 average $\Delta PBLH_{Doppler-MWR}$ also occur when $PBLH_{MWR}$ is underestimated by $PBLH_{Doppler}$. $RMSE$ bears
373 practically constant values during the stable periods (around 100 m). The highest values occur between
374 16:30 and 18:30 UTC (around 450 m). R values are larger than 0.70 between 04:30 and 16:30 UTC, and
375 the higher values (0.90) are in the central region of day, when PBL is fully-developed. After 16:30 UTC R
376 value begins to decrease, reaching their minimum values during the stable period. D values are larger than

377 0.85 during quite all the period, outside of the period between 22:30 and 00:00 UTC, where D is lower than
378 0.70. Similarly to R , the higher values of D (0.99) occur often when PBL is fully-developed.

379 From the combination of the statistics presented in figure 9 it is possible to affirm that $PBLH_{Doppler}$ has a
380 good agreement with $PBLH_{MWR}$ in 80% of the daily cycle, so that the lower results are observed between
381 20:00 and 00:00 UTC. This is due to the different $PBLH$ indicator adopted by each method, because while
382 the variance threshold method is based on analysis of turbulence level, Temperature method detects the
383 $TSBL$, so that these events do not occur always at same height, meanly when PBL has vertical displacements
384 (in this situation decreasing), as mentioned above.

385 Figure 10 shows the statistics describing the comparison between the daily patterns of $PBLH_{MWR}$ and
386 $PBLH_{elastic}$. During all SLOPE-I campaign the absolute average value of $(\Delta PBLH_{Elastic-MWR})$ does not
387 exceed 15%. The higher values are detected at 09:00 UTC, between 10:00 and 11:30 UTC, at 17:00 UTC
388 and between 18:30 and 19:00 UTC (around 13%), where frequently $PBLH$ has fast changes. For all the
389 period, the $RMSE$ has values lower than obtained in the comparison between the retrievals of $PBLH$ by
390 MWR and DL . This difference in the results of $RMSE$ probably occurs due to larger vertical resolution of
391 EL . Outside the period between 11:30 and 12:00 UTC and at 17:30 UTC, where R values are lower than
392 0.8, high correlations are observed, mainly in the beginning of measurement and in the central part of the
393 day. D presents a similar behavior with values lower than 0.85 between 11:30 and 12:00 UTC and at 17:30
394 UTC and higher values in the central of day, when PBL is fully-developed.

395 The joint analysis of these statistical variables reveals a good agreement between $PBLH_{MWR}$ and
396 $PBLH_{elastic}$ mainly in the central part of day, when PBL is fully developed and low average values of
397 $\Delta PBLH_{Elastic-MWR}$ together with high values of R and D are observed. The largest discrepancies are
398 observed in moments of intense increase and/or decrease of $PBLH$, due to great change in PBL affecting
399 in a different way the distinct $PBLH$ tracers used in each method, thus leading to discrepancies in the
400 retrieval of the $PBLH$.

401 5 Conclusions

402 This work presents a comparison between $PBLH$ obtained from three remote sensing systems, namely
403 MWR , EL and DL , which retrieve this variable using as a proxy the vertical profile of potential temperature,
404 aerosol and vertical wind speed, respectively. The data were acquired during SLOPE-I campaign in
405 Granada (Spain) from May to July in 2016.

406 Firstly the $PBLH_{MWR}$ is validated by $PBLH_{radiosonde}$ from the methodology describe in section 3.1. The
407 $PBLH$ provided by both instruments are equivalent in stable and convective situations, with high level of
408 correlations and index of agreement ($R_{Convective} = 0.96$, $D_{Convective} = 0.89$, $R_{Stable} = 0.97$, $D_{Stable} = 0.98$)
409 and low values of $\Delta PBLH_{MWR-Radiosonde}$ (-0.6 and 8.1% for convective and stable cases, respectively).
410 This agreement between the data allowed us to use the $PBLH_{MWR}$ as the reference method, for the rest of
411 the study.

412 Three study cases (well-defined *PBL*, *PBL* with presence of thick clouds and *PBL* with coupled dust layer)
413 are analyzed in detail in order to investigate the behavior of $PBLH_{Doppler}$, $PBLH_{elastic}$ and $PBLH_{MWR}$. In
414 situations where *PBL* is well defined and the growth rate is not so intense, all methods present small
415 percentage differences ($\Delta PBLH$ smaller than 5%). Similar results also were observed by Schween et. al
416 (2014) in its long-term comparison between *PBLH* estimated from *DL* and ceilometer, and by Coen et. al
417 (2014) in its comparison between *PBLH* obtained from *MWR*, *EL*, radiosonde and wind profiler data.
418 However, under scenarios where *PBL* grows rapidly, there are presence of clouds and/or dust layers, the
419 values of $\Delta PBLH$ increase (differences around 60% for *DL* and 35% for *EL*, with respect to the *MWR*
420 estimations). Such differences are originated by the distinct influence suffered by each tracer (inertia,
421 gravitation, etc.), as well as, *PBLH* definition (case with presence of clouds).

422 In addition, a statistical analysis was performed for all SLOPE-I campaign. The comparison between
423 $PBLH_{MWR}$ and $PBLH_{Doppler}$ is performed over the whole 24 h day period, while $PBLH_{elastic}$ and
424 $PBLH_{MWR}$ were compared between 09:00 UTC and 19:00 UTC, due to the shortcomings associated to the
425 rather large height for full overlap of the MULHACEN lidar system. The best agreement between
426 $PBLH_{Doppler}$ and $PBLH_{MWR}$ (low values of average $\Delta PBLH$ and higher values of *R* and *D*) are obtained
427 when *PBL* is fully developed. The worst correlations (low values of *R* and *D* and higher average values of
428 $\Delta PBLH$) occur between 21:30 and 00:00 UTC. In the same ways as $PBLH_{Doppler}$, $PBLH_{elastic}$ has the best
429 correlations with $PBLH_{MWR}$ in the central region of day and the worst results in moments of fast *PBLH*
430 growth and/or decreasing ($R < 0.8$ and $D < 0.85$). From these comparison we can conclude that when *PBL*
431 is full-developed both lidar systems have good results, although $RMSE_{Elastic} < RMSE_{Doppler}$ likely as a
432 result of the best vertical resolution of the MULHACEN lidar in comparison with the *DL*. During the
433 periods of intense *PBLH* increasing and/or reduction $PBLH_{Doppler}$ has correlations (*D* always larger than
434 0.85) better than $PBLH_{Elastic}$. In stable cases $PBLH_{Doppler}$ has more reliable values only from 00:30 UTC.

435 Therefore, although both lidar systems can estimate the *PBLH* with considerable level of agreement in
436 relation to the reference method (*MWR*), *EL* provides better results during the period when *PBLH* is above
437 its overlap limit, except situations of coupled dust layers are present. On the other hand, *DL*, due to its full
438 overlap at low level, can estimates the *SBL* during most of the night with high accuracy.

439 This study demonstrated the feasibility of both algorithms to estimate *PBLH* in simple and complex
440 situations, as well as the level of reliability of each one during the different phases of *PBL* daily cycle.
441 Considering that the different techniques demonstrated in this work are complementary, in the future we
442 will intend to use them synergistically in order to provide a detailed detection of the complex *PBL* structure
443 (*RL*, *SBL* and *CBL*).

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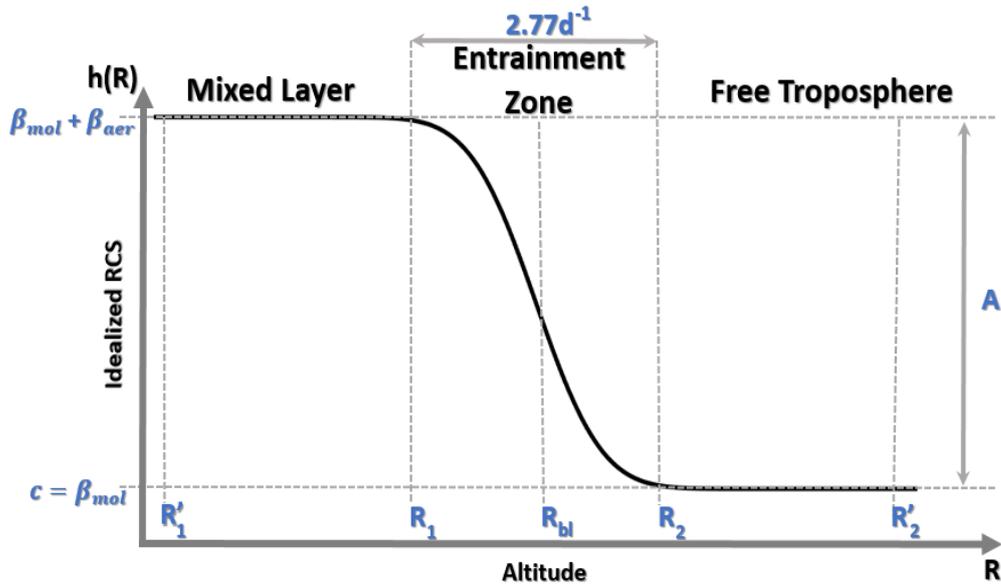


Figure 1– Idealized lidar profile. The pair R'_1 and R'_2 defines the length limit of the observation vector applied in the filter. R_1 and R_2 represent the limits of the erf-like PBL transition zone. R_{bl} is the PBLH guest, β_{mol} is the average value of molecular signal, β_{aer} is the signal obtained from aerosol backscattering, d is a scaling factor to entrainment zone thickness and A is the amplitude of the erf transition.

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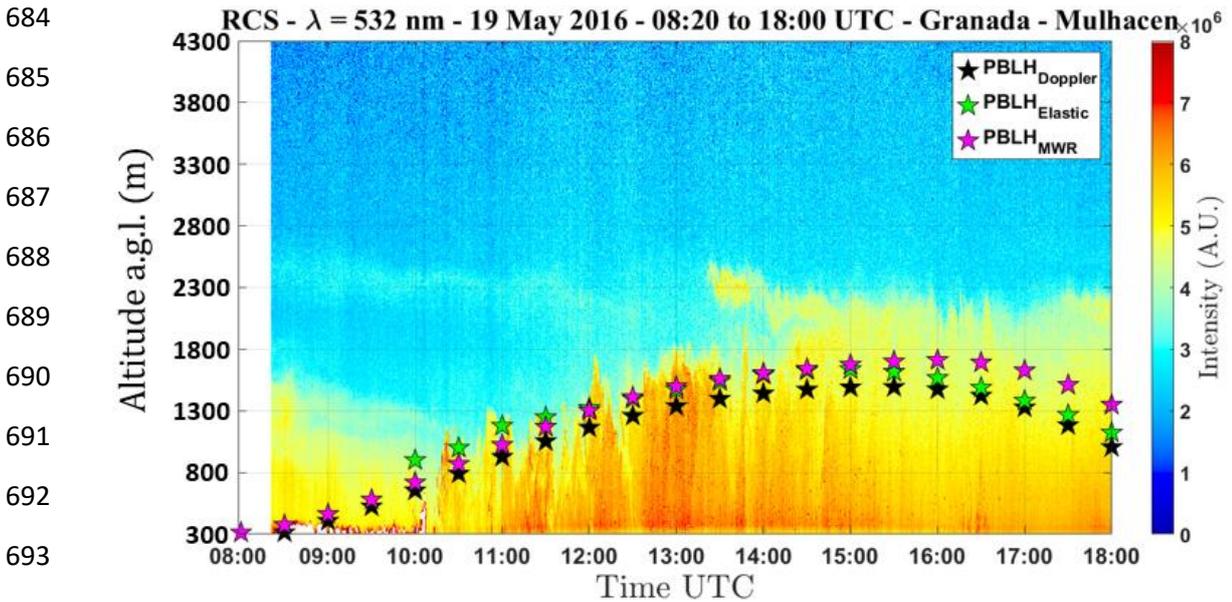


Figure 2 – Temporal evolution of RCS profile and PBLH provided by MWR (pink stars), EL (green stars) and DL (black stars).

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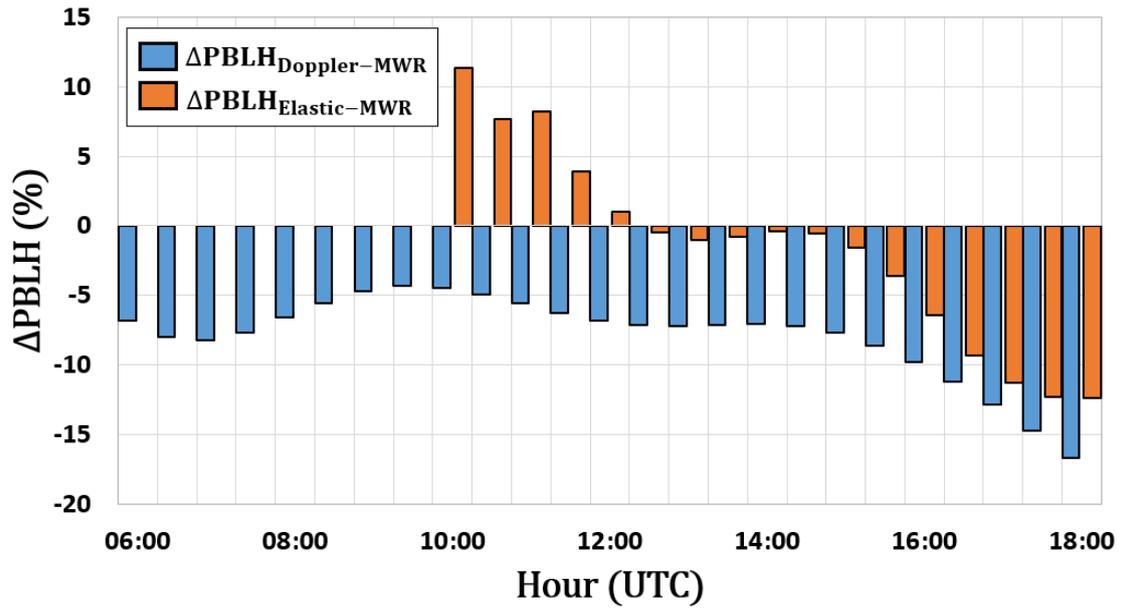


Figure 3 - Temporal evolution of $\Delta PBLH_{Doppler-MWR}$ (blue bars) and $\Delta PBLH_{Elastic-MWR}$ (orange bars).

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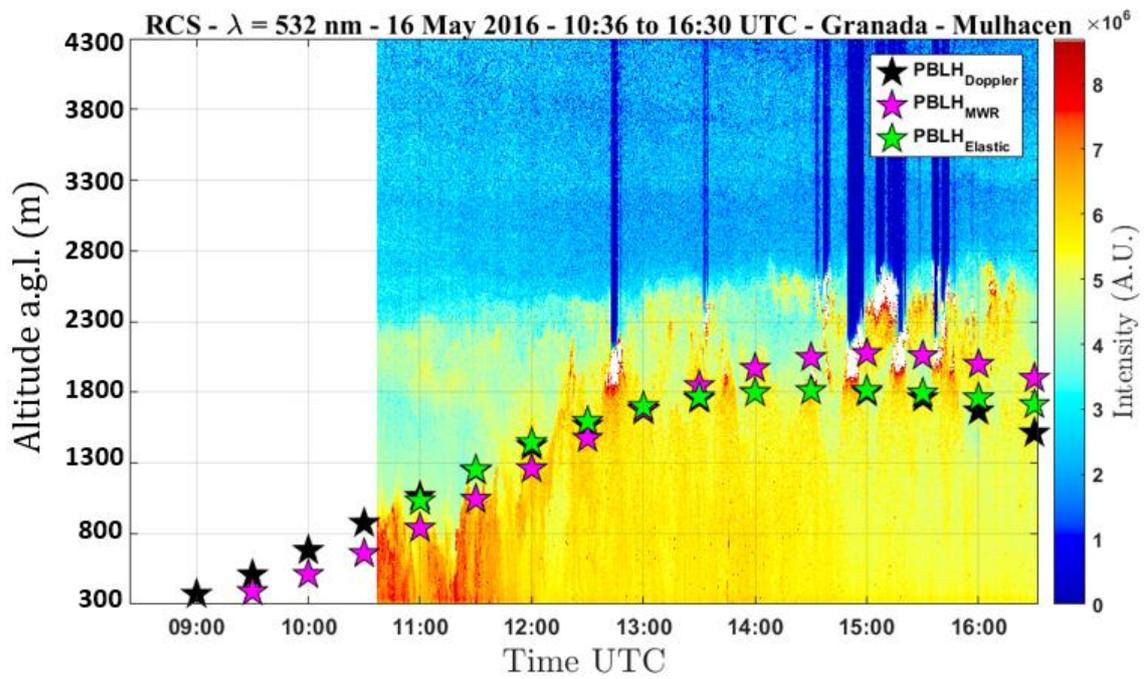


Figure 4 - Temporal evolution of RCS profile and PBLH provided by MWR (pink stars), EL (green stars) and DL (black stars).

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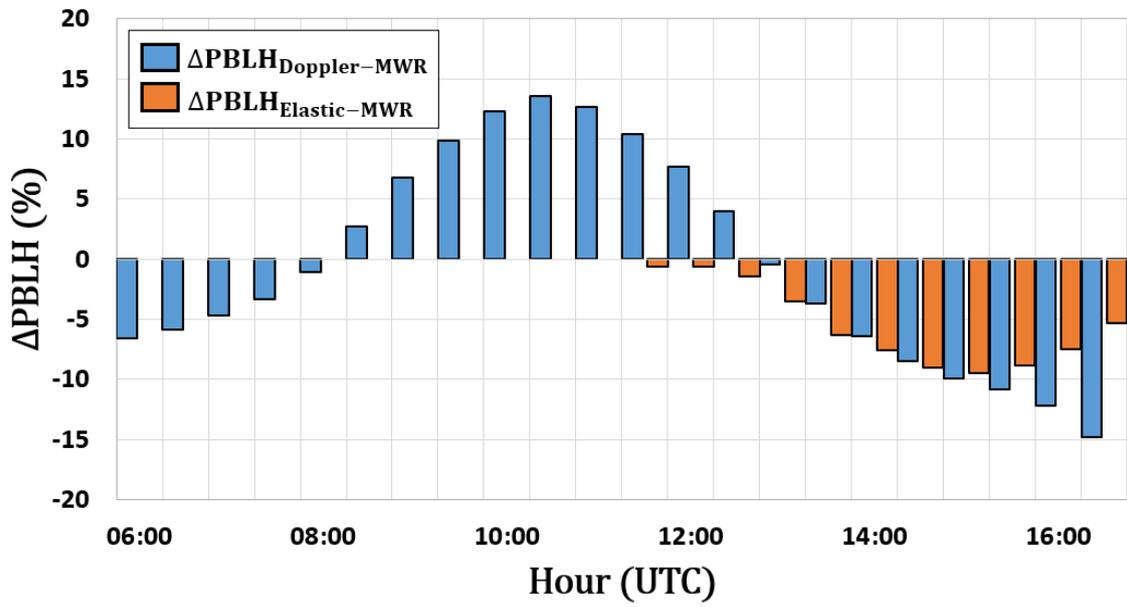


Figure 5 – Temporal evolution of $\Delta PBLH_{Doppler-MWR}$ (blue bars) and $\Delta PBLH_{Elastic-MWR}$ (orange bars).

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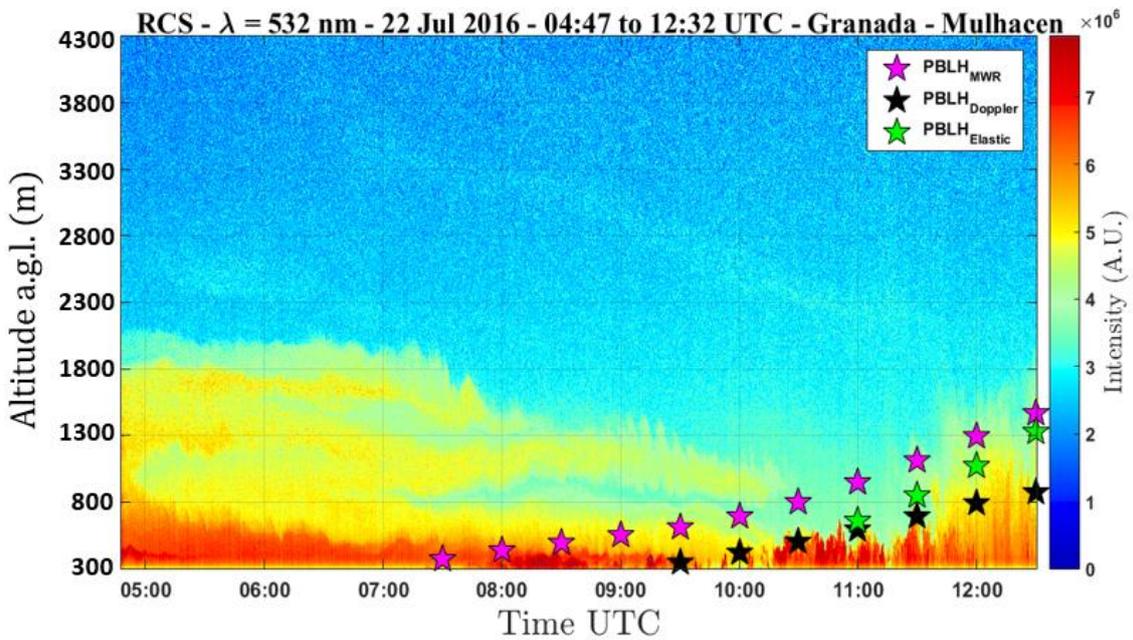


Figure 6 – Temporal evolution of RCS profile and $PBLH$ provided by MWR (pink stars), EL (green stars) and DL (black stars).

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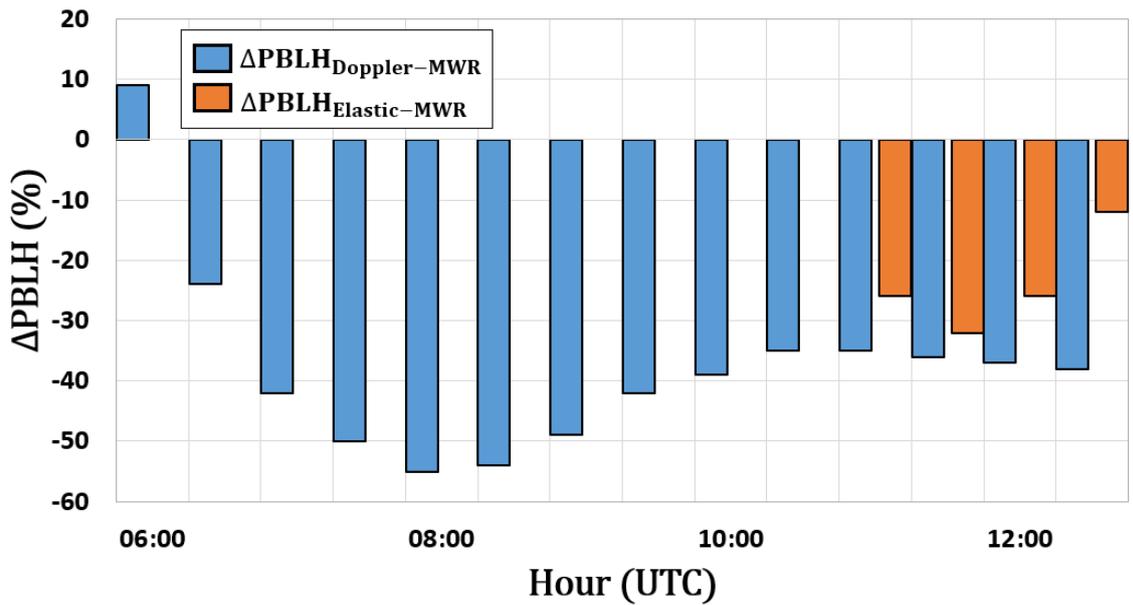


Figure 7 – Temporal evolution of $\Delta PBLH_{Doppler-MWR}$ (blue bars) and $\Delta PBLH_{Elastic-MWR}$ (orange bars).

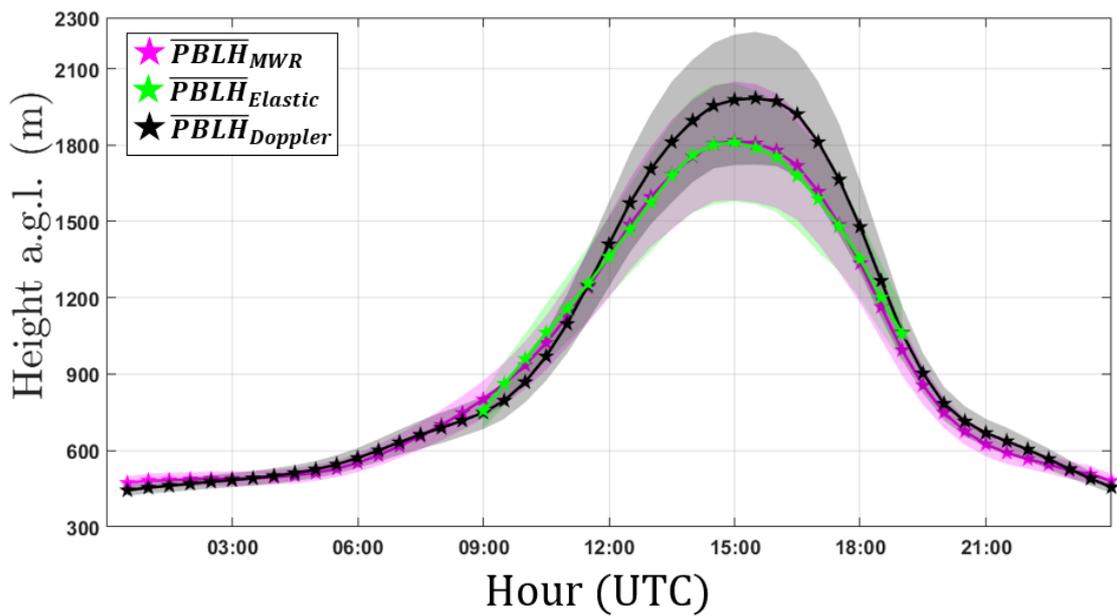
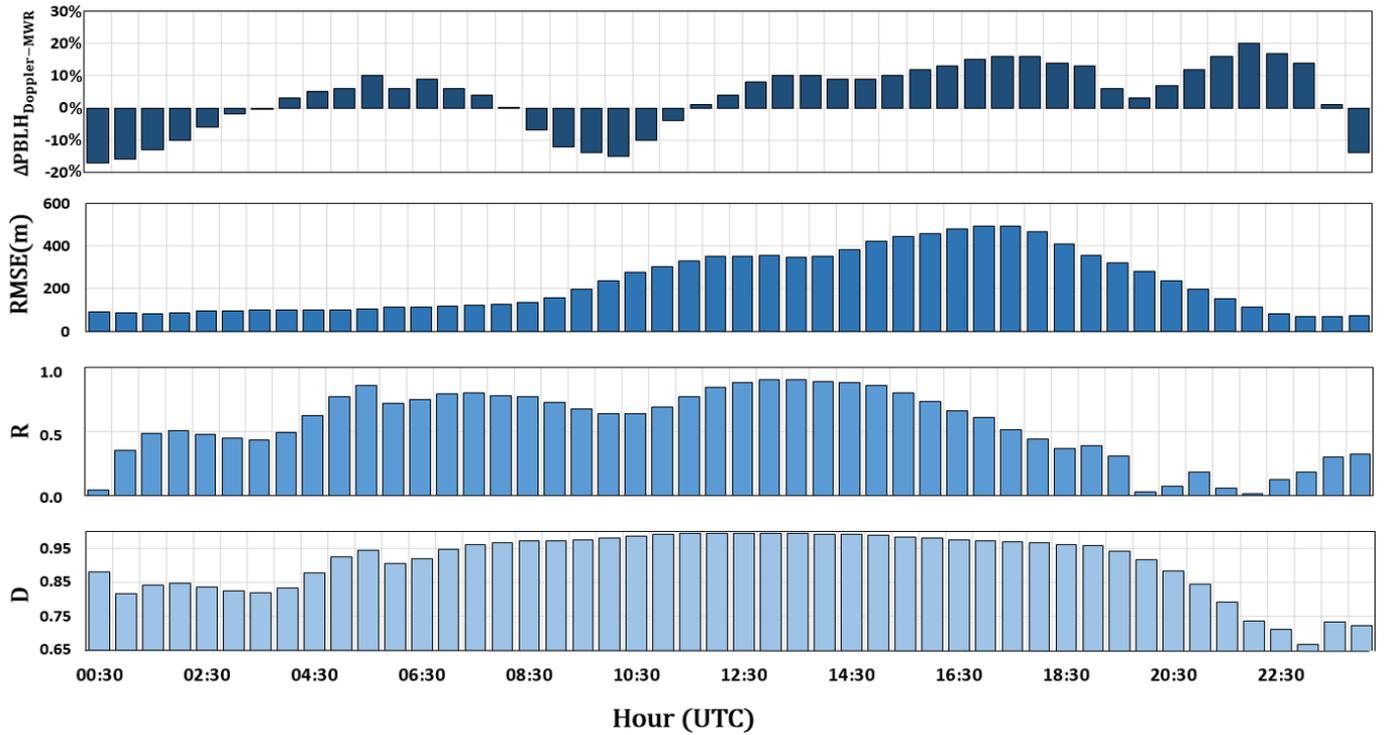


Figure 8 – Average values of $PBLH$ provided by MWR (pink stars), EL (green stars) and DL (black stars). The shadows with the colors of stars mentioned above represent the standard deviation of respective methods.

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Figure 9 – Statistical comparison between the daily patterns of $PBLH_{MWR}$ and $PBLH_{elastic}$ obtained during all SLOPE-I campaign. Each bin size is equivalent to 30 minutes. $\Delta PBLH_{Doppler-MWR}$, $RMSE$, R and D represents average percentage difference, root mean square error, correlation index and index of agreement, respectively.

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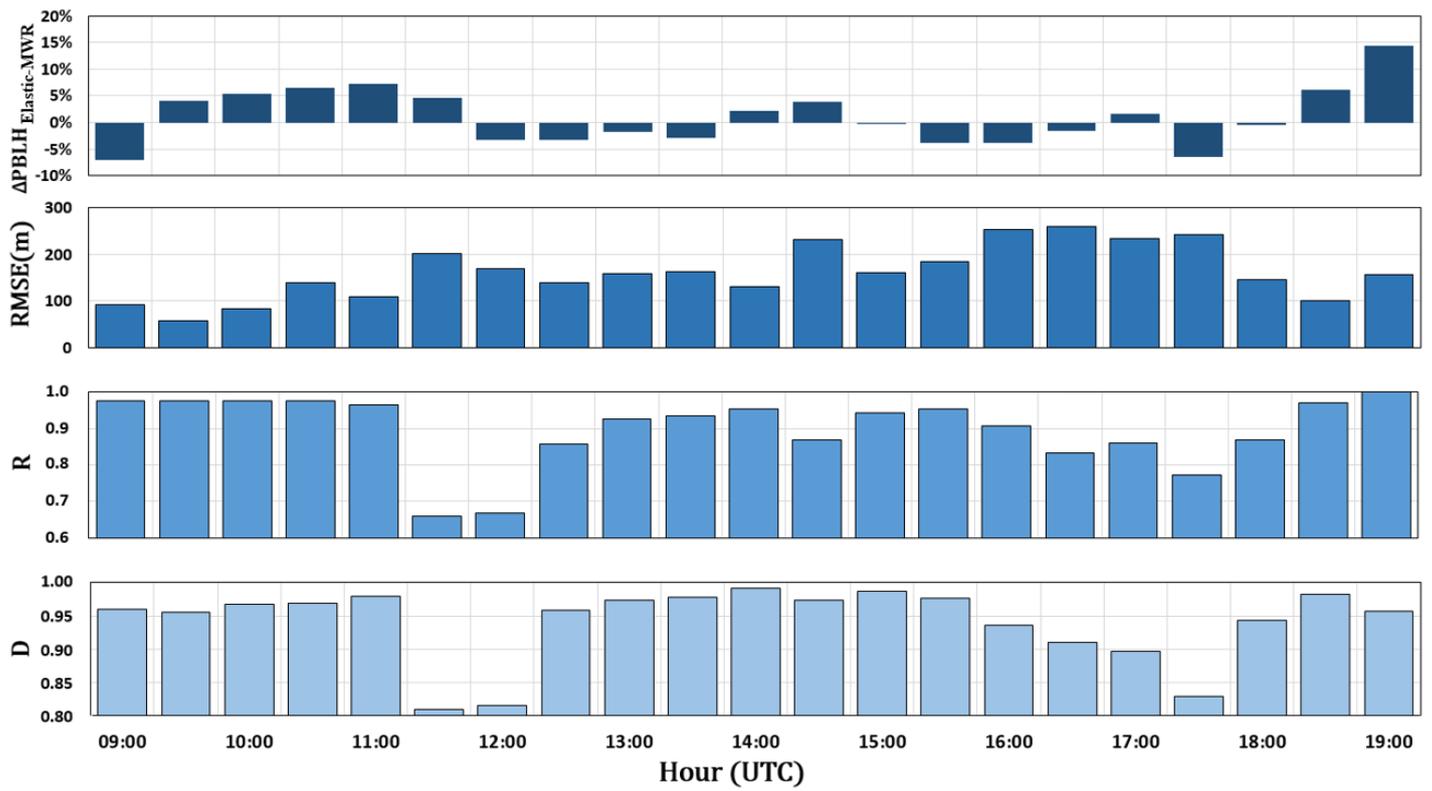


Figure 10 – Statistical comparison between the daily patterns of $PBLH_{MWR}$ and $PBLH_{elastic}$ obtained during all SLOPE-I campaign. Each bin size is equivalent to 30 minutes. $\Delta PBLH_{Elastic-MWR}$, $RMSE$, R and D represents average percentage difference, root mean square error, correlation index and index of agreement, respectively.

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